



University of the  
Highlands and Islands  
Oilthigh na Gàidhealtachd  
agus nan Eilean

# INTRODUCTION TO WELLBORE POSITIONING

**An ISCWSA initiative**

PUBLISHED THROUGH THE RESEARCH OFFICE OF UHI



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## Revisions

The authors of this publication are fully aware the nature of the subject matter covered will develop over time as new techniques arise or current practices and technologies are updated. It is, therefore, the intension of the authors to regularly revise this eBook to reflect these changes and keep this publication current and as complete as possible.

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**CONTENTS**

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### Chapter contributors

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    - David McRobbie who contributed on ‘Gyro surveying’

This book was compiled by members of the Industry Steering Committee for Wellbore Survey Accuracy (ISCWSA), a Society of Petroleum Engineers (SPE) Technical Section for Wellbore Positioning.  
The main author was Angus Jamieson.

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# Introduction to Wellbore Positioning

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# Introduction

AJ Consulting Ltd



The subject of Borehole Surveying has frequently been dealt with in best practice manuals, guidelines and check sheets but this book will attempt to capture in one document the main points of interest for public access through the UHI and SPE websites. The author would like to thank the sponsors for their generous support in the compilation of this book and their willingness to release all restrictions on the intellectual property so that the industry at large can have free access and copying rights.

After matters of health and spirit, Borehole Surveying is, of course, the single most important subject of human interest. We live on a planet of limited resources supporting a growing population. At the time of writing, the efficient extraction of fossil fuels is crucial to the sustainable supply of the energy and materials we need. Whilst renewable energies are an exciting emerging market, we will still be dependent on our oil and gas reserves for many years to come.

As an industry we have not given the accuracy and management of survey data the attention it deserves. Much better data quality and survey accuracy has been available at very little additional cost but the industry has frequently regarded accuracy as an expensive luxury. Simple corrections to our surveys such as correcting for the stretch of the drill pipe or even sag correction and IFR (see later) have been seen as belonging to the 'high tech' end of the market and we have, unlike nearly all other survey disciplines, thrown good data away, when 'better' data becomes available.

The advent of the ISWASA, The Industry Steering Committee for Wellbore Survey Accuracy, brought in a new era in survey practice. Not only was work done on improving the realism of error models, but a bi-annual forum was provided to allow industry experts to share ideas and experiences. This project has emerged out of a recognised need for better educational materials to support the understanding of borehole surveying issues. The contents of this e-book are free to use and distribute. Any additional chapters will be welcome for assessment and potential inclusion in the book so this is the first draft of a work in progress.

My thanks also go to the many participants in this effort who have contributed from their knowledge in specialist areas. In particular, to Andy McGregor who contributed the write up of the error model, Jonathan Stigant who contributed the first chapter on geodesy and John Weston, Steve Grindrod and David McRobbie who contributed other chapters on gyro surveying and magnetic spacing.

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**CONTENTS**

# Introduction to Wellbore Surveying

Compiled and co-written by

Angus Jamieson



*CONTENTS*

# 1. Coordinate Systems and Geodesy

## 1.1 The Origin – Reference Surfaces and Elevations in Mapping

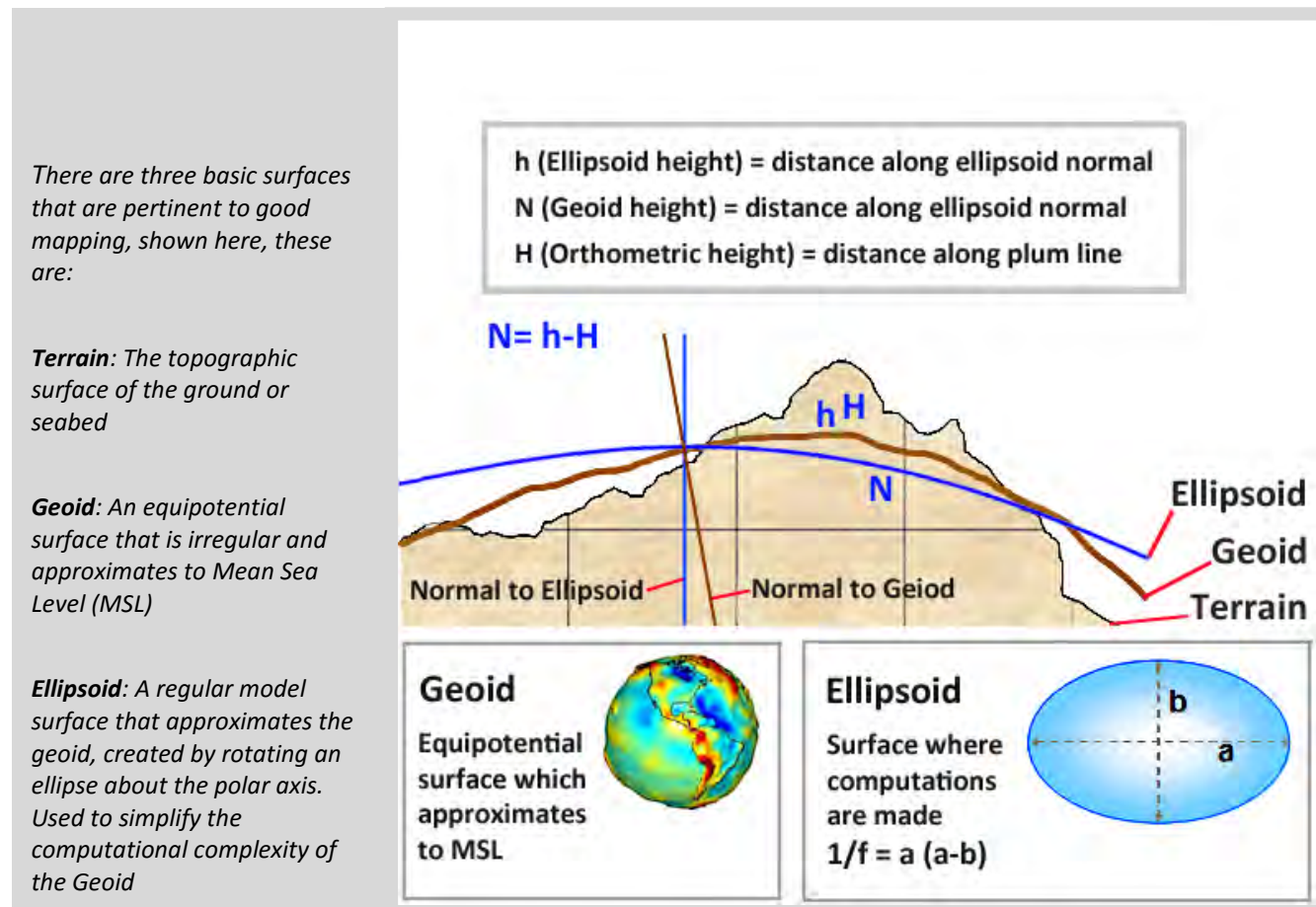


Figure 1: The three reference surfaces in geodesy

**Terrain:** The terrain is the surface we walk on or the seabed. This surface is irregular. It is the surface we have to set up our survey measuring devices, such as a 'total station' or a GPS receiver. The nature of the surface will dictate the direction of gravity at a point. In mountainous terrain, the vertical will deflect in towards the main 'centre of mass' of the mountains.

**The Geoid:** The equipotential surface of the Earth's gravity field which best fits, in a least squares sense, global mean sea level (MSL). An equipotential surface is a one where gravity is an equal force everywhere, acting normal to the surface. The geoid is an irregular surface that is too complex for calculation of coordinates.

**The Ellipsoid:** The ellipsoid is a 'model' of the Earth that permits relatively simple calculations of survey observations into coordinates. The ellipsoid provides the mathematical basis of geodesy. Note that the Geoid is an 'actual physical surface like the terrain, but the ellipsoid is a 'theoretical' surface that is designed to 'match' the geoid as closely as possible in the area of operations. Note also that the normal to the geoid (which is 'vertical') is not the same as the normal to the ellipsoid.



An ellipsoid is created when an ellipse is rotated around its polar axis. The 'mathematical' properties of an ellipse are shown in figure 2. 'a' is assigned to represent the semi-major axis or equatorial radius and 'b' the semi-minor or polar axis. The flattening, 'f', equals the ratio of the difference in 'a' and 'b' over 'a'.

### 1.1.1 MSL, Elevation and Height

Mean Sea Level is established by measuring the rise and fall of the tides. This is another 'inexact' science. The tides are affected by the juxtaposition of 'celestial' objects, most notably the moon but also the planets to varying degrees. A well-established MSL reference datum is one where tidal movement has been observed for over 18 years at what is called a 'Primary port'. The majority of countries with a coastline today have established these primary ports along that coastline and the predicted level of tides is reported by the US National Oceanographic and Atmospheric Administration (NOAA) and the UK Hydrographic Office tide tables.

LINKS [NOAA tide tables](#) [UKHO tide tables](#)

In order to tie MSL to both onshore elevations and offshore depths, these observations are tied to a physical benchmark usually in a nearby building wall or some other place unlikely to be inundated by the sea. This benchmark is quoted as a certain height above mean sea level. Sometimes MSL is used also as chart datum for the reduction of depth measurements to a common reference. Sometimes chart datum is established as the lowest level of low water, in order to provide mariners with the least possible depth at a point (i.e. the worst case). Onshore selected benchmarks represent an origin or starting point that can be used to provide the starting point for levelling across the whole country and continent.

The references for North America are the 'Sea Level Datum of 1929' - later renamed to the 'National Geodetic Vertical Datum' (NGVD 29) - and recently adjusted 'North American Vertical Datum of 1988' (NAVD 88).

Figure 1 shows the difference between heights (h) above the reference ellipsoid and the height above the geoid (H) also known as 'orthometric' height. A more general picture of this relationship with the definitions is in figure 3. The caution is that the GPS system provides 'height' above the ellipsoid, not MSL elevation. These heights have to be adjusted to make sure they match elevations from other datasets.

### 1.1.2 Coordinate Systems

There are three fundamental types of coordinate systems that are used to define locations on the Earth: 'Geocentric' coordinates measuring X, Y, Z from the centre of an ellipsoid, 'Geographical' - latitude and longitude and height (figure 3) and 'Projection' - easting and northing and elevation. Various subsets of these can also be used as '2D' consisting of only latitude and longitude or easting and northing.

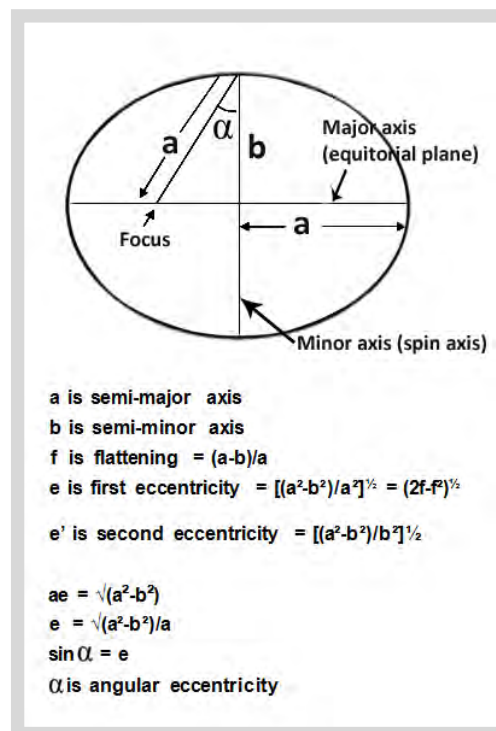


Figure 2: Mathematical properties of an ellipse

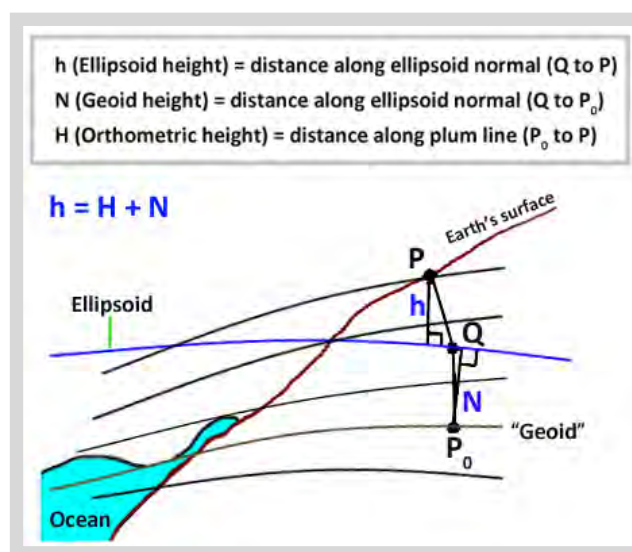


Figure 3: The relationship between surfaces

### 1.1.3 Geographical Coordinates

These are derived from an ellipsoid and the origin of the coordinates is the centre of the ellipsoid.

They are usually referenced to the 'Greenwich' meridian that runs through the Greenwich observatory just east of London in the UK. Meridians increase from  $0^\circ$  at Greenwich to  $180^\circ$  east and west of Greenwich. The 'International Date Line' runs through the Pacific and is nominally at  $180^\circ$  east or west of Greenwich. However, different island groups in the Pacific decide to be one side or the other of the Date Line, and the line is drawn at various longitudes to defer to national boundaries. On older maps the '0' meridian is not always Greenwich. There are several other reference meridians, mainly in Europe. A list of these can be found in the EPSG parameter database.

In order to facilitate loading of data in some software applications, the convention is that North and East are 'positive' and South and West are negative. However, the reader should beware that local applications that do not apply outside their 'quadrant', may not obey this convention.

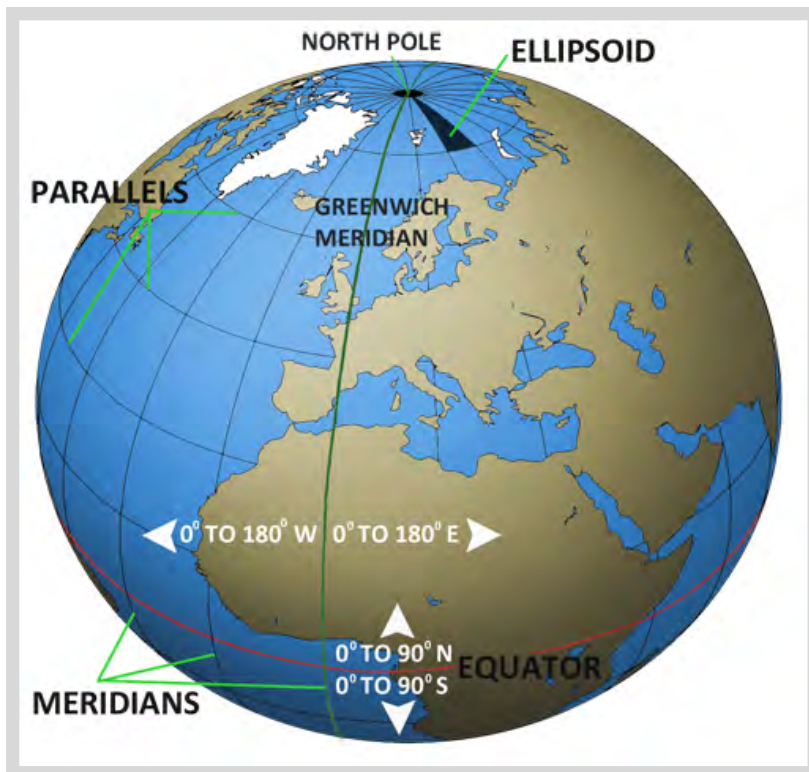


Figure 4: Geographic coordinate system

Projection coordinates are usually called eastings and northings. Sometimes they are referred to as 'x' and 'y'. However, this can be confusing as in about 50% of the world, easting is represented by 'y' and northing by 'x'. Caution is advised!

More information about how these two types of coordinate system relate will be discussed in the following chapters.



## CONTENTS

## 1.2 Principles of Geodesy – The forgotten Earth science!

Why “The Forgotten Earth Science”? Because there is a pervading ignorance of this science, but an illusion that it is inherently understood! (Daniel Boorstin)

### 1.2.1 Geodesy

Geophysics and Geology – is a study of the Earth. We use models as the other two disciplines do, and make adjustments for distortion and errors in those models.

Geodesy provides the ‘frame of reference’ for all good maps. It is the means by which we can put together all sorts of different data attributes and ensure that they are correctly juxtaposed. So while we are interested in the relative position of one piece of data to another, the means by which this is achieved is through providing an ‘absolute’ framework or set of rules that ensures that we can do this correctly. Geodesy is rightly then to be considered the underlying and immutable doctrine required to ensure that maps (the cartographers ‘art’) properly represent the real world they are designed to portray.

Geodesy is defined as the study of:

- the exact size and shape of the Earth
- the science of exact positioning of points on the Earth (geometrical geodesy)
- the impact of gravity on the measurements used in the science (physical geodesy)
- Satellite geodesy, a unique combination of both geometrical and physical geodesy, which uses satellite data to determine the shape of the Earth’s geoid and the positioning of points.

Let us return to the ellipsoid that we studied in the previous section (figure 5). This time, I have ‘cut away’ a quadrant of the ellipsoid so we can see the centre. On this diagram we can see two coordinate systems. One is the Latitude, Longitude and Height of a point ‘P’ in space above the ellipsoid surface (it could just as well be below). The other is a three dimensional Cartesian coordinate system where X is in the direction of the Greenwich meridian in the equatorial plane, Y is orthogonal to the Greenwich meridian and Z is parallel to the polar axis (orthogonal to the other two axes). The Cartesian system is directly referenced to the ellipsoid centre, the geographic system is directly referenced to the ellipsoid surface and indirectly to the ellipsoid centre. However, both systems are valid and both describe in different ‘numbers’ the coordinates of the point ‘P’.

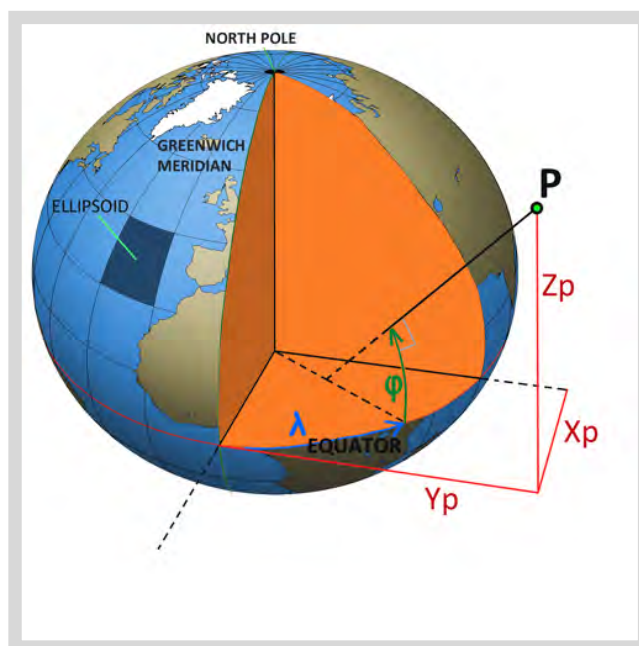


Figure 5: Ellipsoid coordinate reference systems

The relationship between the two systems is per the following algorithms:

$$X = (v + h) * \cos \phi * \cos \lambda$$

$$Y = (v + h) * \cos \phi * \sin \lambda$$

$$Z = [(b^2 * v/a^2) + h] * \sin \phi$$

(where ‘v’ is the radius of the ellipsoid at P).

### 1.2.2 Geodetic Datum

One of the most important lessons in geodesy is the next step. How do we tie the ellipsoid to the real world? Now that the model is set up, we have to attach it to the real world. Here is the definition of a 'Geodetic Reference Datum':

*A Geodetic Datum is an ellipsoid of revolution attached to the Earth at some point. There are two types:*

- *Astro-Geodetic (Regional usage)*
- *Global (Global application)*

We move from simply an ellipsoid, 'floating' in space to a 'geodetic reference datum'. There are two valid ways to do this, the historic, astro-geodetic (regional), pre-navigation satellite days method and the global method using satellite orbits.

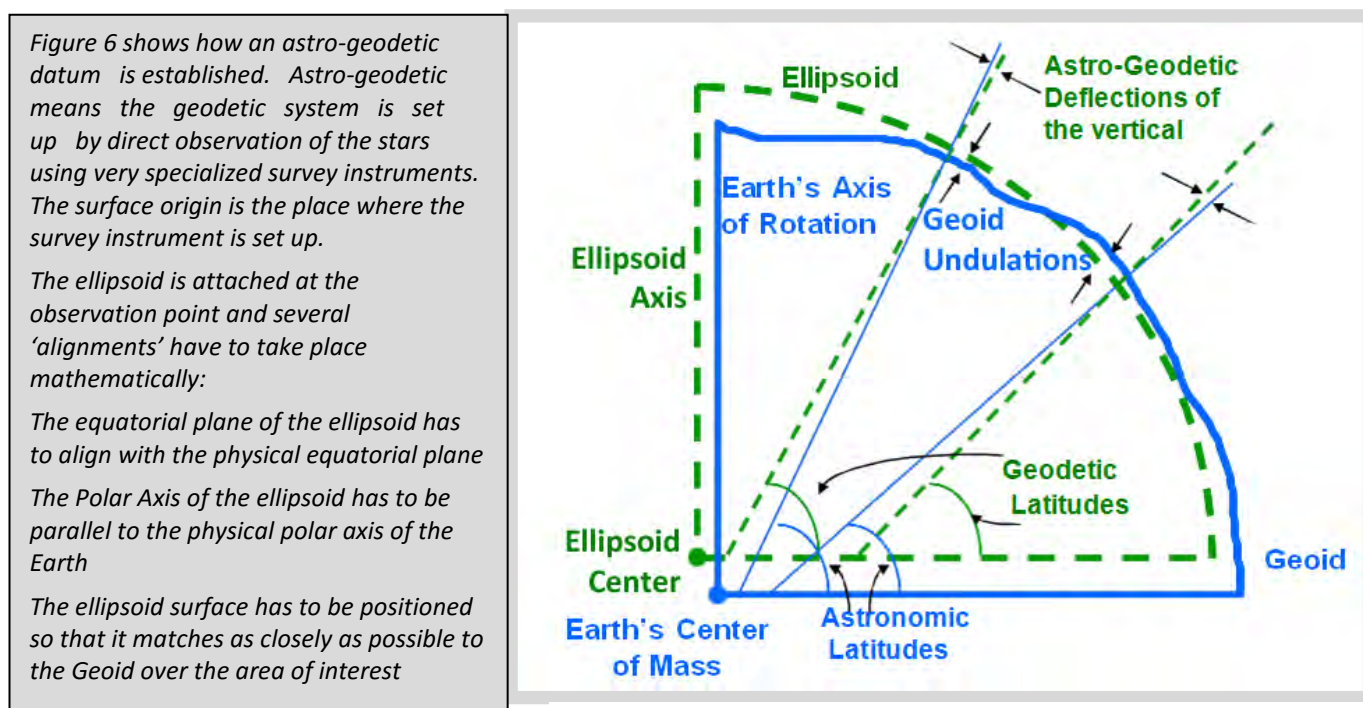


Figure 6: Establishing an Astro-geodetic Datum

**In figure 6, note three significant issues:**

1. Astro-geodetic (geoid referenced) latitudes are not quite the same as geodetic (ellipsoid referenced) latitudes. This due to the slight difference in the normal to the respective surfaces. This is the model 'distortion' due to using an ellipsoid. If the region covered is a continent like the USA or Russia, then as the datum network is spread across the land then least squares corrections called 'Laplace' corrections have to be made to minimize the distortion.
2. They take much time to observe under demanding accuracy conditions which can be affected by the weather.
3. They are subject to the observation idiosyncrasies of the observer. Relative accuracy between datums established in the same place by different observers can be several hundred meters.

The drawback of the astro-geodetic method is that it is only useful over a specified region, and in general cannot be carried across large expanses of impenetrable terrain or water, since inter-visibility is required. Thus in archipelagos, like Indonesia, this can result in a large number of small regional datums none of which quite match with the others. Political boundaries can also mean a multiplicity of datums even in contiguous land masses; West Africa is a good example, where each country has its own unique astro-geodetic datum. Figure 7 shows a global view of continental regional datum 'blocks'. Eight datums to cover the world does not seem so difficult, but in fact there are well over 100 unique astro-geodetic datums. Figure 8 shows the proliferation of datums in SE Asia.





Figure 7: The World's Major Datum Blocks

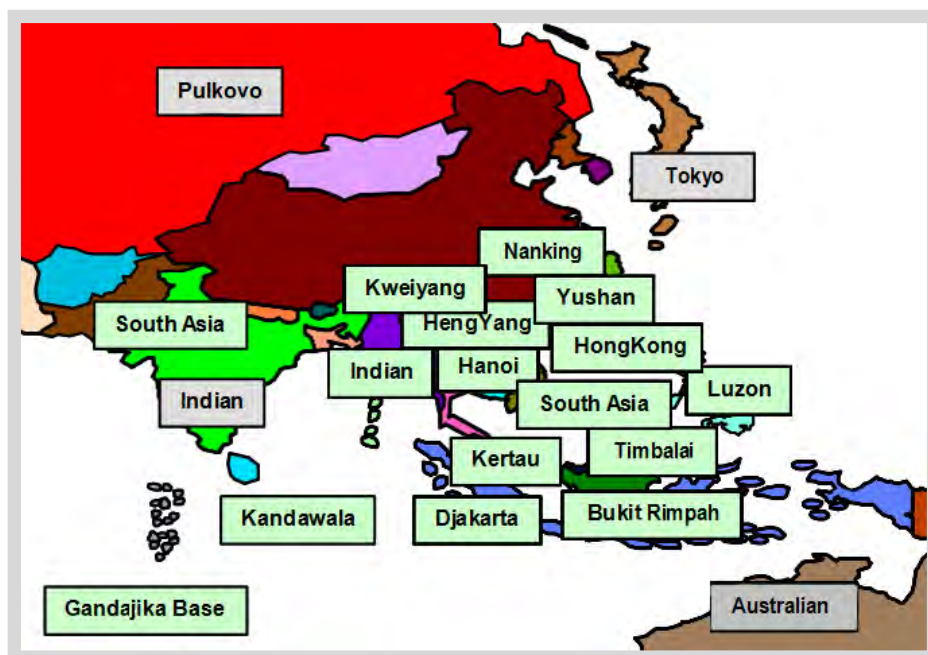


Figure 8: The multiplicity of Astro-geodetic datums in the Indonesian Archipelago

A global datum is a datum that is established to model the entire global geoid as closely as possible; something an astro-geodetic datum cannot do. A global datum is established by observing the orbit of navigation satellites, calculating the Earth's centre of mass based on the orbits and then adjusting the ellipsoid by harmonic analysis to fit the global geoid. There have been several variants, but the two primary ones are WGS 72 and WGS 84. WGS stands for World Geodetic System. The WGS 72 datum was established for the 'Transit Doppler' satellite system, WGS 84 was established for the GPS system. The 'connection' point or origin for the global datums is the Earth's centre of mass. Due to iterative improvement of the gravitational analysis, the centre of mass is slightly different for WGS 72 and WGS 84.

Figures 9 to 12 show, in cartoon form, the juxtaposition of two astro-geodetic datums with the geoid and a global datum. In figure 9 we see the geoid. There is an outline for representation in the other figures. In figure 10 red and green astro-geodetic datums are shown connected to the surface at two different points. The differences are exaggerated for effect. Figure 11 shows the geoid and the global datum. Figure 12 shows all three ellipsoids juxtaposed with the center of the ellipsoids clearly shown in three different places (again exaggerated for effect). Since latitude and longitude are referenced to the centre of the respective ellipsoid, it is clear that a latitude and longitude on one datum will not be compatible with a latitude and longitude on another datum unless some sort of transform takes place to adjust the one to match the other.

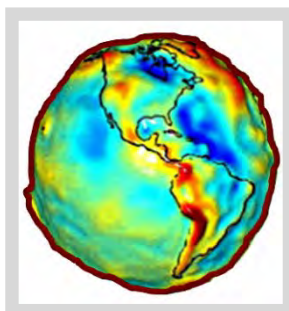


Figure 9: The geoid and an outline of the geoid

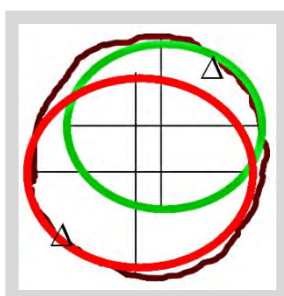


Figure 10: Ellipsoid attached to the earth in two different places

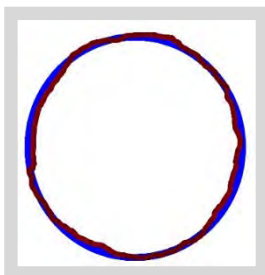


Figure 11: Global' ellipsoid attached to the earth's center of mass

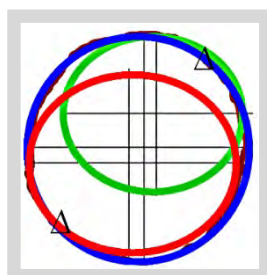
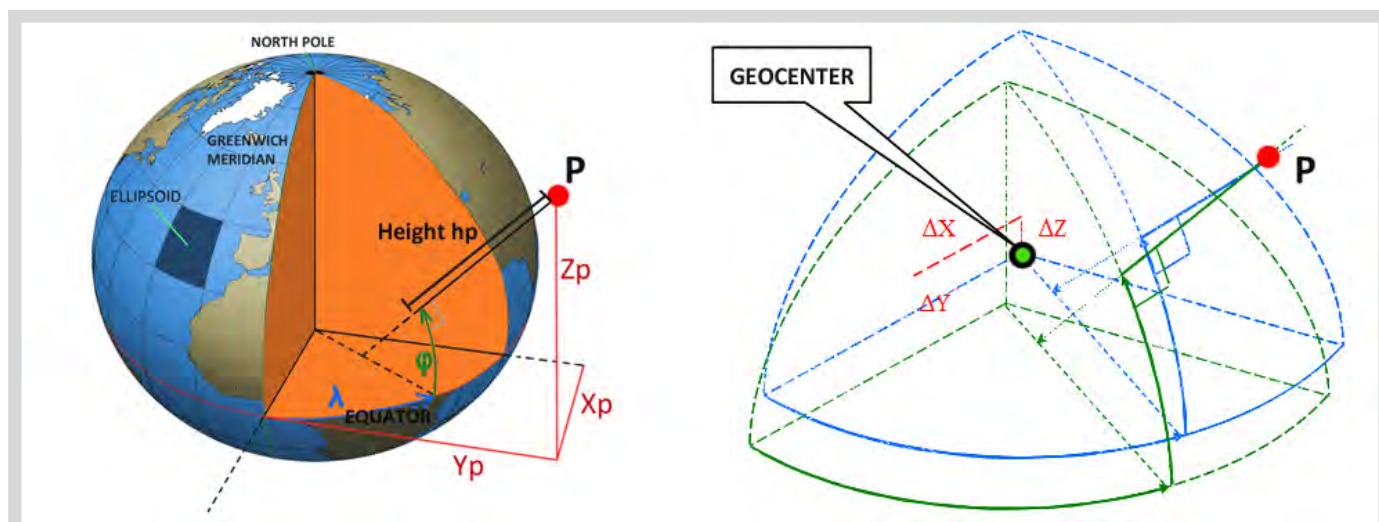


Figure 12: All three datums ellipsoids attached to the earth

Reference Datum Transformation: Figure 13 shows a global (blue) and an astro-geodetic or regional datum (green), with the offset of the two centres. In order for a coordinate on the blue datum to be transformed to the green datum, the latitude and longitude have to be converted to  $x,y,z$  Cartesian coordinates on the blue datum. The  $dx, dy, dz$  have to be applied giving the  $x,y,z$  on the green datum. This can then be converted back to latitude and longitude on the green datum.

Numerically these two sets of coordinates will be different but they will continue to represent the same physical point in space, as can be seen in figures 13 and 14. The corollary is that coordinates referenced to one datum

Figure 13: A global datum (blue) and a regional/astro-geodetic datum (green) and the application of the geocentric transformation



that are mapped in a different datum will appear in the wrong place! The reader should note that in some of the larger regional datums, there are a variety of 3 parameter datum transformation sets depending on where in the region the operator is working (figure 14).

Figure 14 shows three latitude and longitude locations referenced to different geodetic datums that all represent the same point. The differences in the right-hand two columns shows the error in mapped location if the datums are confused.

Datum	Latitude	Longitude	Local to WGS84	Local to Local
<u>Aratu</u>	20° 36' 13.2757"N	38° 56' 56.3341"W	236.7 meters	220.56 meters
SAD69	20° 36' 17.4283"N	38° 56' 50.1240"W	65.12 meters	
WGS84	20° 36' 19.2794"N	38° 56' 51.2166"W		

Figure 14: Lat/long locations on different geodetic datums

Datums in China are WGS 84, WGS 72 BE, Beijing 1954 and Xian 1980. Note the difference in the parameters for the Beijing datum in the Shows various datum transformation parameters in China as they relate to WGS 84 Ordos and Tarim basin, both three parameter transformations and the difference between the South China Sea and the Yellow Sea seven parameter transformations.

These are captured in the EPSG parameter database. Note also there are more sophisticated methods of calculating the datum transformation which may appear in various applications. These include parameters that not only translate but also allow for rotation and scaling differences between the two datums. The EPSG parameter database also contains many of these. Care should be taken when applying such parameters, and it is best to obtain the services of a specialist when using them or coding them into software. For most applications in the E&P domain, a three parameter shift will provide the necessary accuracy. In some countries more elaborate parameters are required by law.

LINK [EPSG parameter database](#)



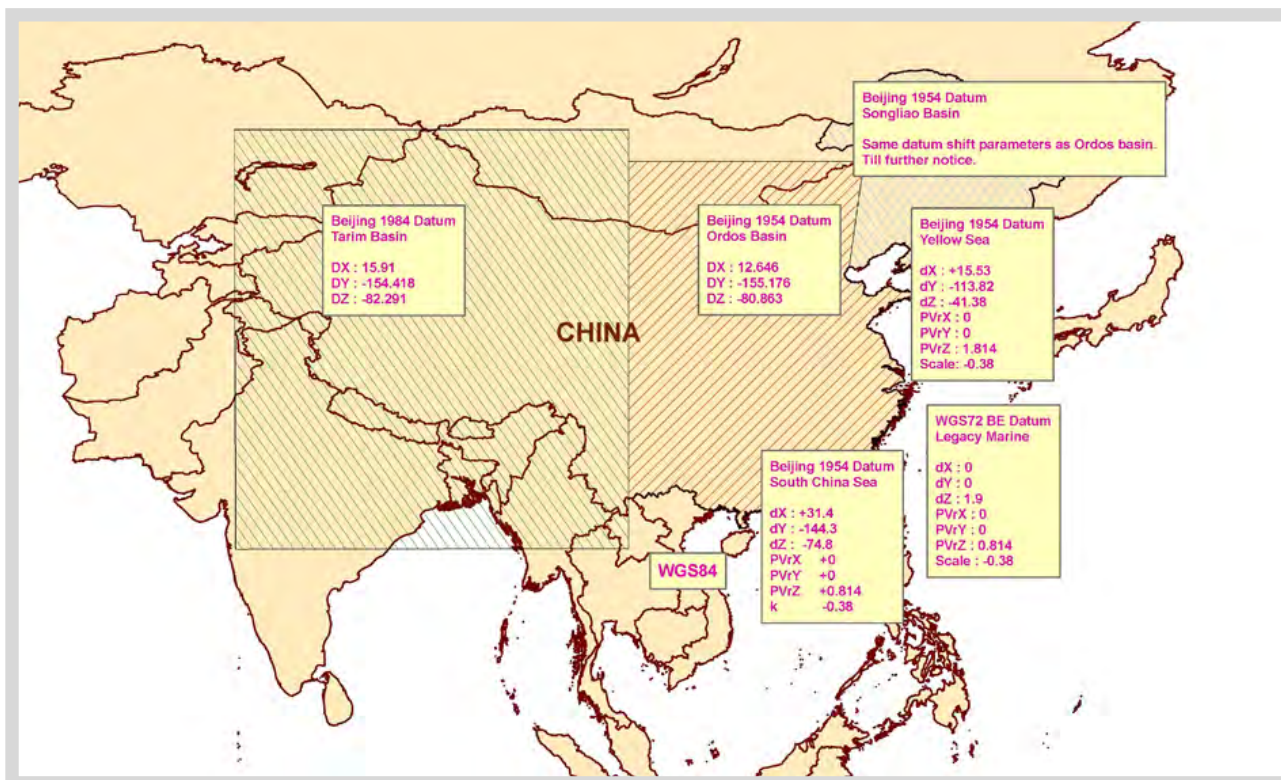


Figure 15: Datum transformation parameters in China

### 1.2.3 Distortions in the Ellipsoidal Model

As the reader will have surmised, the ellipsoidal model is not an exact fit. The larger the area covered by a datum, the more distortion there is.

**Height and Elevation** – the elevation above MSL is not the same generally as the height above the ellipsoid. Corrections must be made to GPS or other satellite derived ‘heights’ to adjust them to mean sea level. Measurements made and adjusted to mean sea level by the surveyor may be assumed to lie on the ellipsoid as long as the separation between the two surfaces is relatively small.

Related to the previous one, the direction of the local vertical is not the same as the normal to the ellipsoid. This difference is known as the ‘deflection in the vertical’ and has to be minimized especially across larger regional and continental datums. This is done using Laplace corrections at regular intervals across the area of interest. Since these corrections vary in a non-regular and non-linear manner, the datum transformation between two datums may vary significantly across larger datums. The EPSG database is a means of identifying where a particular set of parameters should be used.

**Radius of curvature adjustment** (Figure 16) – The ellipsoid has a radius of curvature at a point (varies across the ellipsoid). When measuring distances at heights above or below the ellipsoid of more than about 5000 ft, the distances need to be adjusted to allow for the change in radius of curvature, so that they ‘map’ correctly onto the ellipsoid. Measurements made above the ellipsoid need to be reduced and measurements made below the ellipsoid need to be increased respectively, so that a map of the area (computed at the ‘true’ ellipsoid radius) map correctly onto the map in relation to other features. The calculation can be made with the following equation:

**Ellipsoidal length =  $d[1 - (h/(R + h))]$**  where

d = measured length

h = mean height above mean sea level (negative if below)

R = mean radius of curvature along the measured line



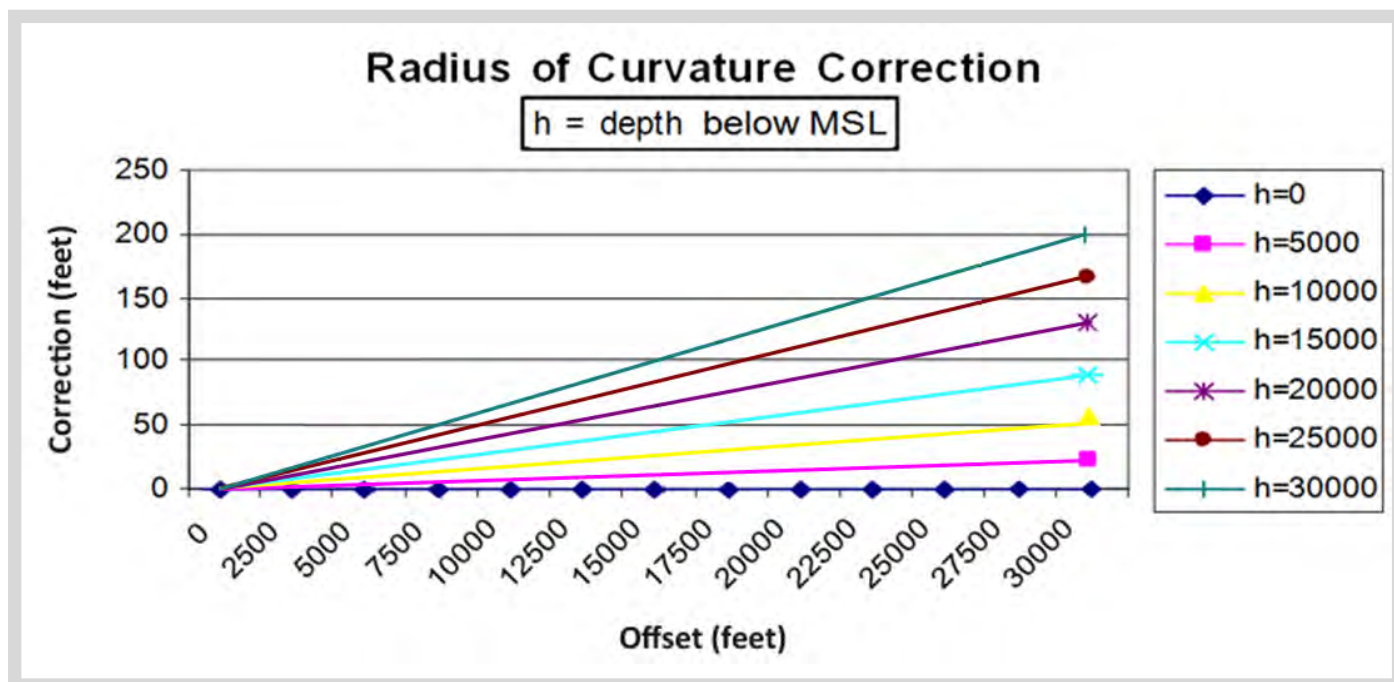


Figure 16: The increase in offset correction with depth and offset distance

## Section summary

### The most important lessons:

The most important lesson from all this is that a latitude and longitude coordinate do not uniquely define a point in space unless the datum name is included as part of the description! Please also note that knowing the name of the ellipsoid is not enough. An ellipsoid is a shape in space and the same ellipsoid can be attached to the Earth at an infinite number of places. Each time an ellipsoid is attached to another place it represents a different datum. Particular examples occur in West Africa, where many countries use the Clarke 1880 ellipsoid but set up as a different astro-geodetic datum in each case, and in Brazil where three datums use the International ellipsoid of 1924.

### Ten Things to Remember about Geodesy and References:

1. Latitude and Longitude are not unique unless qualified with a Datum name.
2. Heights/Elevations are not unique unless qualified with a height/elevation reference.
3. Units are not unique unless qualified with unit reference.
4. Orientations are not unique unless qualified with a heading reference.
5. Most field data of all types are acquired in WGS 84 using GPS.
6. Every time data are sent somewhere there is a chance someone will misinterpret the references.
7. Most datasets have an incomplete set of metadata describing the references.
8. All software applications are not created equal with respect to tracking and maintaining metadata.
9. Data can be obtained by anyone from anywhere – that doesn't make it right!
10. Most people do not understand geodesy - if you are in doubt – check with someone who knows!



## 1.3 Principles of Cartography – It’s a ‘Square World’! Or is it?

The foundation is the datum. Geographic coordinates (latitude and longitude) describe points in the datum. These are then converted into Projection coordinates.

Without knowledge of the datum, projection coordinates are not unique and can easily be wrongly mapped

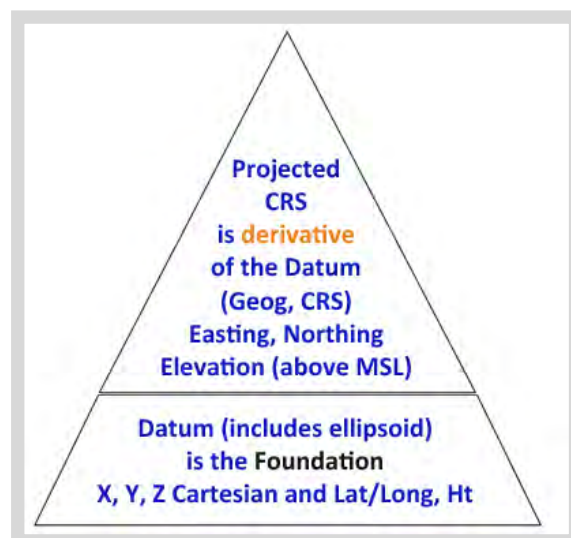


Figure 17: The hierarchy of mapping

Why is it necessary to project geographic coordinates? We do this for three primary reasons:

- Ease of communication
- Ease of computation
- Presentation and Planning

### 1.3.1 Projection Categories

Figure 18 shows the various surfaces and orientation of the surfaces with respect to the ellipsoid axes. The three surfaces for projecting the ellipsoid are a cylinder, a cone and a plane. The main projection types used in E&P are *Transverse Mercator* and *Lambert Conformal Conic*.

Other projection types that occur less frequently are: *Mercator*, *Oblique Mercator (Alaska)* *Oblique Stereographic (Syria)*, *Albers Equal Area*. The majority of the standard projections in use in E&P are listed with parameters in the EPSG database.

There are many ‘standard’ projection parameter definitions, but a project projection can be custom designed for specific purposes if needed. In general, one or two of the following criteria can be preserved when designing a projection:

**Shape**  
**Area**  
**Scale**  
**Azimuth**

The majority of the projections we use are conformal. This means that scale at a point is the same in all directions, angular relationships are preserved (but not necessarily north reference) and small shapes and areas are preserved.

They are also generally computational.

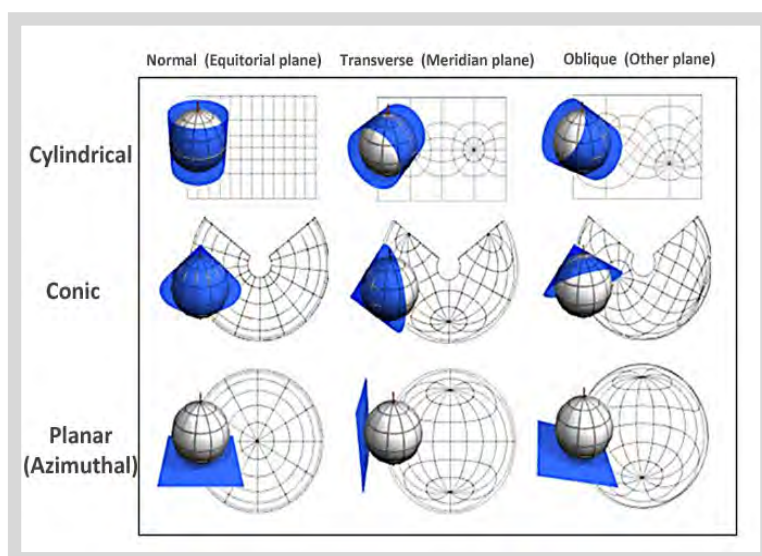


Figure 18: Types of projection based on various plane / orientation of surfaces

Figure 19 shows that making the plane surface secant to the ellipsoid allows for a greater area to be covered with an equivalent scale distortion.

LINK [EPSG parameter database](#)

### 1.3.2 Mapping Parameters

A projection requires a set of parameters that are used to convert between latitude and longitude and easting and northing. These parameters can be found in the EPSG geodetic parameter database.

For a Transverse Mercator projection and a Lambert Conformal Conic projection these are respectively:

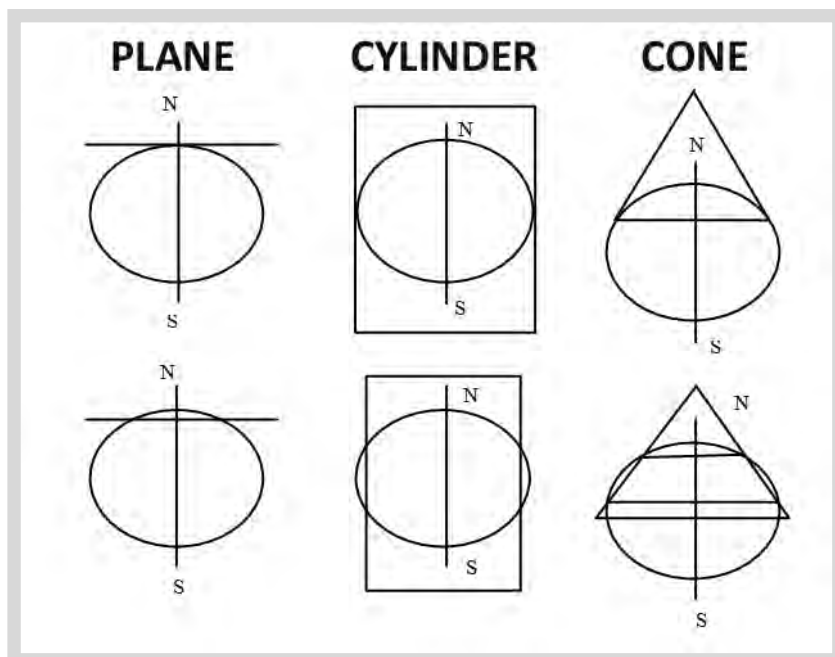


Figure 19: The plane surface to the ellipsoid

<b>Datum</b>	<i>e.g. NAD83</i>
<b>Projection Type</b>	<i>e.g. Transverse Mercator</i>
<b>Projection Name</b>	<i>e.g. Mississippi State Plane Coordinate System</i>
<b>Zone Name</b>	<i>e.g. West</i>
<b>Central Meridian</b>	<i>e.g. 90° 20' W</i>
<b>Latitude of Origin</b>	<i>e.g. 29° 30' N</i>
<b>Central Scale Factor</b>	<i>e.g. 0.99975</i>
<b>False Easting</b>	<i>e.g. 2,296,583.333 (NB = 700,000 meters)</i>
<b>False Northing</b>	<i>e.g. 0</i>
<b>Units</b>	<i>e.g. US Survey feet</i>

<b>Datum</b>	<i>e.g. NAD27</i>
<b>Projection Type</b>	<i>e.g. Lambert Conformal Conic</i>
<b>Projection Name</b>	<i>e.g. Texas State Plane Coordinate System</i>
<b>Zone</b>	<i>e.g. South Central</i>
<b>Central Meridian</b>	<i>e.g. 99° 00' W</i>
<b>Latitude of Origin</b>	<i>e.g. 27° 50' N</i>
<b>*North Standard Parallel</b>	<i>e.g. 30° 17' N</i>
<b>*South Standard Parallel</b>	<i>e.g. 28° 23' N</i>
<b>False Easting</b>	<i>e.g. 2,000,000</i>
<b>False Northing</b>	<i>e.g. 0</i>
<b>Units</b>	<i>e.g. US Survey feet</i>

The geographic origin is the intersection of the central meridian with the latitude of the origin. The projection origin values at that point are the false easting and false northing. The reason for the high positive values for these parameters where applicable, is to avoid negative values. In both cases above this is for the easting but is not necessary for the northings which are both '0', as the projection is not intended for use south of the origin.

There are several other types of projection, most of which are of more interest to cartographers than having any application in E&P.

### 1.3.3 Distortions in Mapping

We have already seen in the Geodesy section above, that by modelling the Geoid using an ellipsoid, we have already introduced some distortion in the way that the Earth is represented. Without adjustment, that distortion increases as we proceed further from the point of origin where the datum was established. However, with a well-established datum, these distortions can be minimized. When we make calculations from the Earth's surface to a flat (projection) surface, we introduce an additional set of distortions. These are in area, shape, scale and azimuth.

These distortions:

- Can be calculated and understood, but without proper care and well educated workforce, it is easy to make mistakes.
- Are non-linear; that is to say, the size of the distortion varies across the projected area are very important component in mapping wellbores.

The most important and potentially destructive distortions when projecting geospatial data to a map are scale and orientation, particularly when mapping wellbore positions. Figure 18 shows a 'macro' level example of scale and azimuth distortion. This effect happens even at short distances but not so obviously to the eye. The orientation or azimuth change is what is called convergence. Its value can be calculated and applied to 'real world' measurements to adjust them to projection north referenced value. Similarly scale distortion can be applied to survey measurements to represent a scaled distance on the map.

### 1.3.4 Azimuth Distortion

A key point to remember is that the projection central meridian is truly a meridian - there is no azimuth distortion. As one moves away from the central meridian east or west, the other meridians plot on the projection as curved lines that curve towards the nearest pole, whereas grid north lines are parallel to the central meridian. At any given point, the difference in azimuth between the grid north lines and the meridian lines is the convergence angle. On the equator, convergence is generally zero also, and increases as one moves north. Figure 20 shows a 'global' cartoon view of the concept.



Figure 20: The plane surface can be tangent or secant to the ellipsoid. Secant even the distortion.

Figure 21 shows a simple way to verify that the value derived is correct (i.e. that the sign of convergence has been correctly applied). It is important when dealing with convergence to do a couple of 'sanity' checks:

- Always draw a diagram (Figure 21)
- Always check that the software application is applying the correct value, correctly
- Always have someone else check that the results agree with supplied results of wellbore location
- If you are not sure – find a specialist. The formal algorithm is  $Grid\ azimuth = True\ Azimuth - Convergence$  but many applications do not observe the correct sign. It is better to use  $True\ Azimuth = Grid\ Azimuth \pm Convergence\ \alpha$  where (per figure 21),  $\alpha$  -ve West of CM, and  $\alpha$  +ve East of CM in Northern hemisphere and the opposite in Southern hemisphere.

In the equation above, use the sign in the diagram, not the sign you get with the software, because some applications use the opposite convention.

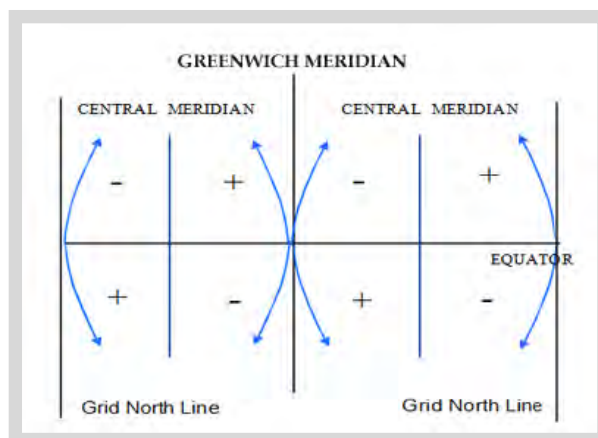


Figure 21: Two projection zones with Central Meridians

Figure 21 shows two project zones with Central Meridians, as well as non-central meridians plotted on the projection (curved lines) that converge towards the nearest pole. Two additional grid north lines are shown to the right and left of the figure. Grid north lines are parallel on the projection, creating a grid. Convergence and scale sign distortion vary in a non-linear fashion across the projection, but can be calculated for any given point.

### 1.3.5 Scale Distortion

Referring back to figure 21, it is clear from the example that a projection will distort the distance between two points. Clearly the true (Earth surface measured) distance between Anchorage and Washington DC has not changed, but the length on the map can change depending on the projection. Most projections we use have a sub unity 'central scale factor'. In the example above the Mississippi West state plane projection has a central scale factor of 0.99975. This means that on the central meridian a 1,000 meter line measured on the ground will be represented by a line 999.75 meters at the scale of the map. If the map has a scale of 1:10,000, then the line on the map will be represented by a line 9.9975 cms long. If you plotted the same line on the central meridian of a UTM projection with a central scale factor of 0.9996, then the line on the map would be represented by a line 9.996 cms long.



**CONTENTS**



## 2. Changing from One Map System to Another

### 2.1 Ellipsoids and Datums

This is covered in more detail in the Geodesy section above but here are some basic guidelines.

The Earth is elliptical in cross section due to the fact that the planet is mainly molten rock and the rotation of the Earth causes a slight 'flattening' as the centrifugal force throws the mass of liquid away from the centre of spin.

A datum by definition is an ellipsoidal model of the Earth and a centre point. Historically we have estimated the dimensions of the ellipsoid and its centre from surface observations and the best fit datum has naturally varied from region to region around the world. For example, in the USA, an elliptical model and centre point was chosen in 1927 and is referred to as the NAD 27 datum.

It uses the Clarke 1866 Ellipsoid (named after Alexander Ross Clarke a British Geodesist 1828 - 1914 with dimensions as follows:

Semi-Major Axis: 6378206.4 metres

Semi-Minor Axis: 6356583.8 metres

Whereas in 1983 the datum was updated to NAD 83 which uses a spheroid as follows:

Semi-Major Axis: 6378137 metres

Semi-Minor Axis: 6356752.3 metres

Not only did the shape update but the centre point shifted by several hundred feet. In order to correctly convert from one system to another, the latitude and longitude have to be converted to an XYZ coordinate from the estimated centre of the Earth (Geo Centric Coordinates). After that a shift in the coordinates to allow for the shift between the centre estimates is applied. Then the coordinates can be converted back to a vertical angle (latitude) and horizontal angle (longitude) from the new centre on the new ellipsoid. In some cases, there may be a scale change and even a small rotation around the three axes so it is not recommended that a home-made calculation is done for such a critical and sensitive conversion.

Latitude and Longitude for a point are NOT UNIQUE. They depend on the centre point and spheroid in use.

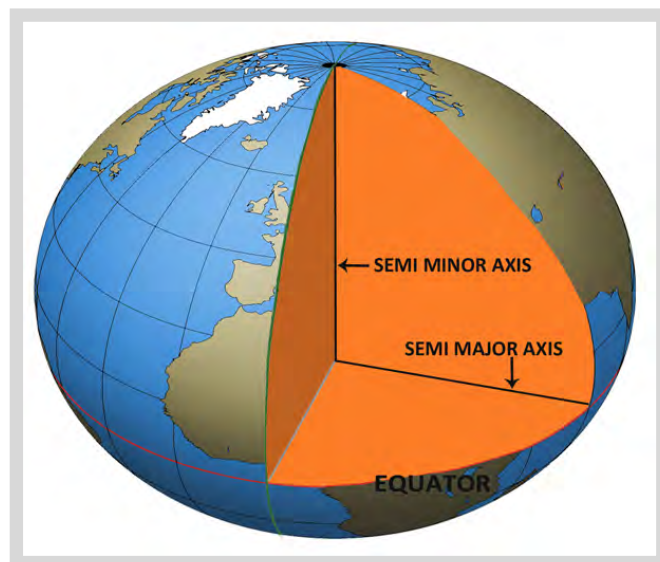


Figure 22: Earth's elliptical cross section

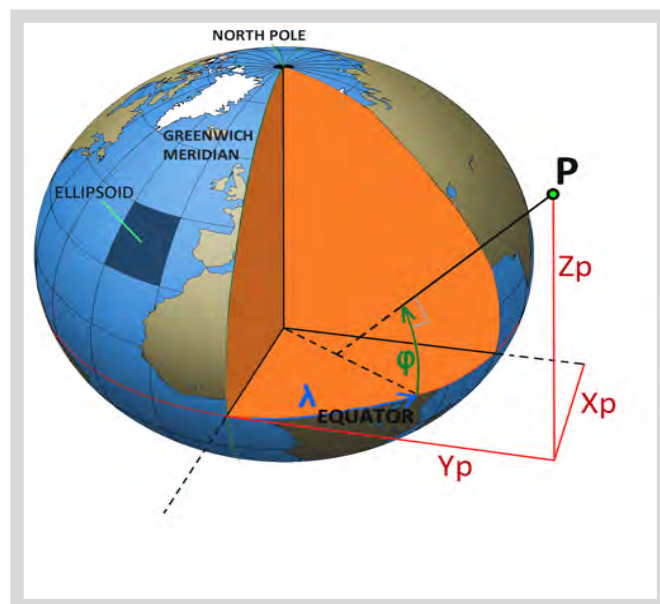


Figure 23: Geo Centric XYZ coordinates

It is worth checking out the EPSG web site. This is the internet domain of the European Petroleum Survey Group which maintains an accurate database of geodetic parameters and provides on line software for doing such conversions.

LINK [EPSG website](#)

Here, for example is the conversion of a point at 30 degrees North latitude and 70 degrees West Longitude from NAD 27 to NAD 83.

	Latitude	Longitude
NAD 27 datum values:	30 00 0.00000	70 00 0.00000
NAD 83 datum values:	30 00 1.15126	69 59 57.30532
NAD 83 - NAD 27 shift values:	1.15126 (secs)	-2.69468(secs)
	35.450 (meters)	-72.222(meters)
Magnitude of total shift:	80.453(meters)	

The main consideration here is that it is essential that when positioning a well, the geoscientists, the operator and the drilling contractor are all working on the same map system on the same datum as the shift in position can be enormous and frequently far bigger than the well target tolerance.



## CONTENTS

## 3. True North, Grid North, Convergence Summary & Exercises

### 3.1 Map Projections

For any point on the Earth's surface True North is towards the Geographic North Pole (The Earth's axis of revolution).

This fact is independent of any map system, datum or spheroid. However, when a map projection surface is introduced, it is impossible to maintain a parallel map North that still meets at a single point.

In this example a vertically wrapped cylinder such as those used in Transverse Mercator map projections includes the North Pole but the straight blue line on the globe will become slightly curved on the surface of the cylinder. The black line in the diagram shows the direction of Map North (Grid North) and clearly they are not the same.

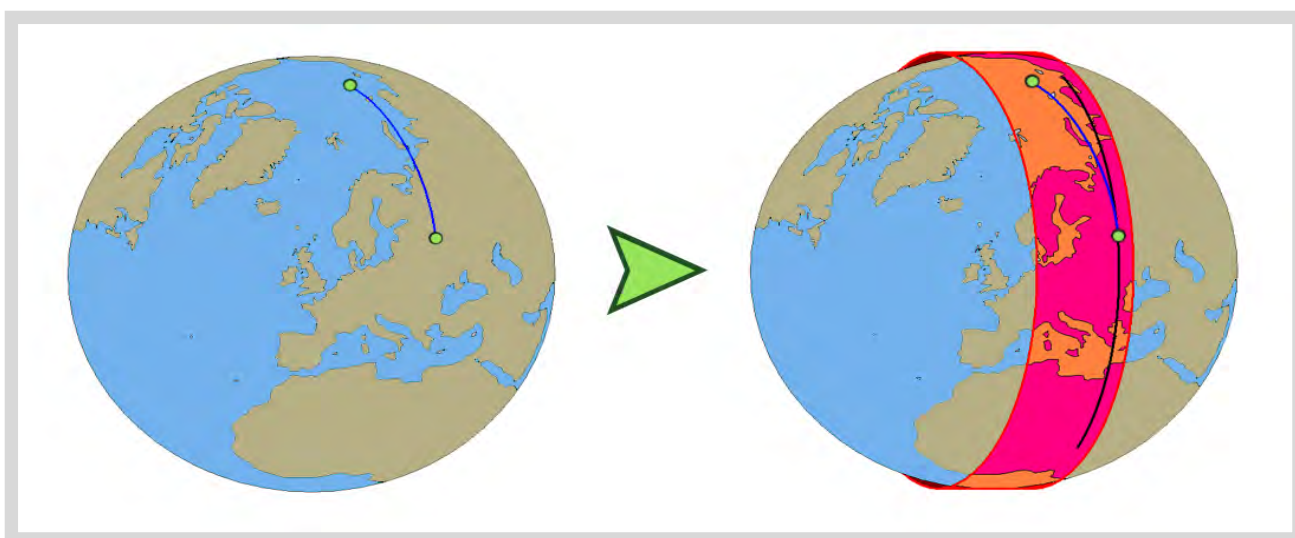


Figure 24: Map projection surface for parallel map North

When the cylinder is unwrapped, the two lines look like figure 25.

Because all True North lines converge to a single point, the angle from True to Grid North is referred to as the 'Convergence' Angle.

**Convergence is the True Direction of Map North.**

In the case of the Universal Transverse Mercator Projection, the convergence within one map zone can vary from -3 degrees to +3 degrees.

When correcting a true North Azimuth to Grid, this convergence angle must be subtracted from the original azimuth. It is essential that a North Arrow is drawn in order to correctly visualize the relative references.

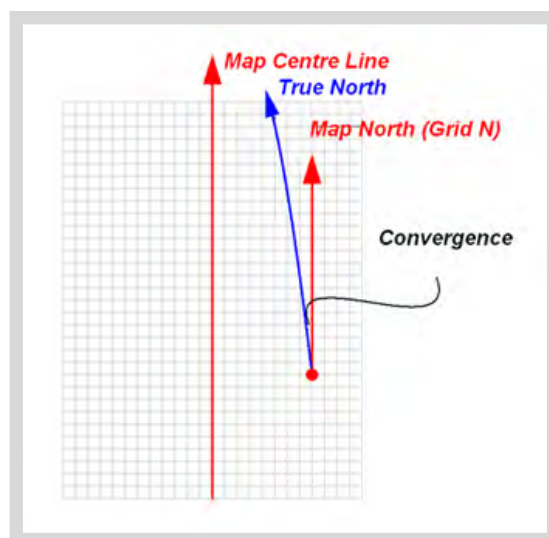


Figure 25: The 'Convergence' Angle



When magnetic north is included (see next chapter) we have three different North References to contend with.

These can be in any order with several degrees of variation between them so a clear North Arrow is essential on all well plans and spider maps.

When correcting from one reference to the other it is common practice to set the company reference North straight upwards and plot the others around it. In figure 26 & 27, Grid North is the preferred company reference, so all quoted azimuths would be referenced to Grid and the North arrow is centred on Grid North.

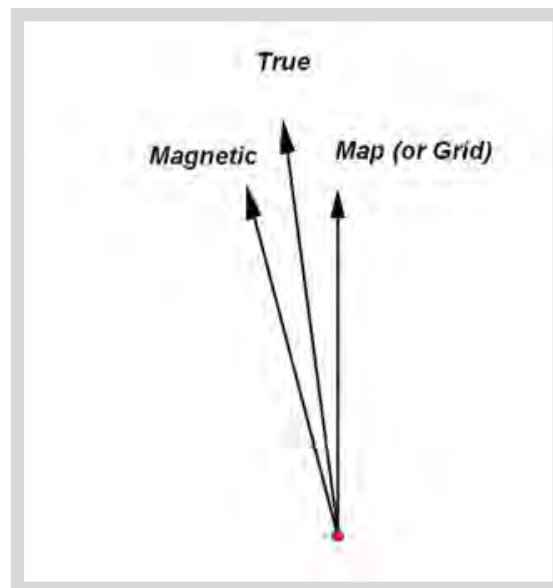


Figure 26: The three north references

In this example the well is heading  $60^\circ$  Grid with magnetic North at  $6^\circ$  west of True and Grid North  $2^\circ$  East of True - figure 27. Depending on which reference we use, the azimuth can be expressed three different ways. It is easy to see how confusion can occur.

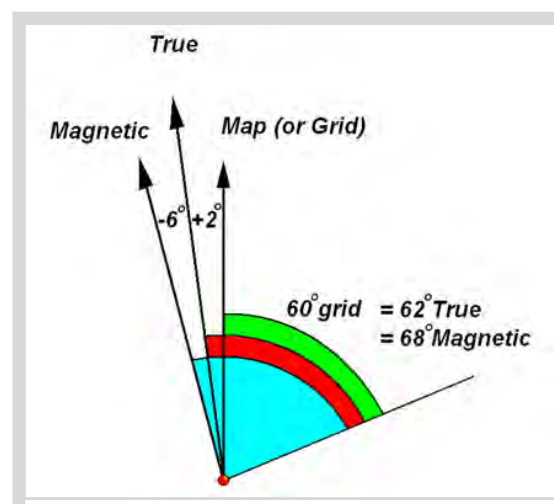


Figure 27: The Convergence angle calculation

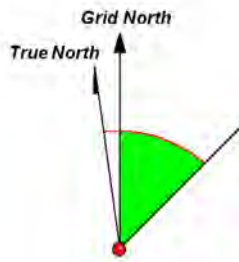
Worked examples follow on the next pages.....



CONTENTS

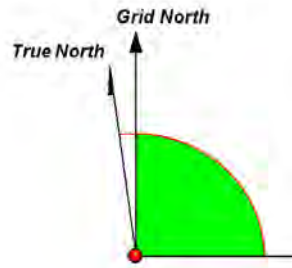
Some simple worked examples:

Example 1



Grid Convergence is +2.5  
 True Direction is 47.5  
 What is the Grid Direction  
 It's 45 degrees

Example 2



Grid Convergence is +1.8 degrees  
 True Direction is 91.8 degrees  
 What is the Grid Direction  
 It's 90 degrees

Example 4



Grid Convergence is - 0.7 degrees  
 True Direction is 312.4 degrees  
 What is the Grid Direction  
 It's 313.1 degrees



Magnetic Declination is - 8 degrees  
 Magnetic Direction is 88 degrees  
 What is the True Direction  
 It's 80 degrees  
 And if the Convergence was -2  
 What would be the Grid Direction  
 It's 82 Degrees

Example 5



Magnetic Declination is - 8 degrees  
 Magnetic Direction is 88 degrees  
 What is the True Direction  
 It's 80 degrees

## Extended example 1

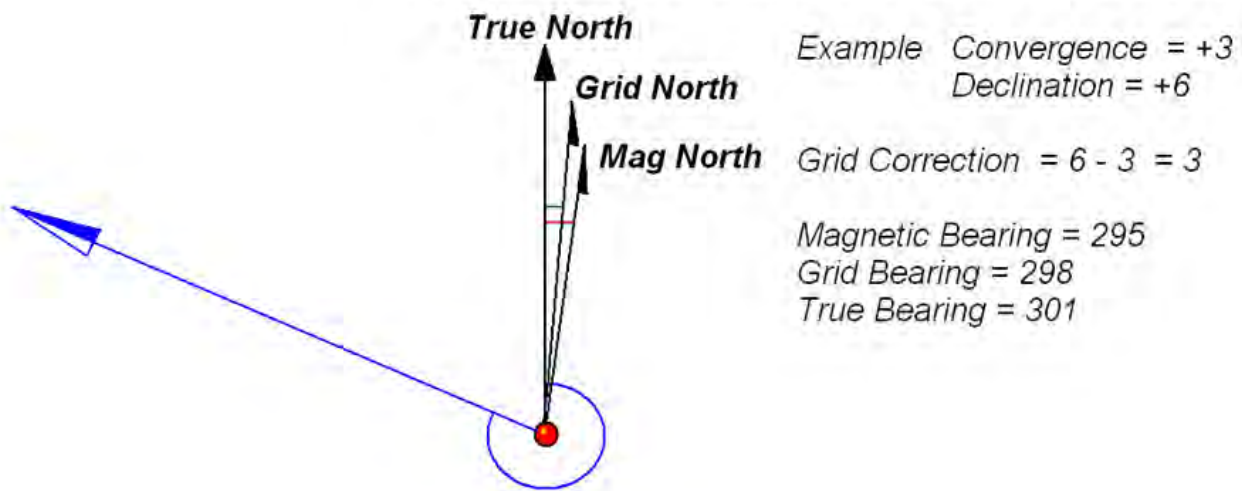
Convergence is the True Direction of Grid North (West is Negative East is Positive)  
 Declination is the True Direction of Magnetic North (West is Negative East is Positive)

$$\text{True Bearing} = \text{Magnetic Bearing} + \text{Declination}$$

$$\text{Grid Bearing} = \text{True Bearing} - \text{Convergence}$$

$$\text{Grid Bearing} = \text{Magnetic Bearing} + (\text{Declination} - \text{Convergence})$$

(Declination - Convergence) is known as the Grid Correction



## Extended example 2

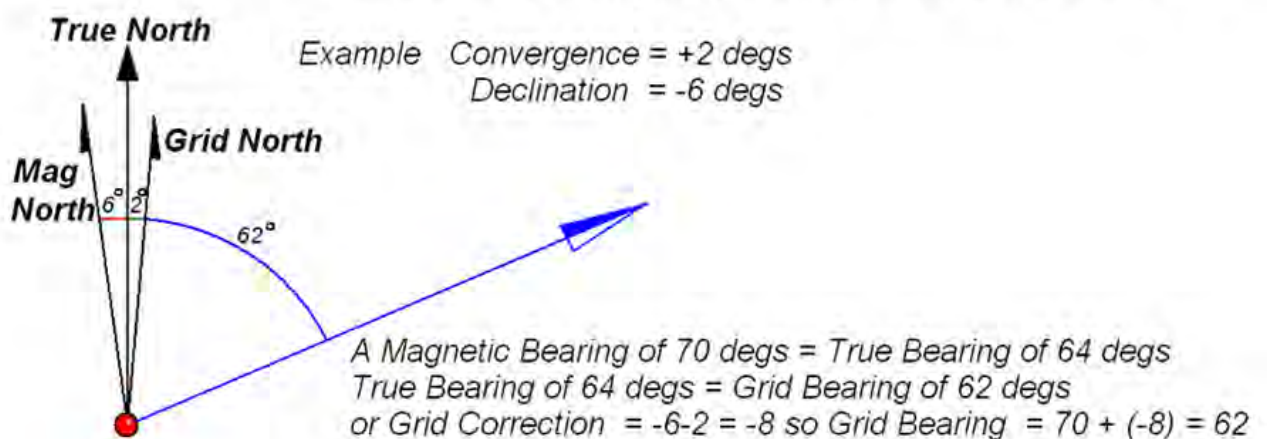
Convergence is the True Direction of Grid North (West is Negative East is Positive)  
 Declination is the True Direction of Magnetic North (West is Negative East is Positive)

$$\text{True Bearing} = \text{Magnetic Bearing} + \text{Declination}$$

$$\text{Grid Bearing} = \text{True Bearing} - \text{Convergence}$$

$$\text{Grid Bearing} = \text{Magnetic Bearing} + (\text{Declination} - \text{Convergence})$$

(Declination - Convergence) is known as the Grid Correction



## 4 The Earth's Magnetic Field

### 4.1 Basic Outline

At the heart of the planet is an enormous magnetic core that gives the Earth's navigators a useful reference. The lines of magnetic force run from south to north and these provide a reference for our compasses.

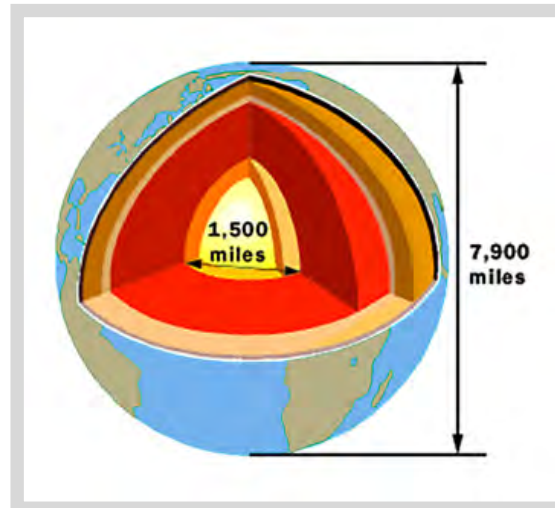


Figure 28: Basic Earth internal layers

To fully define the Earth's Magnetic Field at any location, we need three components of a vector. The Field Strength, usually measured in nano Teslas or micro Teslas, the Declination Angle defined as the True Direction of Magnetic North and the Dip Angle defined as the vertical dip of the Earth vector below horizontal. For computing reasons, this vector is often defined as three orthogonal magnetic field components pointing towards True North, East, and vertical referred to as  $B_n$ ,  $B_e$  and  $B_v$ . A fundamental law of physics relating magnetic field strength to electric current is known as the Biot-Savart Law and this is our best explanation for why  $B$  is used to denote magnetic field strength. If you know better, please contact the author - details at the front of this publication.

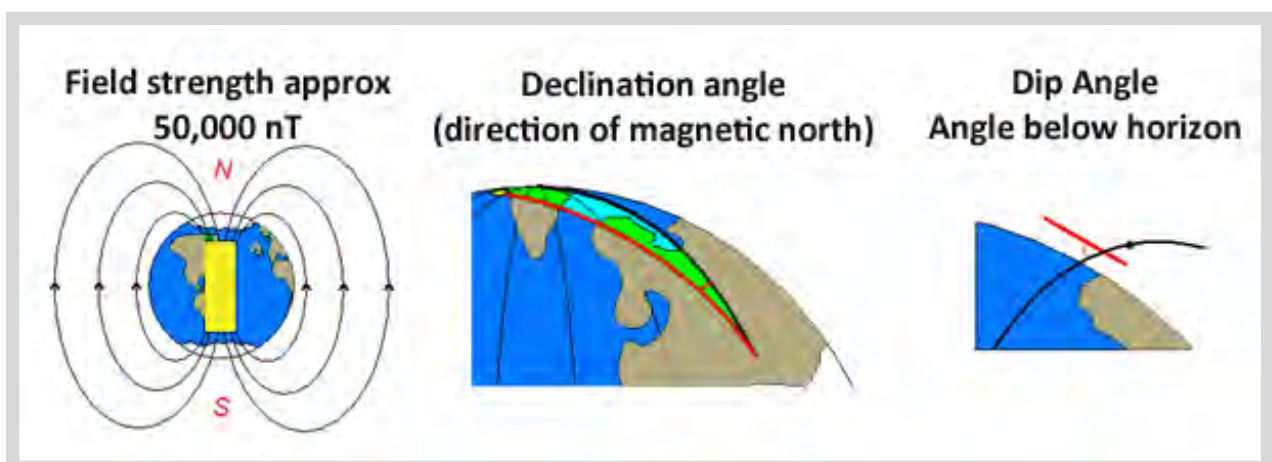


Figure 29: Elements of the magnetic field vector

## 4.2 Variations in the Earth's Magnetic Field

One problem with the Earth's Magnetic Field is that it will not stand still. Over the course of history, the magnetic core of the Earth has been turbulent with the result that the magnetic vector is constantly changing. In geological time scales this change is very rapid. It is referred to as the 'Secular' variation.

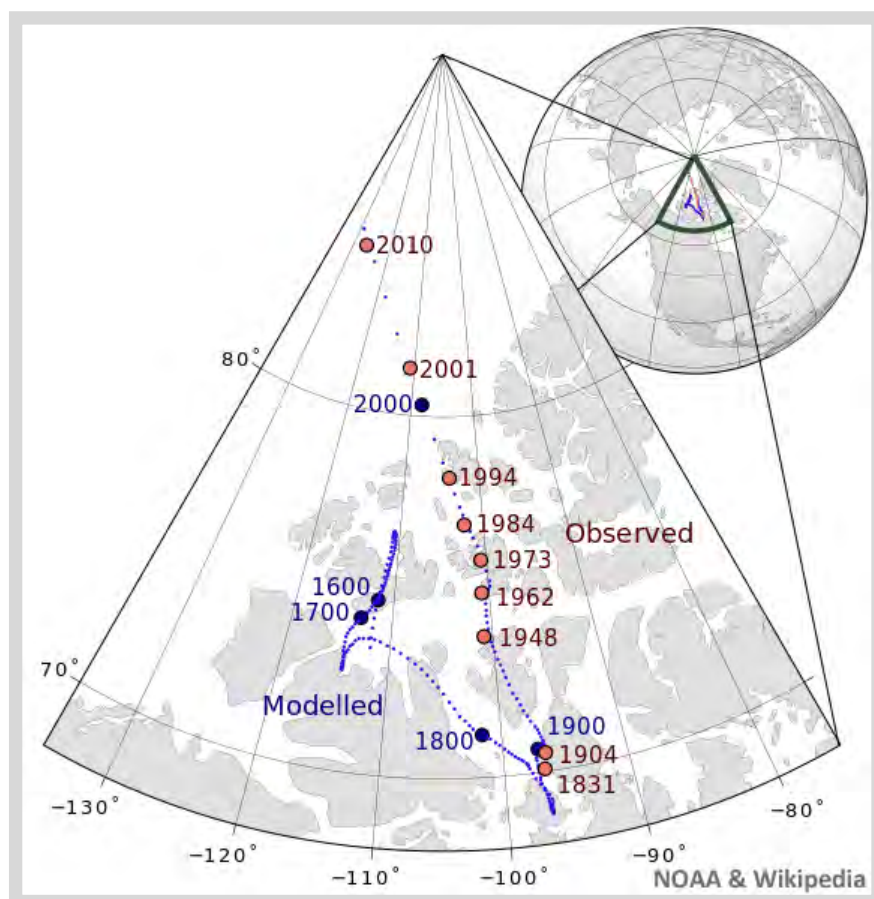


Figure 30: Tracking the magnetic North Pole

In order to keep track of this movement, several global magnetic models are maintained to provide prediction models. For example, an international organization called INTERMAGNET collates data from observatories scattered throughout the world to model the intensity and attitude of the Earth's magnetic field. Every year, the data is sent to the British Geological Survey in Edinburgh where it is distilled to a computer model called the British Global Geomagnetic Model (BGGM). Historically this has been the most commonly used model for magnetic field prediction for the drilling industry but there are others. The United States National Oceanic and Atmospheric Administration (NOAA) also produce a model known as the High Definition Geomagnetic Model from their National Geophysical Data Centre in Boulder Colorado. This takes account of more localized crustal effects by using a higher order function to model the observed variations in the Earth field. In practice, when higher accuracy MWD is required, it is increasingly popular to measure the local field using IFR (see chapter 6) and to map the local anomalies as corrections to one of the global models. In this way, the global model takes care of the secular variation over time and the local effects are not dependent on a mathematical best fit over long wavelengths.

LINKS [BGGM](#) [NOAA](#)



The model in figure 32 below is a combined effort between NOAA and the BGS called the World Magnetic Model which is updated every 5 years. This is a lower order model, as is the International Geomagnetic Reference Field produced by IAGA but these are freely accessible over the internet whereas the higher order models require an annual license.



Figure 31: Magnetic observatories

The higher order world models (BGGM and HDGM) are considered to be better than 1 degree (99% confidence) at most latitudes. This may be less true at higher latitudes above  $60^{\circ}$  but at these latitudes, IFR techniques are frequently used.

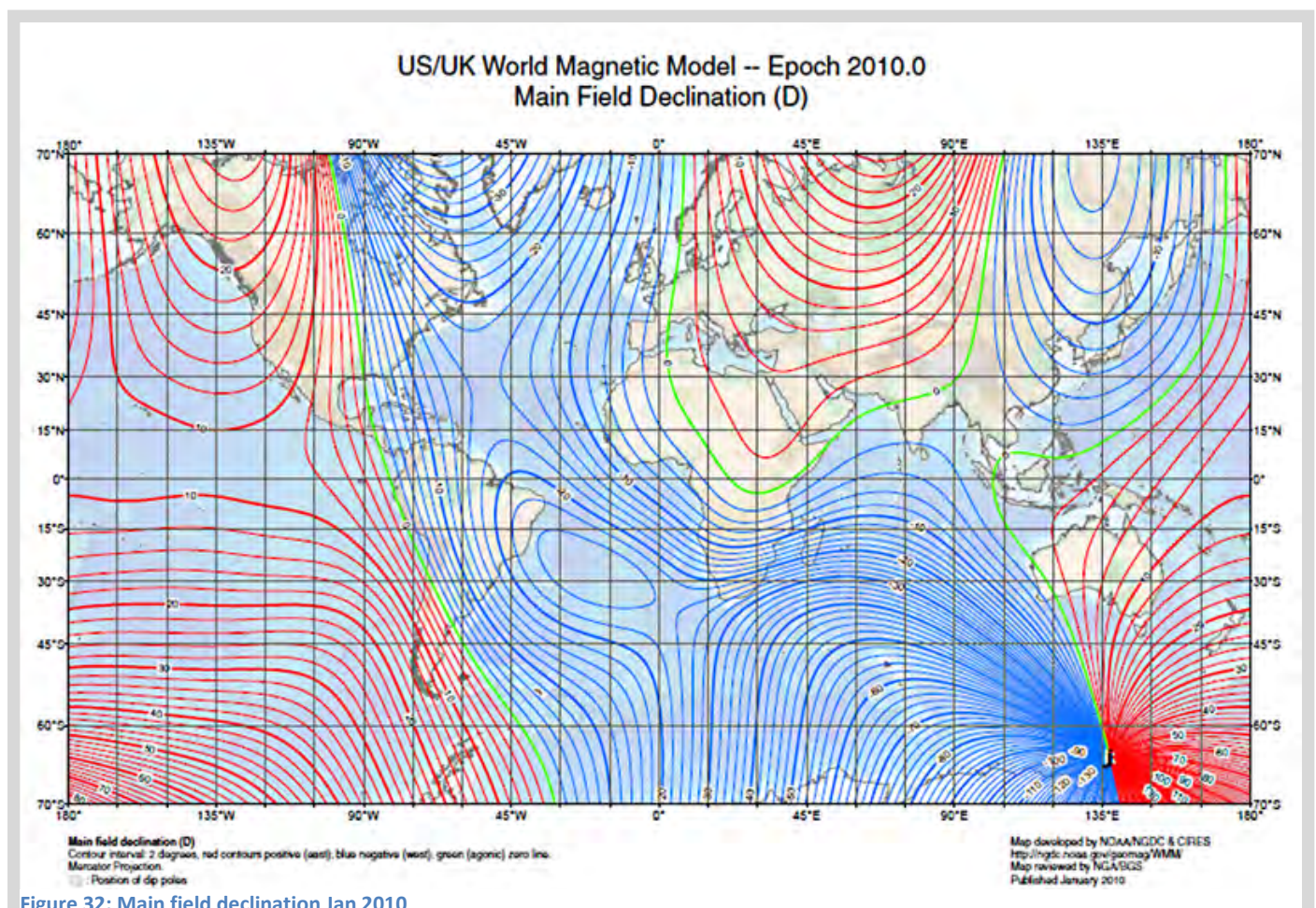


Figure 32: Main field declination Jan 2010

### 4.3 Magnetic Observatory Distribution

It should be noted that the global models such as BGGM and even HDGM, can only measure longer wave length effects of the Earth's magnetic field distribution and cannot be expected to take account of very localised crustal effects caused by magnetic minerals, typically found in deep basement formations in the vicinity of drilling. See chapter 6 for a discussion of In Field Referencing (IFR), a technique for measuring the local field to a higher

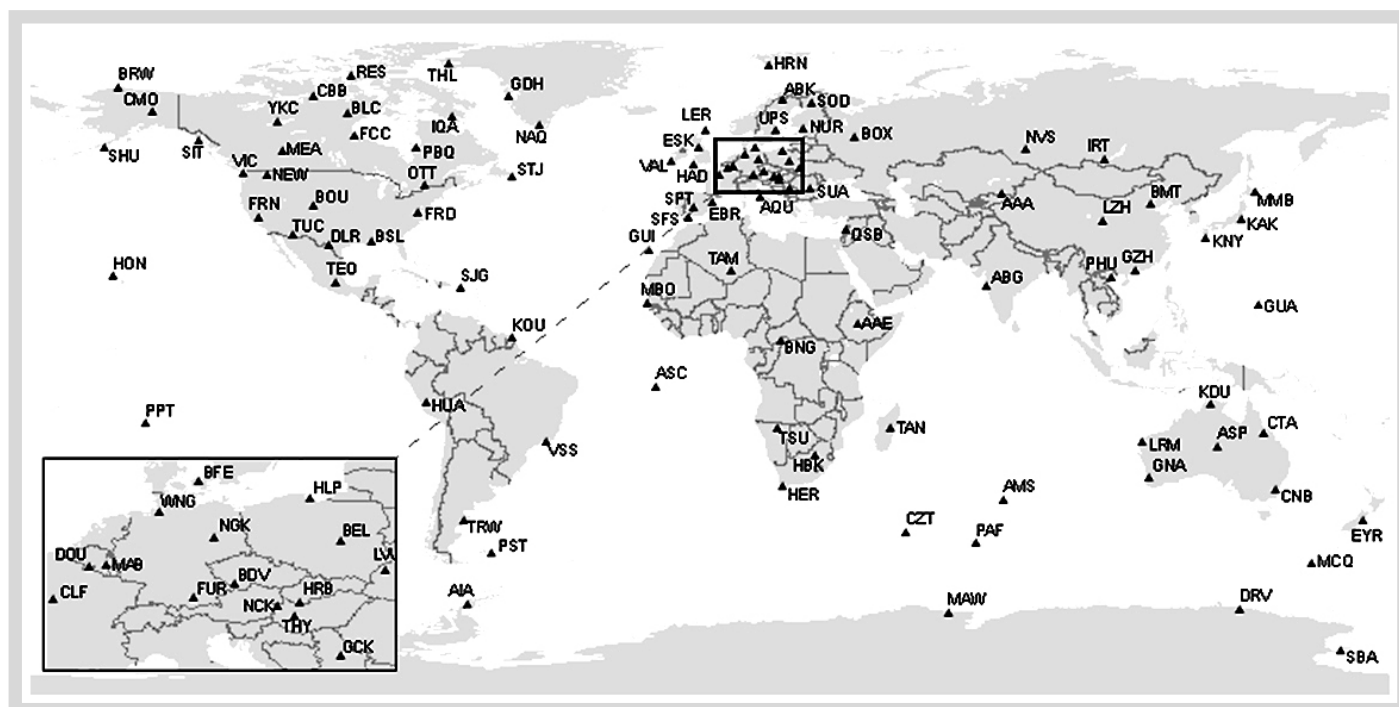


Figure 33: Magnetic Observatory locations

accuracy.

### 4.4 Diurnal Variation

The term Diurnal simply means 'daily' and for many centuries it has been noticed that the magnetic field seems to follow a rough sine wave during the course of the day. Here is a graph of field strength observations taken in Colorado over a 2-day period.

It can be seen that the field strength is following a 24-hour period sine wave. See chapter 7 for a discussion of 'Interpolated In Field Referencing', a method of correcting for diurnal variation in the field.

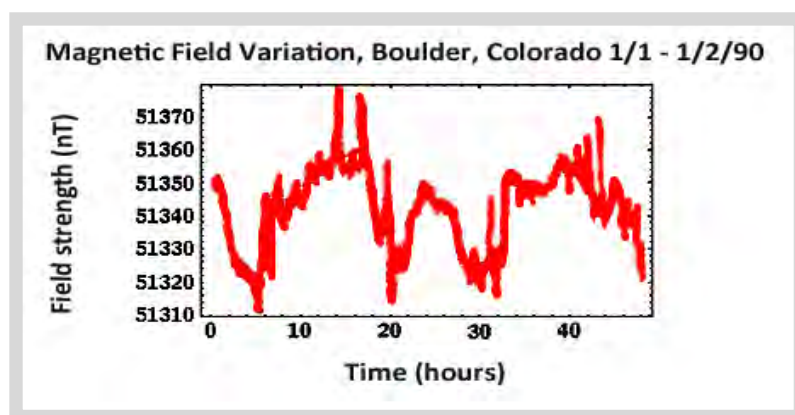


Figure 34: Diurnal field variation

These variations may be small but for high accuracy MWD work especially at high latitudes, they may need to be corrected for. We now know that this effect is due to the rotation of the Earth and a varying exposure to the solar wind. The sun is constantly emitting ionized plasma in huge quantities across the solar system. These winds intensify during magnetic storms and the material can be seen on a clear night at high or low latitudes, being concentrated at the magnetic poles and forming the 'Aurora Borealis' and the 'Aurora Australis'.

**During such storms the measurements taken from magnetometers and compasses are unlikely to be reliable but even in quiet times, the diurnal variation is always present.**



*CONTENTS*



## 5. Principles of MWD and Magnetic Spacing

### 5.1 Measurement While Drilling (MWD)

MWD usually consists of a non-magnetic drill collar as in figure 35, containing a survey instrument in which are mounted 3 accelerometers, 3 magnetometers and some method of sending the data from these to surface.

Accelerometers measure the strength of the Earth's gravity field component along their axis. Magnetometers measure the strength of the Earth's magnetic field along their axis. With three accels mounted orthogonally, it is always possible to work out which way is 'down' and with three magnetometers it is always possible to work out which way is North (Magnetic). The following equations can be used to convert from three orthogonal accelerations,  $G_x$ ,  $G_y$  and  $G_z$  (sometimes called  $A_x$ ,  $A_y$  and  $A_z$ ) and three orthogonal magnetic field measurements,  $B_x$ ,  $B_y$  and  $B_z$  (sometimes called  $H_x$ ,  $H_y$  and  $H_z$ ), to the inclination and direction (Magnetic).



Figure 35: A non-magnetic drill collar

$$I = \cos^{-1} \left( \frac{G_z}{\sqrt{G_x^2 + G_y^2 + G_z^2}} \right)$$

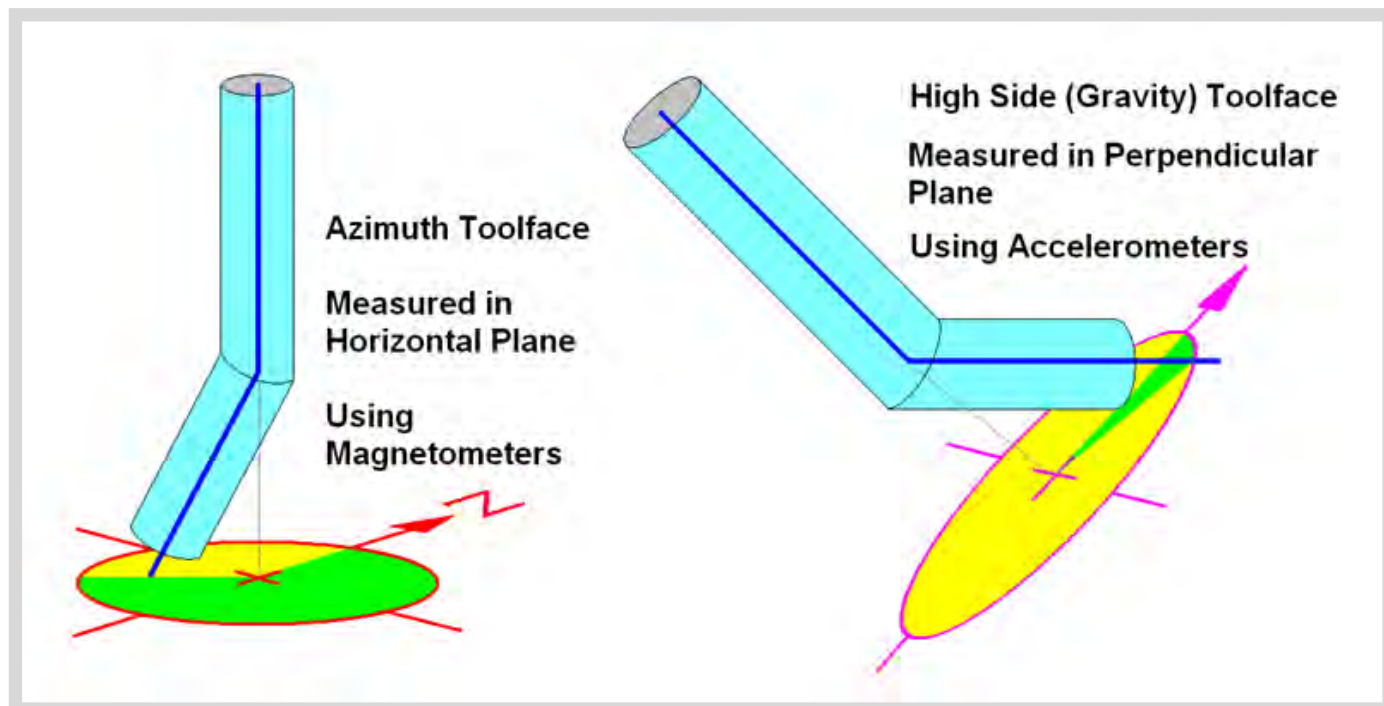
$$A = \tan^{-1} \left( \frac{(G_x B_y - G_y B_x) \sqrt{G_x^2 + G_y^2 + G_z^2}}{B_z(G_x^2 + G_y^2) - G_z(G_x B_x + G_y B_y)} \right)$$

In these equations the z axis is considered to point down hole and x and y are the cross axial axes. Some tools are arranged with the x axis downhole and y and z form the cross axial components so care should be taken when reading raw data files and identifying the axes. Similarly, there is no consistency in units in that some systems output accelerations in gs, others in mg and some in analogue counts. Similarly, the magnetometer outputs can be in counts, nano Teslas or micro Teslas.

The magnetometers are of various types but usually consist either of a coil with alternating current used to fully magnetise a core alternating with or against the Earth field component, or a small electro magnet used to cancel the Earth's magnetic field component.

The accelerometers are simply tiny weighing machines, measuring the weight of a small proof weight suspended between two electromagnets. Held vertically they will measure the local gravity field and held horizontally they will measure zero. In theory we could measure inclination with only one accelerometer but a z axis accelerometer is very insensitive to near vertical movement due to the cosine of small angles being so close to unity. Besides we also require the instrument to tell us the toolface (rotation angle in the hole).

If we want the toolface as an angle from magnetic north corrected to our chosen reference (grid or true) we use the x and y magnetometers and resolve  $\tan^{-1}(B_x/B_y)$  and if we want the angle from the high side of the hole we resolve  $\tan^{-1}(G_x/G_y)$ . For practical reasons, most MWD systems switch from a magnetic toolface to a high side toolface once the inclination exceeds a preset threshold typically set between 3 and 8 degrees.



## 5.1 Data Recovery

Most commonly, the technique used currently is to encode the data as a series of pressure pulses in the drilling fluid using poppet valves that will restrict the fluid flow to represent a one and release to represent a zero. This is known as positive mud pulse telemetry.

There are other systems which will open a small hole to the annulus to allow the pressure to drop for a 1 and recover for a zero. This is known as negative mud pulse telemetry. A third method is to generate a sinusoidal continuous pressure cycle onto which a phase modulation can be superimposed to create a decipherable message signal. This is known as continuous wave telemetry.



Figure 37: Examples of pulsar equipment

Figure 36: Graphical representation of two types of toolface

The data is interpreted at surface and displayed in a surface display unit. Direction is measured from Magnetic North initially but usually corrected to either grid or true. Inclination is measured up from vertical and toolface, as mentioned, can be measured either as an Azimuth Toolface or a High Side toolface. In the picture below, the drilling tool is currently oriented on a gravity of toolface of  $136^{\circ}$  right of high side.



Figure 38: Typical toolface display

## 5.2 MWD Magnetic Spacing

Clearly, if we are to make use of magnetic sensors in an MWD tool, we need to ensure that there is sufficient magnetic isolation to avoid significant magnetic influences from the other drilling equipment.

The following explanation is included courtesy of Dr Steve Grindrod of Copsegrove Developments Ltd.

### **NON-MAGNETIC DRILL COLLAR LENGTH REQUIREMENTS**

This section describes the theoretical background to drillstring magnetic interference, explains the origin of NMDC charts and makes recommendations on NMDC usage and inspection. This is based on [Reference CUR 252] (SPE 11382 by S.J. Grindrod and C.J.M. Wolff on Calculating NMDC length).

### 5.2.1 Drill String Magnetic Interference

The drillstring is a long slender metallic body, which can locally disturb the Earth's magnetic field. Rotation of the string and its shape causes the magnetisation to be aligned along the drillstring axis.

The magnetised drillstring locally corrupts the horizontal component of the Earth's magnetic field and hence accurate measurement of magnetic azimuth is difficult. For sensible magnetic azimuth measurement, the magnetic effect of the drillstring has to be reduced and this is done by the insertion of non-magnetic drill collars (NMDC) into the drillstring.

Non-magnetic drill collars only reduce the effect of magnetic interference from the drillstring – they do not remove it completely. An acceptable azimuth error of  $0.25^\circ$  was chosen based on Wolff and de Wardt (References CUR 443 and CUR 86) as this was the limit for 'Good Magnetic' surveys in their systematic error model. It should be noted that more recent work has suggested that magnetic interference azimuth error is likely to be of the order of  $0.25 + 0.6 \times \sin(\text{Inc}) \times \sin(\text{azimuth})$  so these values can be exaggerated at high angle heading east west.

By making assumptions about the magnetic poles in the steel above and below the NMDC, the expected optimum compass spacing to minimise azimuth error and the magnitude of the expected azimuth error can be calculated.

### 5.2.2 Pole Strength Values

Field measurements by Shell (Reference CUR 252) have been made of pole strengths for typical Bottom Hole Assemblies. These values are for North Sea area in Northern Hemisphere; these should be reversed for Southern Hemisphere. However, it should be noted that the polarity and intensity of magnetic interference is not easily predictable. In many cases the interference is mainly caused by the use of magnetic NDT techniques which of course have nothing to do with geographic location. The numbers suggested here are merely a guide and certainly not an upper limit.

#### *Upper Pole*

Drill collars up to + 900  $\mu\text{Wb}$ .

#### *Lower Pole*

Stabilisers and bit up to -90  $\mu\text{Wb}$ .

10m drill collar below NMDC up to -300  $\mu\text{Wb}$

Turbines up to -1000,  $\mu\text{Wb}$

### 5.2.3 Azimuth Error

Drillstring magnetisation affects the observed horizontal component of the local magnetic field. A magnetic compass detects the horizontal component of the Earth's magnetic field. The drillstring induced error,  $\Delta B_z$  acts along the drillstring axis and this affects the east/west component of the observed field in proportion to (Sine Inclination x Sine Azimuth). This means that the compass error increases with inclination and with increased easterly or westerly azimuth of the wellbore.

### 5.2.4 NMDC Length Selection Charts

Using the formulae from SPE 11382 by S.J. Grindrod and C.J.M. Wolff, NMDC charts can be constructed for various well inclinations and azimuths and for a maximum acceptable azimuth error. The latter is taken as 0.25 degrees as the limit for good magnetic surveying practice. By varying the DIP and B for local conditions, charts can be prepared for various areas of the world.

An example chart for a bit and stabiliser BHA is given in figure 39:

The charts can be used in two ways.

1. To estimate the recommended length of NMDC for a particular situation.
2. If a different length was used, an estimate of the possible azimuth error can be obtained.

To find the recommended length of NMDC for a particular BHA, the azimuth from North or South and the inclination are used to arrive at a point on the selection chart. For example, a section of a well being drilled at 60° inclination and 35° azimuth requires 24 m of NMDC.

This is demonstrated on the example chart above, with the 24 m overall length being found by visually interpolating between the 20 m and 30 m length lines.

Where inadequate lengths of NMDC are used, (or when reviewing past surveys where insufficient NMDC was used) it is possible to estimate the resulting compass error: -

Area:	North Sea
BHA:	Bit and Stabiliser

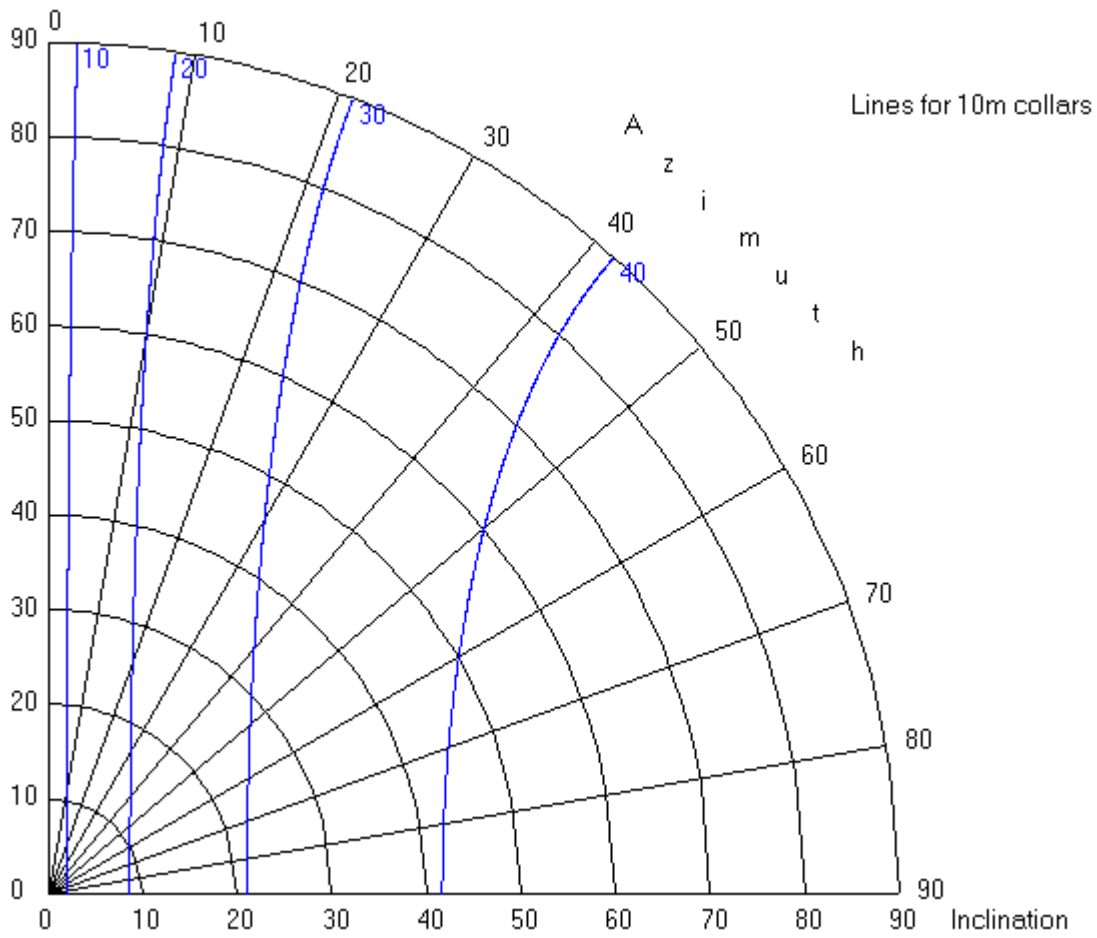


Figure 39: Example NMDC length selection chart



Upper Pole Strength:	900 uWb
Lower Pole Strength:	90 uWb
Length Steel Below NMDC:	2.00 m
Total Magnetic Field:	50,000 nT
Magnetic Dip Angle:	72.00 deg
Acceptable Azimuth Error:	0.25 deg
Optimum Compass Spacing:	30 % from bottom of NMDC

Produced by Copsegrove Developments Ltd

Possible Azimuth Error for length of NMDC used = Acceptable Azimuth Error x (Length required)<sup>2</sup> / (Length used)<sup>2</sup>

**Example:**

If only 2 NMDC's with a total length of 18.9 m (62 ft) were used instead of the recommended NMDC total length of 24 m (69 ft) we have: -

Estimated possible azimuth error =  $0.25 \times (24)^2 / (18.9)^2 = 0.4 \text{ deg}$

Note that it is not valid to deliberately cut back on NMDC usage and plan to theoretically correct a survey by the above formulae. This is because the formula assumes pole strengths for the BHA components and actual pole strengths are not generally measured in the field.



**CONTENTS**

## 6. In-Field Referencing

### 6.1 Measuring Crustal Anomalies Using In-field Referencing

The biggest source of error in MWD is usually the crustal variation. The global models such as the BGM and HDGM can only take into account the longer wave length variations in the Earth Field and cannot be expected to allow for the localised effects of magnetic rock in the basement formations. In order to correct for these effects, the magnetic field has to be measured on site. From these local measurements, a series of corrections from a global model can be mapped out for the field so that in future years, the more permanent effect of local geology can be added to the secular effects for an up to date local field model.

IFR is a technique that measures the strength (Field Strength), direction (Declination) and vertical angle (Dip Angle) in the vicinity of the drilling activity to give the MWD contractor a more accurate reference to work to.

To accurately measure the magnetic field locally we can take direct measurements from the land, the sea or the air. On land, a non-magnetic theodolite with a fluxgate magnetometer aligned on its viewing axis, is used to measure the orientation of the magnetic field against a true north, horizontal reference from which accurate maps can be made. A proton or Caesium magnetometer is used to accurately the local field strength. In the air, only the field strength variations can be measured but if a wide enough area is measured at high resolution, the field strength data can be used to derive the effects on the compass and good estimates of the declination and dip angle can then be mapped. At sea, specialist non-magnetic equipment can be towed behind a vessel or carried on board a non-magnetic survey vessel with very accurate attitude sensors and magnetometers that output their data at high frequency and the motion effects are taken out in the processing.



### 6.1.1 IFR Survey Maps

Once the measurements have been taken, contoured maps are produced to allow the MWD contractor to interpolate suitable magnetic field values for use on his well.

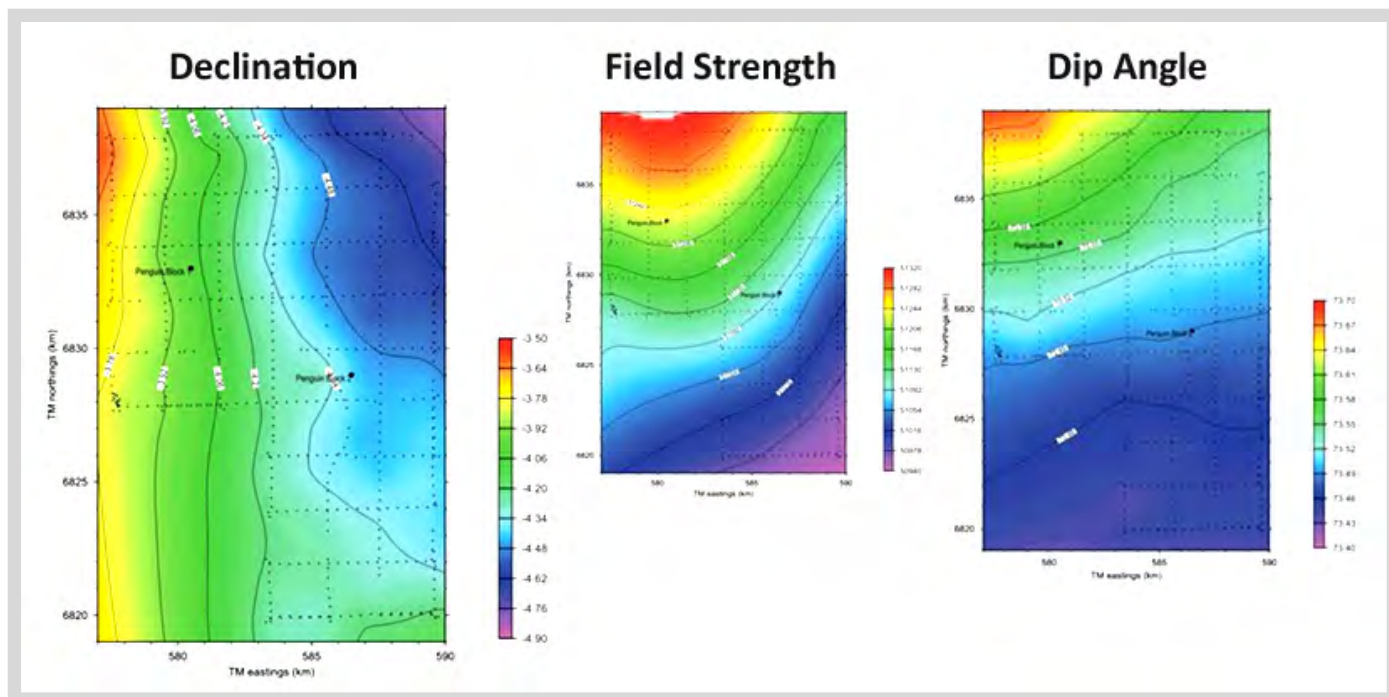


Figure 39: Examples of IFR survey results

The IFR survey results are usually provided as digital data files which can be viewed with the supplied computer program. This allows the contractor to view the data and determine magnetic field values at any point within the oilfield.

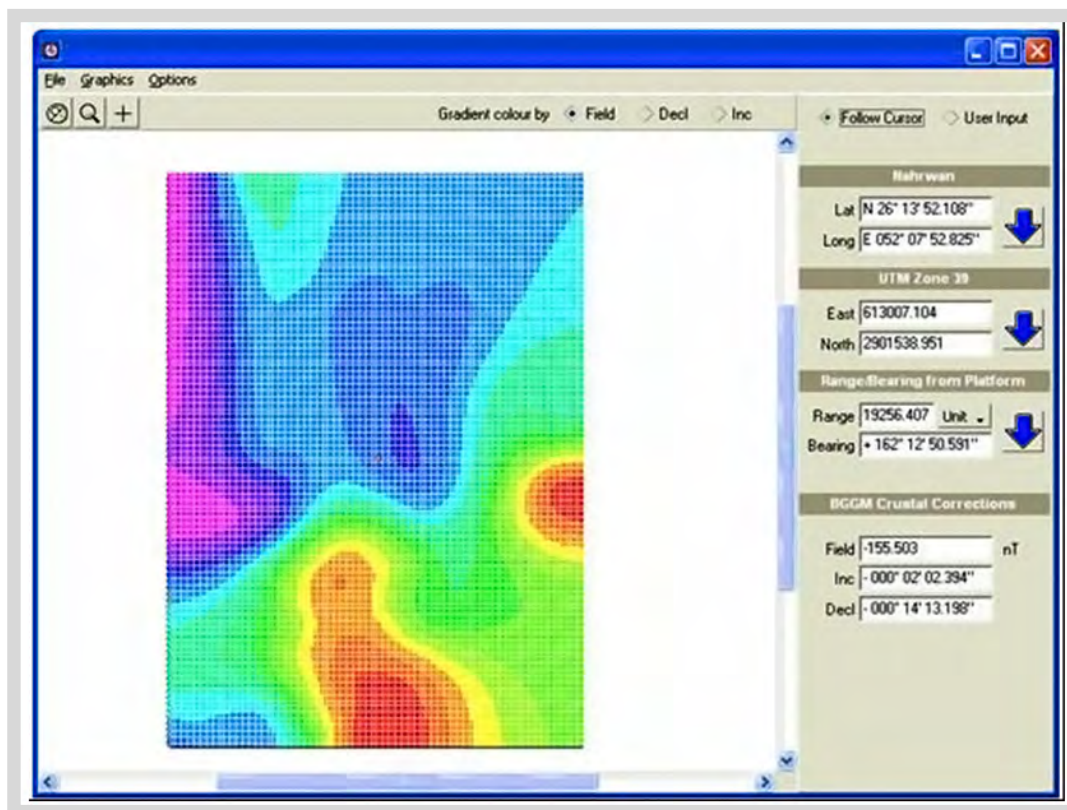


Figure 40: Typical software display of an IFR survey

Two versions of the field maps are supplied. The first shows the absolute values of the total field, declination and dip angles, observed at the time of the IFR survey. The second set of maps shows how these values differed from the predictions of the BGGM model, due to the magnetic effects of Earth's crust in the oilfield. It is these crustal corrections which are used by MWD contractors.

The crustal corrections vary only on geological timescales and therefore can be considered to be fixed over the lifetime of the field. The BGGM model does a very good job of tracking the time variation in the overall magnetic field. By combining the BGGM model and the IFR crustal corrections, the MWD contractor obtains the best estimate of the magnetic field at the rig.

First, we use the BGGM model to get an estimate of the total field, dip and declination. Then the IFR correction values for the background magnetic field are applied by adding the BGGM values and the corrections. i.e.

<b>Total Field</b>	<b><math>T_f = T_f\text{BGGM} + T_f\text{Crustal Correction}</math></b>
<b>Declination</b>	<b><math>\text{Dec} = \text{DecBGGM} + \text{DecCrustal Correction}</math></b>
<b>Dip Angle</b>	<b><math>\text{Dip} = \text{DipBGGM} + \text{DipCrustal Correction}</math></b>

In most cases, this just involves selecting the location of the rig and choosing a single set of crustal corrections. In some cases, when the magnetic gradients are strong, the MWD contractor may choose a different declination for each hole section along the wellbore. If the declination or dip value varied by more than 0.1 degrees, or the field strength varied by more than 50nT along the wellbore, it would be recommended to derive values for each hole section.

**Note on Use of Error Models** – see from chapter 17

Once IFR has been applied to an MWD survey, the contractor can change the error model applied to the survey to determine the uncertainty on its position. The Industry Steering Committee for Wellbore Survey Accuracy (ISCWSA) maintain industry standard error models for MWD that allow software to determine the positional uncertainty of the wellpath.

Normal MWD for example would have a declination error component of 0.36 degrees at 1 standard deviation but with IFR this is reduced to 0.15 degrees.

The effect of all this is to significantly reduce the uncertainty of the well position with all the benefits of the improved accuracy for collision risk, target sizing, close proximity drilling, log positional accuracy, relief well planning and so on.



Figure 41: Calibrating a marine observation frame on land & using a non-magnetic vessel for marine surveying

## 6.2 Interpolated In-field Referencing

One solution to diurnal variations is to use a reference station on surface. In this way, the observed variations observed at surface can be applied to the Downhole Data which will experience similar variation. This is not always practical and requires a magnetically clean site with power supply nearby and some method of transmitting the data in real time from the temporary observatory. The other issue is establishing the baseline from which these variations are occurring in order to correct to the right background field values.

In a combined research project between Sperry Sun and the British Geological Survey, it was discovered that the diurnal and other time variant disturbances experienced by observatories, even a long way apart follow similar trends. The researchers compared observations made at a fixed observatory with derived observations interpolated from those taken at other observatories some distance away. The match was very encouraging and a new technique for diurnal correction was established called Interpolated In-Field Referencing or IIFR (not be confused with IFR discussed below). This technique is a patented method of correcting for time variant disturbances in the Earth's magnetic field but is widely used under licence from the inventors. The readings observed at the nearby stations are effectively weighted by the proximity to the drill site and the time stamped combined corrections applied to the Downhole observations either close to real time or retrospectively.

LINK BGS - [GeoMagnetic](#)



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## 7. Survey Calculation Methods

### 7.1 Examples of Current Methods

Over the years there have been several methods of calculating survey positions from the raw observations of measure depth, inclination and direction. At the simplest level if a straight line model is used over a length  $\delta M$  with inclination  $I$  and Azimuth  $A$ , we can derive a shift in coordinates as in figure 42.

This simple technique is often referred to as the Tangential Method and is relatively easy to hand calculate. However, the assumption that the inclination and direction remain unchanged for the interval can cause significant errors to accumulate along the wellpath.

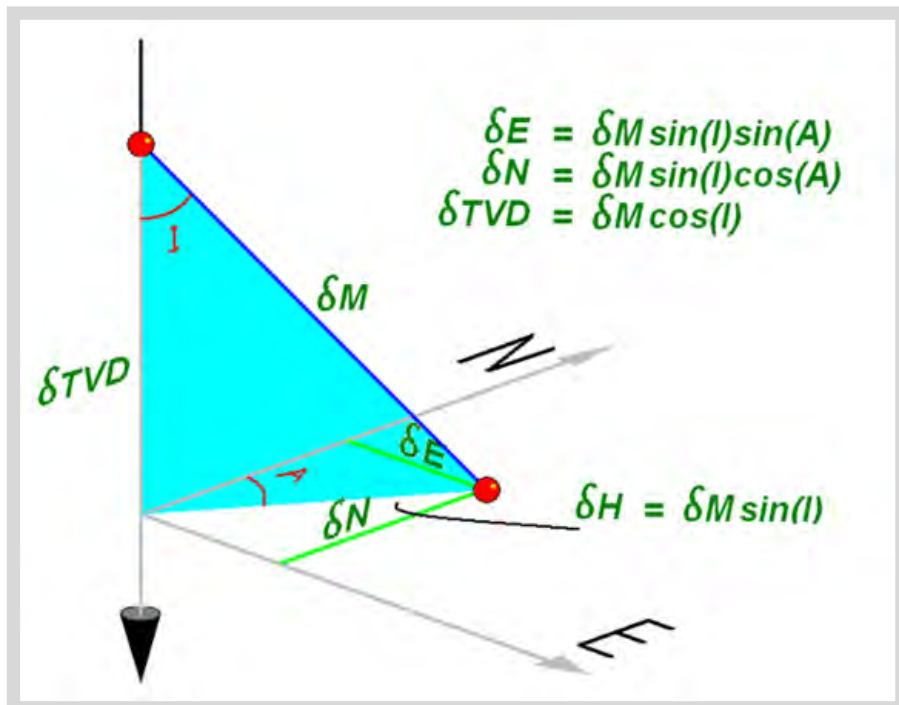


Figure 42: Tangential method to derive a shift in coordinates

An improvement to this was the 'Average Angle Method' where the azimuth and inclination used in the above formulas was simply the average of the values at the start and end of the interval.

In the days when there were no personal computers the average angle was the preferred method of calculating surveys and it produces results similar to the more recent minimum curvature method currently in use.

$$I = \frac{Inc1 + Inc2}{2} \quad A = \frac{Azi1 + Azi2}{2}$$

$$\begin{aligned} \delta E &= \delta M \sin(I) \sin(A) \\ \delta N &= \delta M \sin(I) \cos(A) \\ \delta TVD &= \delta M \cos(I) \end{aligned}$$

#### Average Angle Example

- $Md1 = 1000$   $Inc1 = 28$   $Azi1 = 54$
- $Md2 = 1100$   $Inc2 = 32$   $Azi2 = 57$
- $\Delta MD = 100$
- Average  $Inc = 30$
- Average  $Azi = 55.5$
- $\Delta East = 100 \sin(30) \sin(55.5) = 41.2$
- $\Delta North = 100 \sin(30) \cos(55.5) = 28.3$
- $\Delta TVD = 100 \cos(30) = 86.6$

A further improvement was the Balanced Tangential Method whereby the angle observed at a survey station are applied half way back into the previous interval and half way forward into the next.

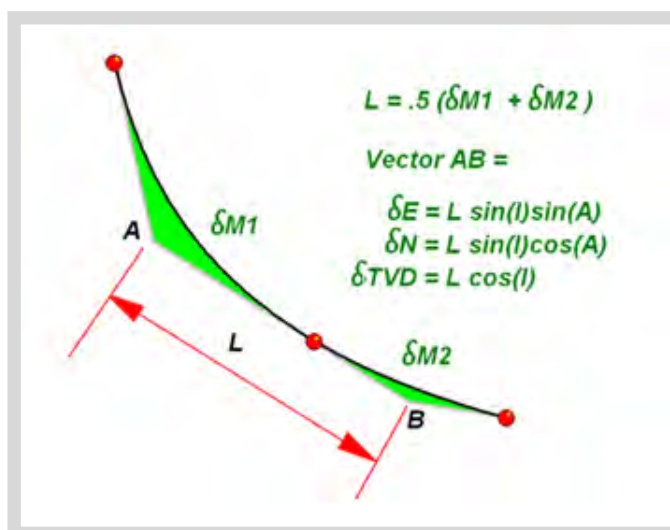


Figure 43: Balanced Tangential Method

These techniques all suffer from the weakness that the wellpath is modelled as a straight line. More recently, the computational ability of computers has allowed a more sophisticated approach. In the summary slide figure 44 we see two curved models.

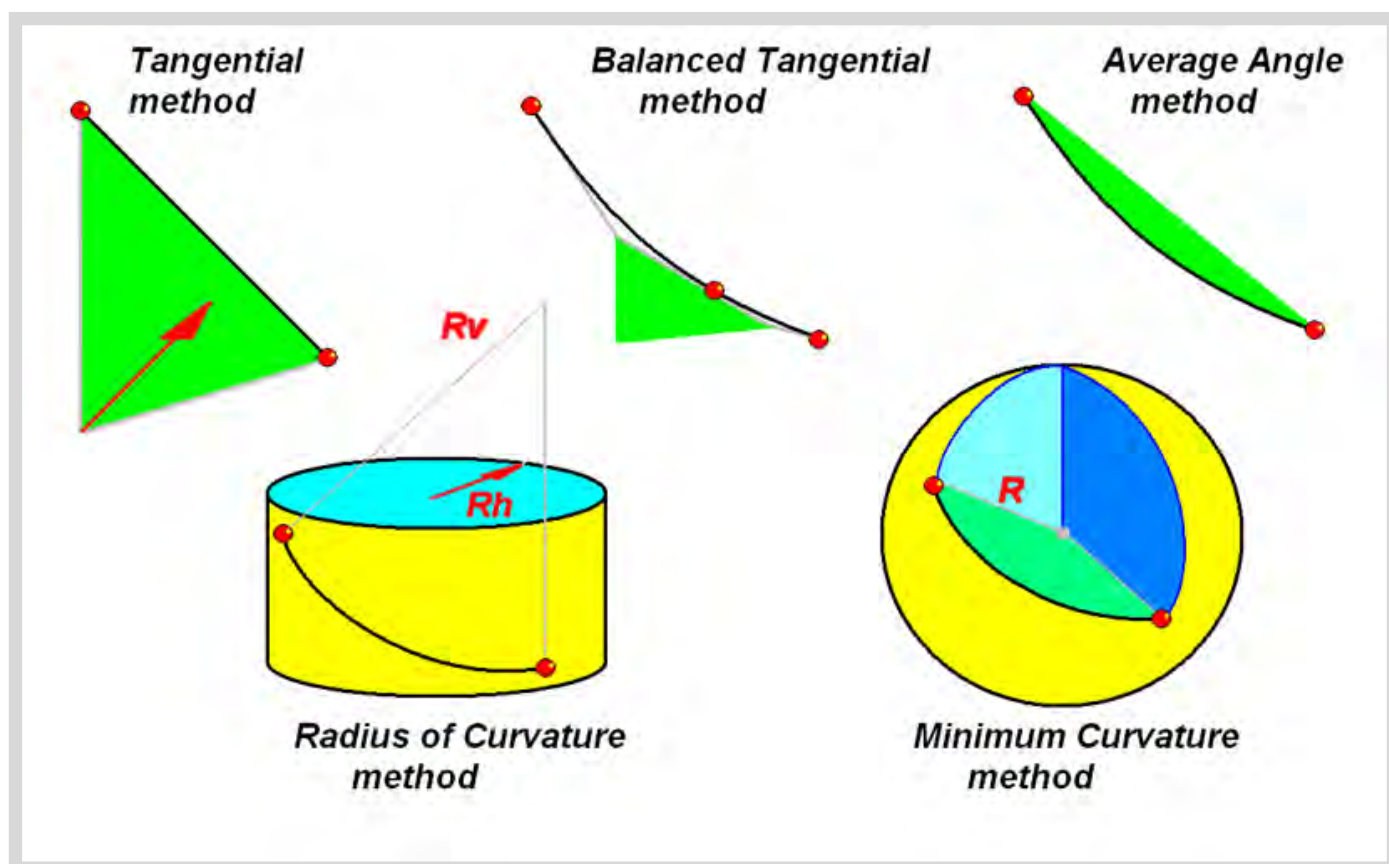
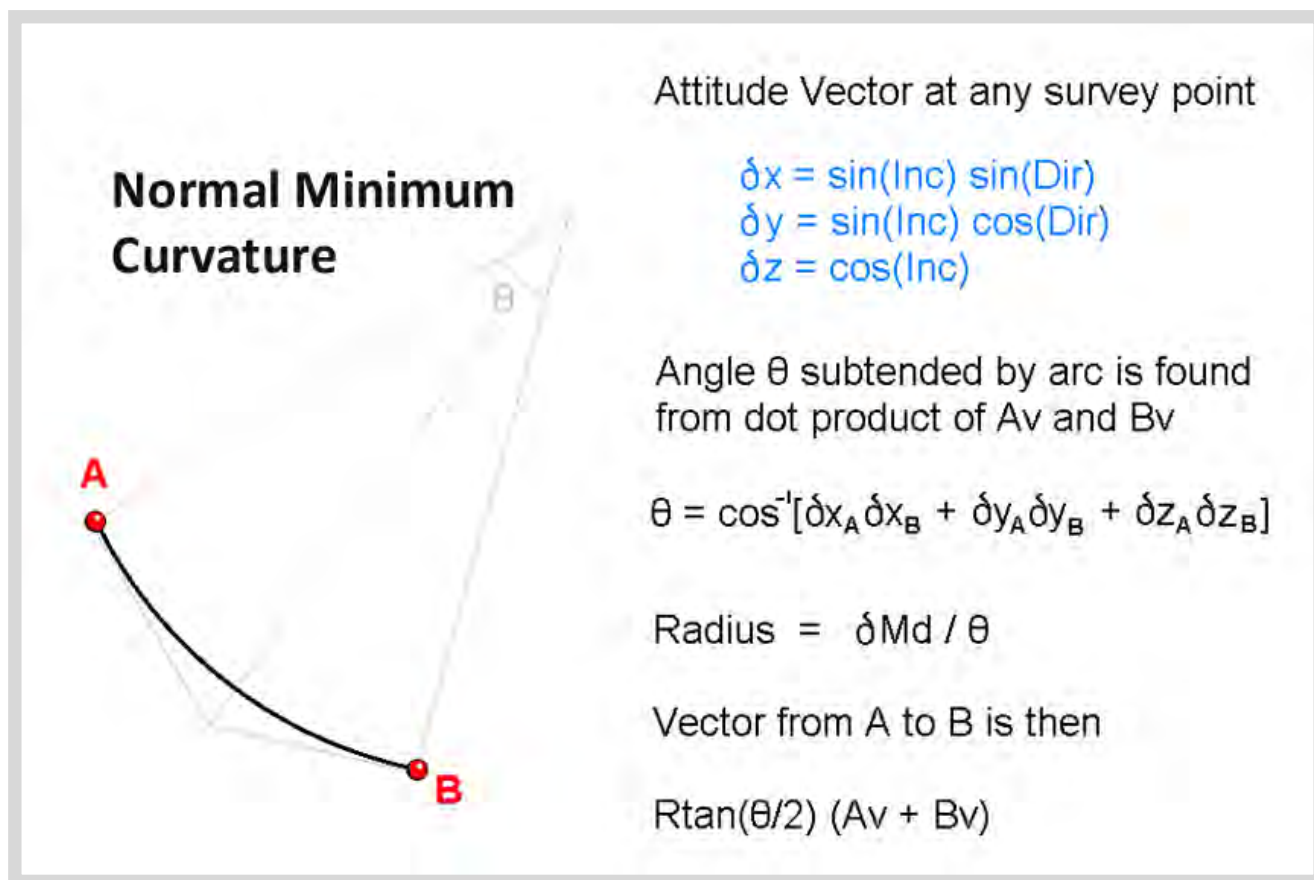


Figure 44: Methods of dealing with curvature

The one on the left assumes that the wellpath fits on the surface of a cylinder and therefore can have a horizontal and vertical radius. The one on the right assumes the wellpath fits on the surface of a sphere and simply has one

radius in a 3D plane that minimizes the curvature required to fit the angular observations. This method, known as the 'Minimum Curvature' method, is now effectively the industry standard.



Imagine a unit vector tangential to a survey point. Its shift in x, y and z would be as shown above. The angle between any two unit vectors can be derived from inverse cosine of the vector dot product of the two vectors. This angle is the angle subtended at the centre of the arc and is assumed to have occurred over the observed change in measured depth. From this the radius can be derived and a simple kite formed in 3D space whose smaller arm length follows vector A then vector B to arrive at position B.

Notice however that the method assumes a constant arc from one station to the next and particularly when using mud motors, this is unlikely to be the case.



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Figure 45: Minimum curvature method

## 8. Survey Frequency

### 8.1 Determining TVD

Consider two possible procedures for drilling from A to B - both of these trajectories start and end with the same attitude and have the same measured depth difference.

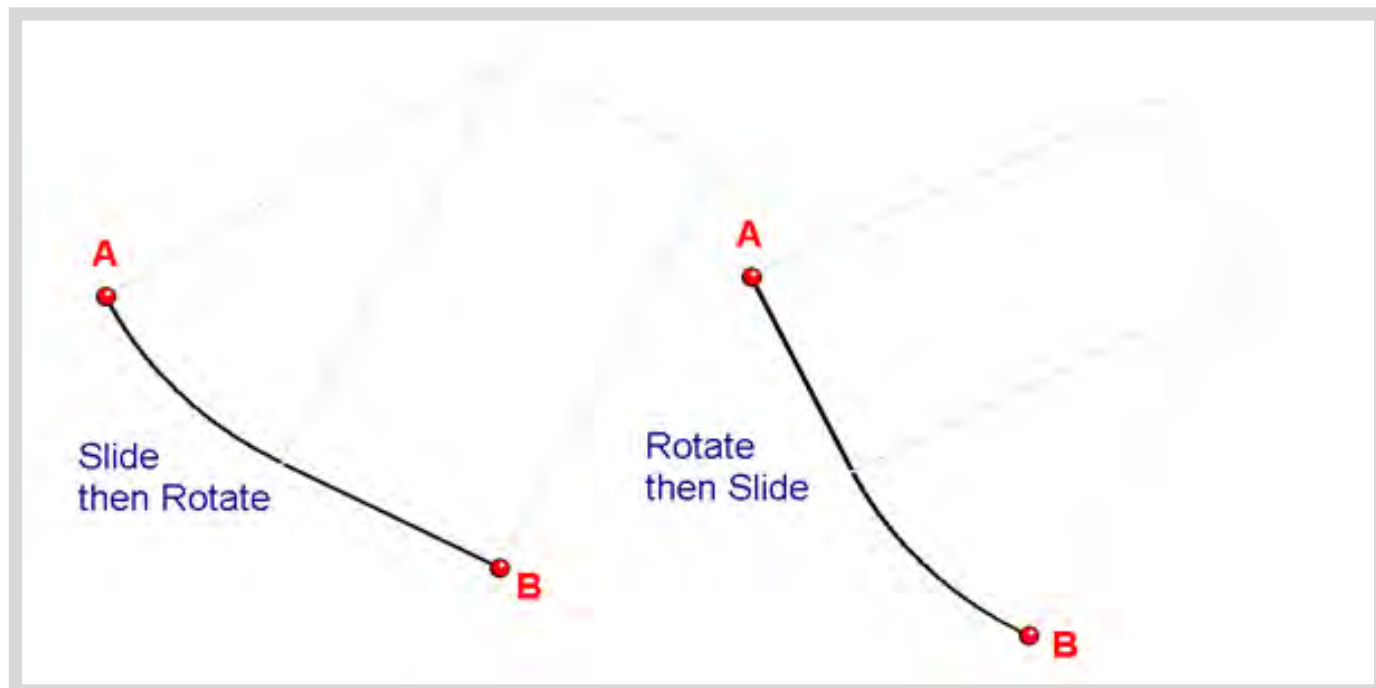


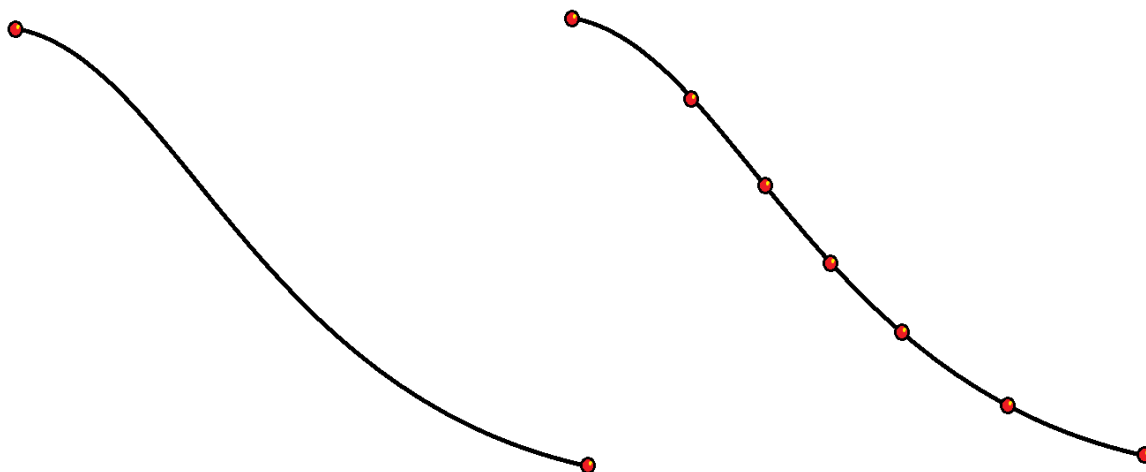
Figure 46: Example drilling trajectories

Suppose we were at 50 degrees inclination at A and built to 60 degrees inclination at B. In the case on the left the curve comes first followed by a straight and vice versa on the right. Clearly the wellpaths are different but the surveys would be identical since the measured depths are the same, the azimuth has not changed and the inclinations have risen by 10 degrees. Because a single arc is applied, there is a potential for significant TVD error to accumulate along the wellpath if the changes in geometry are not sufficiently observed.

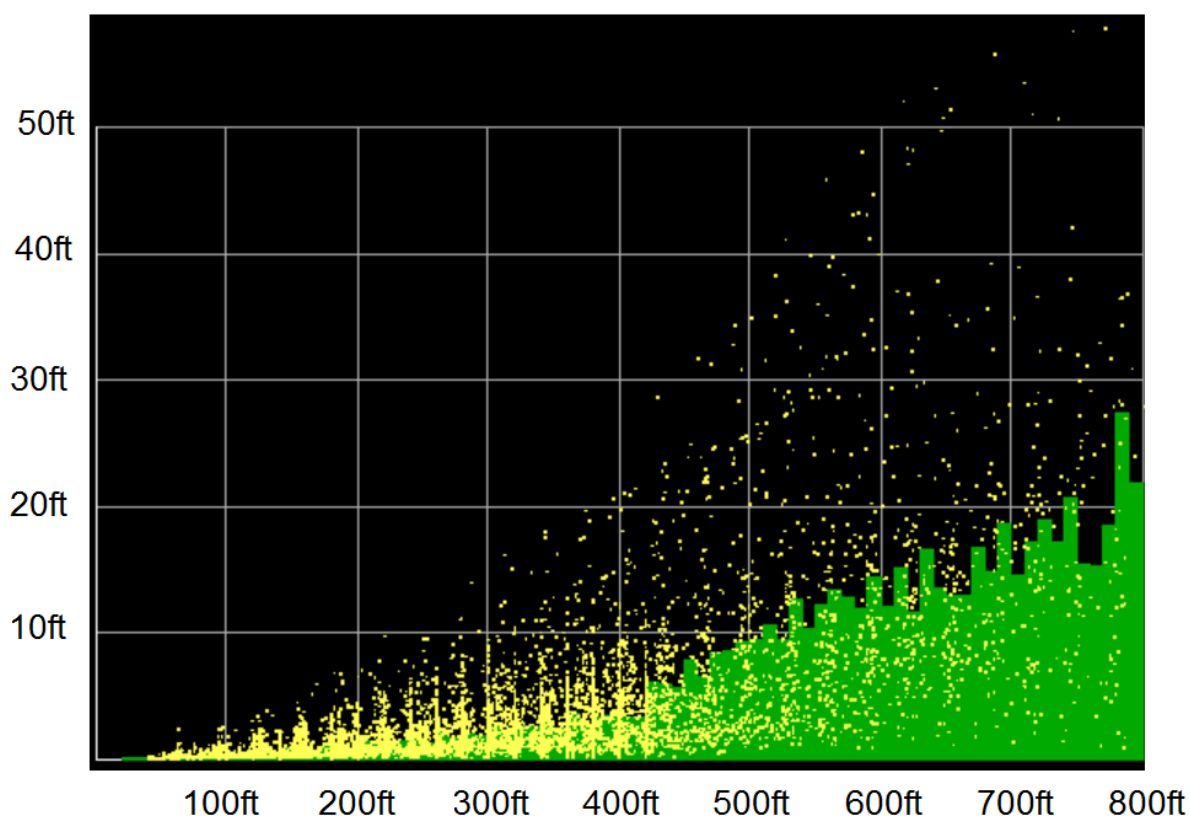
For this reason, it is often recommended that when building angle faster than 3 degrees per 100 ft (or 30 m) it is best to survey every pipe joint rather than every stand to ensure adequate observations to truly represent the well path. In the next chapter it will be seen that a rate gyro can observe at very short intervals indeed with no additional survey time and in general these are better at determining TVD than MWD. Normally however, gyro surveys are interpolated at 10 or 20 ft intervals or equivalent just for ease of handling and processing the data.

### 8.2 Effect of Survey Interval on Well Path Positional Uncertainty

It is important to note that our industry standard systematic error models have not traditionally modelled for the effect of survey interval. It is very hard to quantify what the effect of missing data might have been and so the error models have been published with the caveat that adequate surveys must be taken to accurately reflect the geometry of the wellpath.



Clearly if the minimum curvature algorithm were applied to the survey on the left where the inclination and azimuth are identical at the start and end of the curve, a simple straight line path would be assumed whereas the reality is better represented by the surveys on the right. I conducted a study using some of Shell's survey database a few years ago. I removed every second survey from some high intensity gyro surveys and recalculated. Then I removed more and plotted the errors against the survey interval. The actual positional error grew in a quadratic. Here is one example plot.



On the x axis is the survey interval and the scatter on the y axis represents positional errors from the original surveyed position. The green histogram is a set of average positional errors for each survey interval in 10ft increments.

The approximate equation relating these is of the order of  $.3 \times (\text{Interval}/100)^2$  which has an interesting effect. If this is even close to correct then reducing our survey interval from 90ft to 30ft reduces our positional error by a factor of 9 not 3. Similarly, we might expect that missing a 90ft survey will increase our positional error due to lack of surveys by a factor of 4 rather than 2.



What should we do about this? Some companies would argue that a simple additional inclination and azimuth error should be added in proportion to their respective changes from one survey to the next. For example, we might add  $.1 \times$  azimuth change as an azimuth error and perhaps  $0.1 \times$  inclination change as an inclination error. The shorter the interval, the smaller the change and therefore the smaller the error applied. Since the md difference is also proportional to the interval, this has a square term on interval just like the study shows. Others would argue that as we are trying to model missing data, we might generate misleading uncertainty models and we should cover this by best practice.

Most companies agree that when the dogleg severity exceeds 3 degs / 100ft it is good practice to survey every single rather than every stand.

However, there are some occasions where the lack of surveys has to be remedied long after the event.

Sometimes when a well is misplaced in TVD, it is necessary to re-analyse the MWD survey to obtain a better estimate of TVD. This is done by including the slide sheet information. The technique can only be used as a rough guide to the likely TVD adjustment required but has often explained poor production results or severe disagreement between gyro and MWD depths.

Using the slide sheet in figure 47 as an example:

BHA	Survey Depth	Incl. Degree	Azimuth Degree	Depth From	Depth To	Feet	Drill O/R	Tool Face / RPM	Drill Hrs.	VOB 1000#	PUSO & ROT VT	Pump SPM	Flow Rate	Pressure OFF/ON	Comments Date	Bit to Surveys
6	11519	82.8	177.3	11537	11559	22	R	50	1.25	10	165,155	94	230	3000/3120	28-Nov	40
6				11559	11573	14	o	10R	1.75	10	165,155	94	230	3000/3120	28-Nov	40
6	11551	82.2	176	11573	11591	18	r	50	1.50	10	165,155	94	230	3000/3120	28-Nov	40
6				11591	11615	24	o	15L	4.50	20	165,155	94	230	3000/3120	28-Nov	40
6	11581	83.7	175.7	11615	11621	6	r	45	0.75	5	165,155	94	230	3000/3120	28-Nov	40
6				11621	11639	18	o	hs	1.75	20	165,155	94	230	3000/3120	28-Nov	40
6				11639	11649	10	o	hs	1.25	20	165,155	94	230	3000/3120	29-Nov	40
6	11613	86.1	173.9	11649	11653	4	r	45	0.25	8	165,155	94	230	3000/3120	29-Nov	40
6				11653	11665	12	o	15R	1.25	20	165,155	94	230	3000/3120	29-Nov	40
6	11644	88.3	175.6	11665	11684	19	r	45	1.00	8	165,155	94	230	3000/3120	29-Nov	40
6				11684	11699	15	o	hs	3.25	20	165,155	94	230	3000/3120	29-Nov	40
6	11676	89.9	176.1	11699	11716	17	r	45	1.50	8	165,155	94	230	3000/3120	29-Nov	40
6	11707	90.4	176.2	11716	11747	31	r	45	3.00	8	165,155	94	230	3000/3120	29-Nov	40
6	11739	90.5	175.3	11747	11779	32	r	45	2.75	8	165,155	94	230	3000/3120	29-Nov	40
6				11779	11785	6	o	70R	1.00	8	165,155	94	230	3000/3120	29-Nov	40
6	11771	90.5	175	11785	11811	26	r	45	2.75	8	165,155	94	230	3000/3120	29-Nov	40
6				11811	11843	32	r	45	3.50	8	165,155	94	230	3000/3120	29-Nov	40
6				11843	11851	8	o	50R	2.00	8	165,155	94	230	3000/3120	30-Nov	40
6				11851	11872	21	r	45	1.75	8	165,155	94	230	3000/3120	30-Nov	40
				11872	11390	-482				8	165,155	94	230	3000/3120	30-Nov	43
8				11390	11402	12	o	65L	12.50	8	165,155	94	230	3000/3120	12-Dec	37
8				11402	11421	19	o	45L	9.00	8	165,155	94	230	3000/3120	13-Dec	37
9				11421	11426	5	o	65L	2.00	8	165,155	90	230	3000/3120	15-Dec	37

Figure 47: Typical slide sheet

Looking at the data for BHA 6, we can see a few points where surveys were taken and several changes from rotating to oriented (sliding) mode. The lengths and toolfaces are listed for each slide. Whilst these values will only be approximate it is possible to then estimate the wellbore attitude at the points where the slides began and ended.

Firstly if we take the total curvature generated over the BHA run by measuring the angle changes between surveys (see minimum curvature described above in [chapter 7](#)) we can work out the dogleg severity capability of

this assembly. If we then apply that curvature on the toolfaces quoted, it is possible to determine a fill in survey at the beginning and end of each slide by using the approximation that the inclination change will be:

***DLS x length x cos(Toolface) and the azimuth change will be the DLS x length x sin(Toolface) / sin(Inclination)***

- where DLS means dogleg severity in degrees per unit length. This allows us to complete surveys at the start and end of each slide and minimum curvature will then be more valid when joining the points.

This assumes that:

1. The DLS is unchanged during the run
2. The curvature all happens when sliding
3. The toolface was constant during the slide

These assumptions are very simplistic but the analysis will generally give a better idea of TVD than the assumption that the sparse surveys can be safely joined with 3D constant arcs.



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## 9. Gyro Surveying

### 9.1 Background and History of Gyros

#### What is a Gyro?

A Gyroscope is a device which enables us to measure or maintain an orientation in free space and rotor gyros specifically, operate on the principle of the conservation of angular momentum. The first gyros were built early in the 19th century as spinning spheres or disks (rotors), with designs incorporating one, two or three gimbals, providing the rotor spin axis with up to three degrees of freedom. These early systems were predominantly used within the academic community, to study gyroscopic effects as rotor speeds (angular momentum) could not be sustained for long periods, due to bearing friction effects. The development of the electric motor overcame this rotation decay problem and led to the first designs of prototype gyrocompasses during the 1860's.

As with most scientific and technology advances, continued development and refinement was propagated and accelerated to address military applications and by the early 1900's gyros were being used in many attitude control, orientation and navigation applications. Rotor gyros are still by far the most common system used by the oil industry.

During the second half of the 20th century several additional technologies were developed and exploited providing gyroscopic capabilities. These included:

- Vibrating Gyros
- Hemispherical Resonator Gyros
- Quartz Rate Sensors
- MHD Sensor
- Fibre Optic Gyros
- Laser Gyros
- MEMS Gyros

The systems currently considered to have the most potential for the oil industry are the Laser and MEMS systems. Indeed, *Inteq* developed and successfully marketed and operated the highly accurate RIGS (Ring-Laser Inertial Gyro Surveyor) for many years servicing the North Sea. The current performance capability of the MEMS unit is still less than desired but is regarded as having potential for the future.

## 9.2 Oilfield Applications – A Brief History

In the early years of oil well drilling the process of drilling the borehole was more of an art than a science. The general principals of geology and exploration were understood and followed but the effects of formation changes and dip on bit deflection and hence borehole trajectory were not clearly understood and largely ignored. This perpetuated state of ignorance lead to many unresolved lease disputes, where wells drilled and brought on stream, close to an adjacent lease, would often result in diminished production rates on the adjacent lease wells. However, as now, wells already in production were cased and the magnetic compass based survey instruments available, could not provide post completion trajectory data. Throughout this time, many inclination-only devices were developed, later versions of which were accurate to 1 or 2 degrees throughout their operating range.

In 1928 Alexander Anderson published a study of Borehole Survey Inclination Data obtained from a significant population of wells from various locations. Anderson had developed a Pendulum Instrument, the position of which was recorded on film as the tool was lowered in the borehole. This publication, illustrating universal and significant wellbore deviation, brought focus on the extent of the problem within the industry. As a direct result of Andersons study, J. N. Pew, then the Vice President of Sun Oil Co. instructed a team of Engineers working out of the Sun Research Laboratory in Dallas, to design and develop instruments which would provide the Inclination of the borehole and the Direction of that Inclination within casing. The 5.5" SURWEL Gyro Instrument incorporated a Gyro Compass Face superimposed over a Bubble Level Unit with the permanent record obtained with a Camera.

The Sperry Gyroscope Co. was chosen as the Gyro supplier and with each company holding a 50 per cent stake in the new company, the Sperry-Sun Well Surveying Company was formed and gyro referenced borehole surveying became a reality on 9th October 1929.

## 9.3 Chronology of Gyro Development

- 1920's: Several designs of Inclinometers and very basic Magnetic Compasses are in use. Companies of note operating Directional Survey Services are H. John Eastman, Hewitt Kuster and Alexander Anderson.
- 1929: First Gyro Survey Tool designed and built by Sperry-Sun Well Surveying Company, a joint venture between Sun Oil and Sperry Gyroscope Co. The gyro had a DC Rotor speed of 14,000 RPM and was 5.5" Dia.
- 1930: Gyro Survey Tool Data used in settlement of many Lease Line violation cases in East Texas and California. In-Run and Out-Run Data were recorded.
- 1936: Gyro Tool Intercardinal Error and Drift Curve Corrections, refined to improve accuracy of survey data in inclined boreholes.  
Survey Tool True Centre Correction methodology developed using a two dimensional Polar Coordinate System Calculation.
- 1939: 1st K Monel Non Magnetic Drill Collar designed (Not a gyro but notable)
- 1945: Humphrey (Gyro) provides Instrumentation to Directional Service Companies for the first time (Post WW11 manufacturing surplus)
- 1947: Transistors developed but not yet used by industry.  
Sperry-Sun buys out Sperry Gyroscopes interest in Sperry-Sun Well Surveying Company.
- 1950's: By late 1940's wellbores get deeper and smaller with 5" Casing frequently used necessitating a requirement for smaller Gyro Tools.
- 1960: East Texas Railroad Commission Scandals again encourage tool development. Many wellbores are small diameter (5" Casing) and some have > 65 deg Inclination.
- 1961: Use of Solid State Electronics for first time in Instrument Timers and Solenoids for Film Advance mechanisms. Computers used for Survey Calculations at the Office. Field Data continued to be hand calculated until mid-seventies.
- 1961: Atomic Energy Commission (AEC) in the USA uses Gyro Survey Tools in 4" – 144" Dia. Test Holes, drilled 800 – 6000 ft deep, in Nevada and Alaska. Project ends in 1976.

- 1962: 3" Dia. Surwell Gyro built utilizing 40,000 rpm AC Rotor.
- 1964: Counter Claims made against Gyro Survey accuracy related to numerous Law Suits. A Test Pipe is laid down the Hurricane Messa in Utah. Over 2000ft of Aluminium Irrigation Pipe is fixed down the hillside on a continuously irregular course. The first 200ft was near vertical with sections of the pipe path reaching 60-70 degs of inclination. Multiple surveys were performed with both Gyro and Magnetic tools, with surveys taken at 25 ft intervals. In the final analysis the accuracy of both Survey Systems were proven and the East Texas Claims Issues finally settled.  
1.75" Gyro Tools developed using 26,000 rpm AC Rotors. Specifically designed for Directional Drilling Tool Orientation and surveying of Production wells in Tubing.
- 1971: Atomic Energy Commission Test Bore intersected at 6000 ft TD with Bottom Hole location land surveyed in at < 5 ft variance/error.
- 1974: Multi-well Platform drilling is prevalent. Level Rotor Gyro System developed with glass file Mercury Switch used to control the inner gimbal horizontal position to +/- 1-2degs but system is sensitive to gimbal/switch attitude, resulting in azimuth error propagation.
- 1977: Introduction of Surface Recording Gyros (SRG's - 3" and 1.75" versions), transmitting data to surface via Wireline. Inner gimbal position now monitored and controlled by electronic resolver to +/- 0.01 degs resulting in significantly reduced error propagation.
- 1978: Ferranti Full Inertial System introduced into the North Sea as reconfigured Harrier Jump Jet IN System, developed for Shell, Mobil, BNOB (BP) and marketed by Eastman Christiansen (Inteq). Proven Accuracy < 1/1000 ft potentially at all attitudes.

## 9.4 Improving Performance and Service Capability

As outlined above, Gyro Survey Tools were initially and primarily introduced into the industry, to provide a means of obtaining or checking borehole attitude, when the wellbore was already cased, negating the application or repeated use of magnetic based tools (Lease Scandals). Similar conditions were to foster the requirement for reduced diameter tools when later legal argument ensued over deeper smaller diameter wells. However, the primary motivation for technology advancement has been the requirement to survey ever deeper, higher angle boreholes (beyond horizontal), with significant azimuthal change at greater latitudes.

The first gyros used by the industry had no means of inner gimbal/spin axis control but the surveyor could determine its approximate position from the film record at each survey station. These gyros were originally intended for use up to 20 – 30 degs inclination. However, as borehole inclinations increased, hardware improvements were made and operational techniques were developed which enabled these tools to be used successfully beyond 60 degs inclination. As noted above, Gimbal Tilt control and Drift Curve correction methods were refined to better account for the increasingly difficult operating conditions encountered and its interactive effects on gyro stability and data quality at a relatively early stage.

## 9.5 The Gyro Survey Process

### 9.5.1 Surface Reference Orientation

Prior to the use of North Seeking Gyros the gyro had to be 'Referenced' and set to a known bearing at surface (On the rig floor) before entering the borehole. On land, this was a relatively simple process involving the establishment of a Sight Mark or Back Sight (Reverse Sight), from a distant mark clearly visible from the rig floor through the Sighting Scope oriented and attached to the Survey Tool in line with the internal Gyro Compass Reference. This Land Sight Mark was on occasion provided by the client, using the land survey company responsible for locating the rig but was often determined by the well survey company, using conventional land survey techniques and a Magnetic Brunton Compass. For low angle wells the gyro reference was then set to the Grid or True North orientation (dependent on the client requirements).



For offshore locations this observed and required Sight Reference had either to be pre-established (for each Slot Position) relative to Platform Centre or calculated using distant installations or features visible from the rig floor rotary. If/when no feature was visible from the rig floor the Sight Orientation Reference would be transferred from a position external to the rig floor (e.g. Helideck).

These techniques were also applicable to semi-submersible (floating) installations, with the added complication that the sight reference value might be subject to small but constant change. As a last resort the rigs Ships Compass Heading value would be used. This mobile condition had implications for both the start and end reference for the survey and its effect on Drift Curve closure and survey reference accuracy.

When setting the Gyro Orientation Reference for higher inclination surveys the gyro would be set with the spin axis perpendicular (oriented across) to the wellbore path, with due account taken of the expected gyro drift rate and any change in the wellbore azimuth trajectory. Setting the spin axis in this attitude, provides the most stable orientation for gyro operation as the gimbals tilt with inclination and reduces the potential for Gimbal Lock (System Bearing Jam) and subsequent gyro spin out and survey miss-run. The offset reference orientation value (relative to True or Grid North) applied in this technique was accounted and corrected for by applying a baseline shift to the calculated Drift Curve.

### 9.5.2 Gyro Drift – Precession Correction

The vast majority of gyro surveying performed for the industry, even today, still utilises rotor systems. A spinning gyro rotor tends to keep its axis pointing in the same direction. This is called Gyro Rigidity. If a force is applied which tends to change the direction of the spin axis, the axis will move at right angles to the direction of the applied force. If the spin axis is horizontal and you try to tilt it, the axis will turn. If the axis is horizontal and you try to turn it, the spin axis will tilt. This second characteristic of a gyro is called Precession.

In normal operational use, conditions such as bearing wear, Temperature Coefficients of Expansion (Inertial Mass Distribution – C of G) and System Attitude Change (related to a given well profile) all interact to generate a net force which acting on the Gyro Spin Axis cause the gyro to precess (drift from its initial orientation reference).

The gyro precession experienced during a survey has historically been corrected with a Drift Curve constructed with drift data samples recorded during the in-run and outrun survey. The frequency and duration of drift checks has tended to change over time but the basic premise has always been to take samples related to time, attitude change and temperature (particularly for deeper, hotter surveys). Drift checks were normally taken at least every 15 minutes, for a sample duration of 5 minutes with film systems. However, with the introduction of later Vernier scale readings, SRG and digital data, sampling criteria tended to change to 10 minute intervals with 3 minute sample duration.

Drift Checks during the survey were no longer relevant or required with the advent of earlier discreet sampling North Seeking Systems (more later). However, they are beneficial and recommended when operating the current North Seeking Systems in continuous Dynamic Mode where the individual or calculated survey sample stations are not determined by discreet north seek sensing.

The drift correction data is then either applied on its own or as a super set to the Gyro Calibration Model (current systems). The calculated real-time drift correction curve is tied and closed to the start and end reference data, be it a sight observation or north seek reference as in current technology systems.

### 9.5.3 True Centre Correction (or Offset Centre Correction)

From an early stage it was recognised that a gyro survey tool had inherent misalignments associated with the modular structure of the Instrument Stack and more particularly the vane type centralization (Weatherford) which was universally adopted for running in both open and cased hole. These centralizers were not a precision piece of manufactured equipment and variants of this centralizer design, all be it with improved centralization

capability, continue to be used today for some applications. These misalignments result in small errors in both the inclination and azimuth values calculated and recorded for each survey point.

In 1936 the Sperry-Sun Well Surveying Company developed a 'True Centre Correction' methodology which still forms the basis of current applications. The 'true centre' and 'corrected values' are calculated using a Polar Coordinate Method by representing each Station data set as a radial and angular coordinate. Provided sufficient tool rotation has taken place between the in-run and out-run samples, the common intercept of each sample vector pair denotes the True Centre Correction Value which can then be applied to each individual survey sample. True Centre Correction is particularly important in shallow, low angle, multi-well applications where small errors in Inclination can seriously misrepresent current well position and hence adjacent well displacement.

#### 9.5.4 Tool Centralization

Gyro Tool Centralization or Decentralization within the cased borehole remains a fundamental and important aspect of all gyro surveys performed. This applies equally to the limited number of surveys still carried out using older technologies as well as those performed with the latest systems inclusive of full inertial applications. As noted above, earlier forms of Spring Bow (Weatherford Type) centralizers could contribute significantly to errors in true borehole axis representation. Early attempts at offset calculation and correction did provide a partial solution but this improvement was also dependent on the centralizer integrity with respect to uniform vane wear and varying borehole inclination. As now, the main dilemma was to use centralization which adequately supported the tool in the central axis whilst allowing the system to smoothly progress down hole, keeping in mind the loss of effective mass ( $\alpha \cos \text{incl.}$ ) in the borehole axis to aid transport and the simultaneous increasing mass supported by the centralizers.

Ultimately, the most effective and practical solution was to run full centralization until the tool could be guaranteed to run low-side. However, dependent on the casing/survey program deployed, this procedure could require a minimum of two separate runs in hole in which the second run was performed with very stiff (rigid) under gage centralization which basically operated as skids and supported the tool at a fixed constant distance from the contact low-side and hence parallel to the borehole axis.

As wellbore inclination increased, various forms of Sinker Bar were used to aid tool transport but these too could generate off-axis problems where the Sinker Bar is screwed directly to the survey tool but not adequately supported (centralized), with a tendency to bias the overall tool alignment. Ideally, Sinker Bar should be attached to the survey tool using a universal joint or more preferably a connecting rod with universal joints at each end. This hook-up predominantly isolates any off-axis interaction between tool and weight bar.

These basic criteria still hold true today where the use of Centrollers (Precision Wheeled Centralizers) and Roller Bearing De-centralizers are used with North Seeking and full Inertial Gyro Tools in cased boreholes up to  $\approx 70^\circ$  inclination.

Ideally the use of De-centralizers should be avoided where possible, in large surface casings near vertical as tool alignment can be disturbed by the effects of off-axis cable tension. Similar problems can exist in the early build or high dogleg sections within smaller casings.

## 9.6 ERD and Horizontal Transit

With the prevalence of ERD and Horizontal Well Profiles, gyro surveying became even more difficult to perform by conventional wireline operations. Various techniques were adopted with improvements made relative to technology advances in both assisted tool transport and survey tool development.

### Side-Entry Sub

The Side-Entry Sub was first used with the Magnetic W/L Steering Tool Systems (Pre MWD) in order that drilling could proceed during deeper drilling operations without the requirement to trip out the W/L – Steering Tool from the drill pipe to make a connection (Add Pipe). Using this system enabled W/L Gyro Surveys to be performed in extended reach horizontal wells, with the survey tool latched within the BHA and surveys recorded at each planned depth interval.

The Side Entry Sub consisted of a sub with a side wall orifice with associated clamp and stuffing gland arrangement which allowed the cable to pass through the sub wall with the clamp and gland seal applied as required. The BHA/drill pipe would be tripped in hole to the high angle survey start depth. The W/L and survey tool would then be run to bottom within the pipe entering via the side wall sub connected to the drill pipe at surface. The survey would then commence by tripping in hole to TD with pipe added as normal. The assembly was then tripped out (with outrun data also recorded) to retrieve the Sub at surface with the W/L Tool then pulled out of hole. The system was subsequently applied to W/L FE logging prior to equivalent MWD sensor development.

## 9.7 Ring Laser Gyro

Ring Laser Gyros (RLGs) are a form of optical rotation sensor and unlike the preceding mechanical rotor systems, contain no moving parts, in their simplest form. Within the sensor, containing a machined quartz block, two laser beams are formed, one moving clockwise and the other anti-clockwise around an enclosed polygonal optical path loop of three, four or more sides with mirrors at the vertices. These laser beams interfere with each other, creating a standing wave(s) diffraction pattern observed by a photo-detector located at one of the vertex mirrors. This is a little like dropping two stones into a still pond, where the waves from each stone meet and form a pattern of waves with even higher peaks and lower troughs where they cancel out.

If the device is rotated, one beam experiences a shift up in frequency, whilst the other experiences a shift down, causing the interference pattern to move. As the device rotates the vertex photo-detector counts the fringes and hence measures the rotation of the sensor. This relativistic phenomenon, is known as the Sagnac effect after G. Sagnac (Frenchman) demonstrated and recognised the condition whilst conducting experiments to detect “the effect of the relative motion of the ether” (1913). Related experiments were also conducted by F. Harress in 1911 but his results were misdiagnosed at the time and attributed to “unexpected bias”.

Typically, a RLG consists of a triangular block of low-expansion quartz. The laser cavity is machined into the glass and filled with He & Ne creating an HeNe laser. A high voltage is applied across areas of this cavity to create the lasing action. At two points of the triangle, very high quality mirrors are placed and at the third vertice the beams are combined in a prism to produce the interference pattern which is detected by a photodiode array. Typically, RLG size is around 8cm on a side.

The sensitivity of a Ring Laser Gyro is proportional to the area enclosed by the laser beams and the scale factor of the instrument depends on the ratio of the enclosed area to the path length. RLGs can be extremely accurate devices and can measure a range of rotations from as low as 0.01 deg/hr to more than 360 deg/s. This gives them an enormous dynamic range, of as much as  $10^9$ . They have excellent scale-factor stability and linearity over this range.

Gyros performance is typically quantified in terms of bias stability and random walk. RLG can have bias levels of 0.01 deg/hr and random walks of 0.005 deg/rt (hr).

To ensure good sensor performance and bias stability the devices must be built in a high standard cleanroom, since any contaminants in the laser cavity will degrade performance. They must be machined from glass blocks with very low coefficient of thermal expansion to ensure that performance is maintained over a wide thermal range. The use of thermal shielding is essential for deeper oilfield applications.

RLGs suffer from a problem known as ‘lock-in’ where back scatter from the laser beams at a mirror causes the interference fringes to ‘lock’ together, giving the sensor a dead band, with no output at very low rotation rates. To minimise lock-in, extremely high quality mirrors are used. Also, typically the sensors are mechanically ‘dithered’, that is, vibrated rapidly and precisely through the dead band. It is small remaining periods in the dead band which causes the random walk performance of the sensor to deteriorate.

Ring laser gyros are very commonly used in inertial navigation systems in both civil and military aircraft, rocket launchers, tanks, artillery and high accuracy attitude systems, such as those used for geophysical surveys from the air.

RLG’s have only been utilised in one borehole survey system within the oil industry to-date. The RIGS Tool was developed by Sundstrand for Eastman Whipstock (Later to become part of Eastman Christiansen, Eastman Teleco and then Baker Hughes INTEQ). The Inertial Measurement Unit for a second generation RIGS was manufactured by Honeywell. The Tool was 5 ¼” in diameter, 14 ft long in standard configuration with a temperature rating of 100°C. A thermal shield allowed RIGS to survey to TD in wells with bottom hole temperatures of up to 150°C. The

RIGS Tool demonstrated consistent lateral accuracy performance of 1-2 /1000 MD (2 sigma) at all attitudes. However, the tool was only ever operated within the North Sea Region. It was in commercial service from 1990 to 2006.

The main drawback of currently available RLGs is their relatively large size, which limits their use to >5" dia. Sonde Tools operating within >7" casings. The sensors commercially available have a temperature limitation of around 90 deg C. RLG technology is also currently covered by international arms trafficking laws and associated import and export restrictions which severely restricts product placement, R&M and Tool Utilization for any potential global operation by a service company.

## 9.8 Fibre Optic Gyro

Fibre Optic Gyros (FOGs) consist of a coil of fibre optic cable in which two light beams travel through the entire cable length in opposite directions and are then combined. The development of low loss, single mode, optical fibre in the early 1970's, enabled Sagnac effect fibre optic gyros to be developed. The sensor operates on a similar principle to the RLG, where the interference pattern created from the counter-propagating light waves, after travelling through the fibre, is a measure of the angular rotation of the device. However, they differ in that an incoherent broadband light source is used.

Fibre optic gyros tend to be packaged in cylindrical containers, for example 10cm diameter by 2.0cm deep. A sensor may contain as much as 5 kilometres of fibre. FOG sensitivity is a function of coil radius (enclosed area) and optical path length, so once again larger sensors tend to be more accurate sensors.

FOG performance in general, is similar to but not quite as good as RLG. Bias stabilities of 0.1 deg/hr or better and random walks of 0.005 deg/rt(hr) would be typical. RLG has inherently better scale factor stability.

Outside of the oilfield, FOG sensors tend to be used for similar applications to RLGs, but for those applications where environmental conditions and accuracy is less important and where cost is a factor. Although experimental devices have been developed, no FOG system has been commercially marketed within the oilfield. Once again sensor size and temperature concerns are limiting factors. In general FOG performance is more sensitive than RLGs to environmental conditions such as shock, vibration and temperature gradients.

Large diameter, high accuracy systems have been developed and are in use in space and submarine applications, where size restrictions are secondary.

## 9.9 Vibrating Structure Gyroscope

### Coriolis Effect

The Coriolis Effect is an inertial force first described by the 19th century French engineer-mathematician Gustave-Gaspard Coriolis in 1835. Coriolis showed that if the ordinary Newtonian laws of motion of bodies are to be used in a rotating frame of reference, an inertial force – acting to the right of the direction of body motion for counter clockwise rotation of the reference frame or to the left for clockwise rotation – must be included in the equations of motion.

The effect of the Coriolis force is an apparent deflection of the path of an object that moves within a rotating coordinate system. The object does not actually deviate from its path, but it appears to do so because of the motion of the coordinate system. A simple demonstration example of the effect is a ball rolling across the surface of a rotating merry-go-round.



## 9.10 Coriolis Vibratory Gyros (CVG)

A Coriolis Vibratory Gyro (CVG) operates on the principal that a vibrating object (mass) tends to keep vibrating in the same plane as its support is rotated in space. This type of device is known as a Coriolis Vibratory Gyro where the plane of oscillation of a proof mass is rotated, the orthogonal response resulting from the Coriolis term in the equations of motion, is detected by a pickoff transducer.

CVGs have been produced in various forms, including the original Foucault pendulum (1851), vibrating beams, tuning forks, vibrating plates and vibrating shells. In the Foucault pendulum (non-commercial), the swing path of the pendulum rotates a fraction of the Earth's rotation, dependent on the location latitude. Due to friction effects in the mounting fixture, some of the energy is transposed into quadrature effects, so that the pendular path becomes elliptical and theoretically, ultimately circular, negating the angular measuring capability of the system. This unwanted quadrature effect is present in the majority of CVG designs and necessitates quadrature suppression control loop electronics, signal processing and compensation. Two CVG systems show potential [Tuning Fork Gyro (TFG) and the Hemispherical Resonator Gyro (HRG)] and these sensor developments are continuously kept under observation by the industry.

### 9.10.1 Micro Electro Mechanical System (MEMS) – Tuning Fork Gyro

A typical MEMS-TFG incorporates a single or dual (contra – mass-balanced) tuning fork (Proof Mass) arrangement, integrated on a silicon chip. Capacitive measurements are made between the fork tines (Proof Mass) as they contort relative to device rotation (Coriolis Effect). Current fabrication and manufacturing techniques enables the production of very small sensor devices with proof mass size typically only 1-5 mm. However, even the best commercially available MEMS gyro struggles to reach a bias performance of 1 deg/hr, with units in associated defence developments approaching 0.3 deg/hr. Oilfield applications requires the sensor have a performance capability within the range 0.1-0.01 deg/hr.

MEMS Gyros have to-date found a wide market in low performance applications. They are used in cars, smartphones, gaming systems etc. In the navigation world they are used to assist GPS acquisition in artillery shells, but have not yet been used for any form of unaided inertial navigation.

The small size and mass of current sensors results in lower performance and resolution with poorer signal to noise characteristics. Their size does however lend the device to thermal shield encapsulation providing the necessary thermal operating stability. Improved performance is expected to follow as the industry succeeds in developing techniques and production methods to produce thicker and larger component parts including the proof mass. This should result in improved stability and signal to noise characteristics and hence improved performance. These developments will hopefully lead to low volume, high accuracy, high value applications and the Holy Grail for down-hole surveying in small, rugged, robust, vibration insensitive, accurate inertial navigation systems which can operate throughout all phases of the drilling process.

### 9.10.2 Hemispherical Resonator Gyro (HRG)

The HRG is often referred to as the Wineglass gyro as the CVG properties for a wineglass were first discovered and noted by Bryan in 1891. Due to Coriolis Forces, a vibration standing wave pattern induced on a hemispherical, cylindrical, or similarly shaped resonating cavity, rotates relative to the gyro case by a fraction of the rotation angle experienced about the angle of symmetry. The wave rotation scale factor is a function of resonator geometry but for a hemisphere is  $\approx 0.3$ .

High quality Hemispherical Resonators are commonly machined from quartz, due to its excellent mechanical properties and it is the dimensional accuracy of the precision ground and polished unit which determines its accuracy. Temperature effects remain critical in this respect producing quadrature non-uniform mass distribution.

The system is robust, with almost no moving parts and can be very accurate, under strictly controlled temperature environments. Litton, now part of Northrop Grumman, produces a unit with  $< 0.01^\circ/\text{hr}$  performance which is used by the military and for space flight in which it has recorded millions of operating hours without failure. This system has potential for oilfield use but is expensive, requires significant temperature stabilization which results in size implications. The system is also covered by the international arms trafficking laws with all the implications and restrictions applicable as noted above for RLG.



## *CONTENTS*

## 10. Basic Gyro Theory

The purpose of this chapter is to explain the principles of gyroscopes and how such sensors are used specifically in *Gyrodata* gyro survey tools to determine borehole azimuth. This section was donated to the book by John Weston of *Gyrodata*, but the operating principles are largely applicable to any commercial rate gyros.

### 10.1 Fundamental Principles

Gyroscopes are used in various applications to sense either the angle turned through by a body (displacement gyroscopes) or, more commonly, its angular rate of turn, about some defined axis (rate gyroscopes).

The most basic and the original form of gyroscopes make use of the inertial properties of a wheel or rotor spinning at high speed. Many people are familiar with the child's toy which has a heavy metal rotor supported by a pair of gimbals. When the rotor is spun at high speed, the rotor axis continues to point in the same direction despite the gimbals being rotated. This is a crude example of a mechanical, or conventional, displacement gyroscope.

The operation of a conventional spinning mass gyroscopes depend the following phenomena:

- gyroscopic inertia
- angular momentum
- precession.

#### 10.1.1 Gyroscopic Inertia

This is fundamental to the operation of all spinning mass gyroscopes, as it defines a direction in space that remains fixed. The establishment of a fixed direction enables rotation to be detected, by making reference to this fixed direction. The rotation of an inertial element generates an angular momentum vector which is coincident with the axis of spin of the rotor or 'wheel'. It is the direction of this vector which remains fixed in space, given perfection in the construction of the gyroscope.

A practical reference instrument may be designed by having the rotor supported in a set of frames or gimbals which are free to rotate with respect to one another about orthogonal axes as shown in Figure 48. The orientation of the case of the instrument with respect to the direction of the spin axis may be measured with angle pick-off devices mounted on the gimbals.

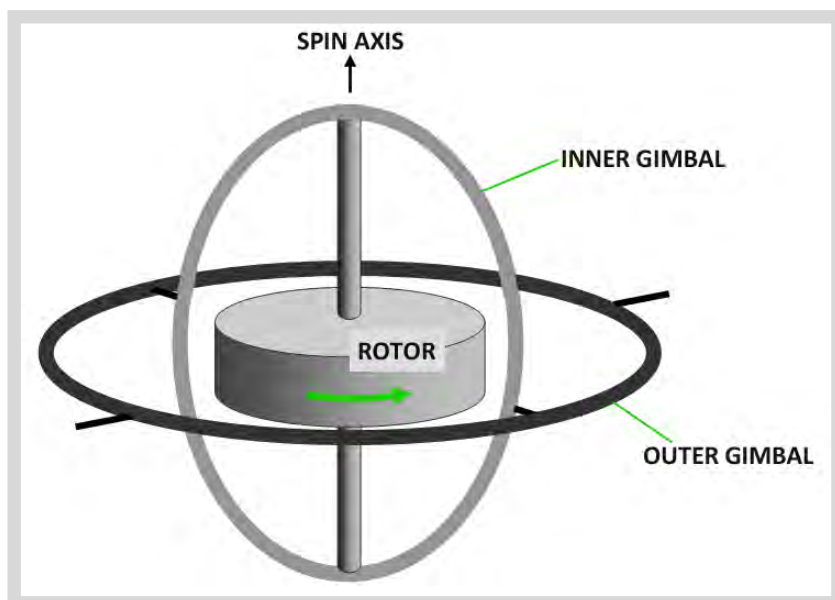


Figure 48: Schematic representation of a two axis gyroscope

### 10.1.2 Angular Momentum

The angular momentum of a rotating body is the product of its moment of inertia and its angular velocity. The angular momentum is chosen to be very high, so that the effects of undesired torques that can act on a rotor and cause errors are small. This results in a gyroscope with little movement of the direction of the spin axis. Any undesired movement of the direction of the spin axis is usually referred to as 'drift'.

### 10.1.3 Precession

The tilting or turning of the gyro axis as a result of applied forces. When a deflective force is applied to the rim of a stationary gyro rotor the rotor moves in the direction of the force. However, when the rotor is spinning, the same force causes the rotor to move in a different direction, as though the force had been applied to a point 90° around the rim in the direction of rotation.

A gyro will resist any force that attempts to change the direction of its spin axis. However, it will move (precess) in response to such force; NOT in the direction of the applied force, but at right angles to it, as illustrated in Figure 49. The figure shows the application of a force which gives rise to a couple about the torque axis. The resulting turning movement about the axis of precession causes the rotor to move to a new plane of rotation, as the spin axis attempts to align itself with the axis about which the torque is applied.

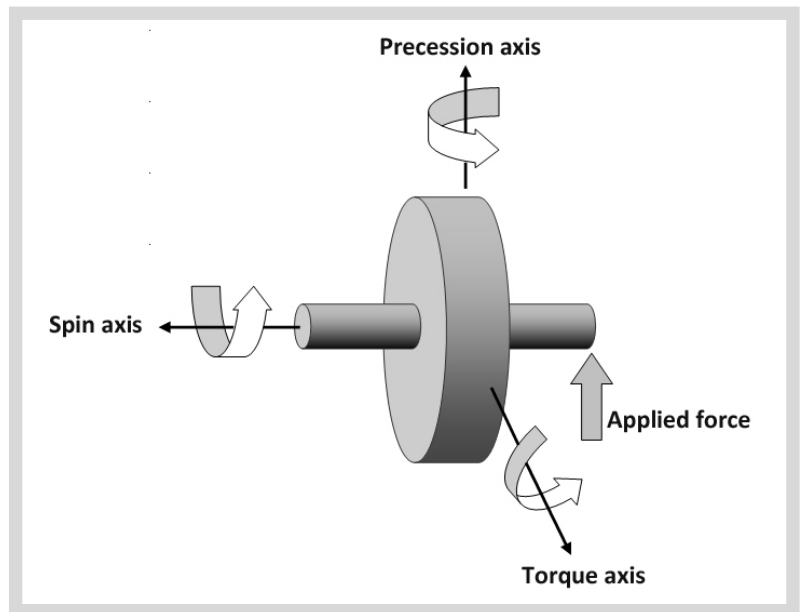


Figure 49: Illustration of gyroscopic precession

These rules apply to all spinning gyros:

1. A gyro rotor will always precess about an axis at right angles to both the torque axis and the spin axis.
2. A gyro rotor always precesses in a direction so as to align itself in the same direction as the axis about which the torque is applied.
3. Only those forces tending to rotate the gyro rotor itself will cause precession.
4. Precession continues while torque is applied and remains constant under constant torque.
5. Precession ceases when the torque is removed or when the spin axis is in line with the torque axis (the axis about which the force is applied).

### 10.1.4 The Application of the Precession Principle

The principle of precession can be exploited to provide a very accurate measure of angular rotation or rotation rate. Since a spinning wheel, or rotor, will only precess if a torque is applied to it, a rotor suspended in an instrument case by gimbals will maintain its spin axis in a constant direction in space. Changes in the angles of the gimbals will then reflect any changes in orientation of the case with reference to the spin axis direction.

Alternatively, if controlled torques are applied to the rotor to keep its spin axis aligned with a direction defined by the case of the instrument, then the measurement of these torques will provide measurements of the angular velocity of the instrument, and hence of the angular velocity of any body to which the instrument is attached. Various sensor configurations have been developed over the years based on the principles described above. Attention is focused here on the dual-axis gyroscope, the type of sensor used in *Gyrodata* survey tools.



## 10.2 Gyrodata Rate Gyro

The gyroscope used in *Gyrodata* tools is known as a dynamically tuned or tuned rotor gyroscope. It has two input axes (denoted x and y) which are mutually orthogonal and which lie in a plane which is perpendicular to the spin (z) axis of the gyroscope. The rotor is connected to the drive shaft by pairs of flexure hinges to an inner gimbal ring. This inner 'gimbal' is also connected to the drive shaft by a pair of flexure hinges, the two axes of freedom being mutually orthogonal. This is often called a Hooke's joint and allows torsional flexibility in two directions (it is noted that this mechanical arrangement constitutes an internal type of gimbal and is far more compact than the external gimbal structure shown in Figure 50). At the other end of the drive shaft is a synchronous motor. The gyro derives its name from the rotor suspension mechanism which theoretically allows the rotor to become decoupled from the drive shaft at a certain tuned speed; typically in excess of 12,000 rpm. The rotor contains permanent magnets which set up a radial magnetic field within the assembly.

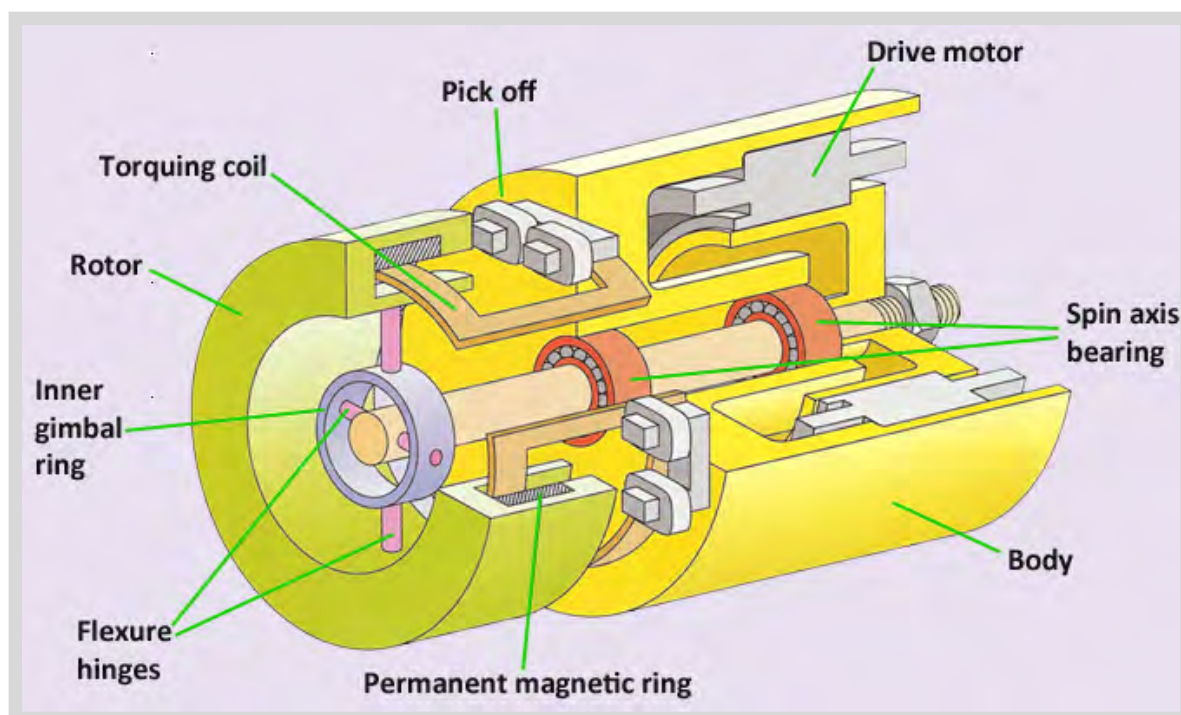


Figure 50: Dynamically tuned gyroscope

In the presence of an applied turn rate which causes a displacement of the rotor with respect to the case of the gyro, the spin axis of a rotor is made to precess back to the 'null' position by the application of a suitable torque. A very accurate angular measurement can be made, provided that the torque required to null the deflection can be generated and measured. The mechanism by which this is achieved is outlined below.

The angular position of the rotor is sensed by pick-offs attached to the case of the gyroscope. When rotor deflection occurs, the resulting pick-off signals are sent to the gyro servo electronics which in turn drives currents through the torquer coils. The interaction of the magnetic field generated by these currents with the field produced by the rotor magnets produces forces on the rotor which cause it to precess and so drive its deflection to zero. When the system is 'balanced', the currents in the torquer coils provide a direct measure of the angular rate to which the gyro is subjected.

This application of the precession principle enables very accurate measurements to be made of the rate of turn of the case of the gyroscope. The torque re-balance technique described is fundamental to the application of inertial measurement systems in which the sensors are attached rigidly to the survey tool (often referred to as strapdown

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systems) as employed in *Gyrodata* tools. The application of a rate gyroscope to determine the azimuth of a borehole relies on measurement of the Earth's rate of turn, which forms the subject of the following section.

### 10.3 Earth's Rate of Rotation

The Earth rotates about its polar (north-south) axis in 24 hours, rotating from West to East at a rate of approximately  $15^\circ/\text{hour}$ . The duration of a solar day is 24 hours, the time taken for an Earth fixed object to point directly at the Sun. The time taken for the Earth to rotate to the same orientation in space, known as the Sidereal day, is 23 hours 56 min 4.1 seconds. The Earth rotates through one geometric revolution each Sidereal day, not in 24 hours, which accounts for the slightly strange value of Earth's rate;  **$15.041067^\circ/\text{hour}$** .

Any point on the Earth's surface is moving in a circular arc because the Earth is spinning on its axis at this rate. The direction of the spin vector at any point on the Earth is parallel to the axis of rotation, i.e. the Earth's polar axis defined by the geographic North and South poles.

At any point on the Earth's surface, the Earth rate can be resolved into horizontal and vertical components as illustrated below.

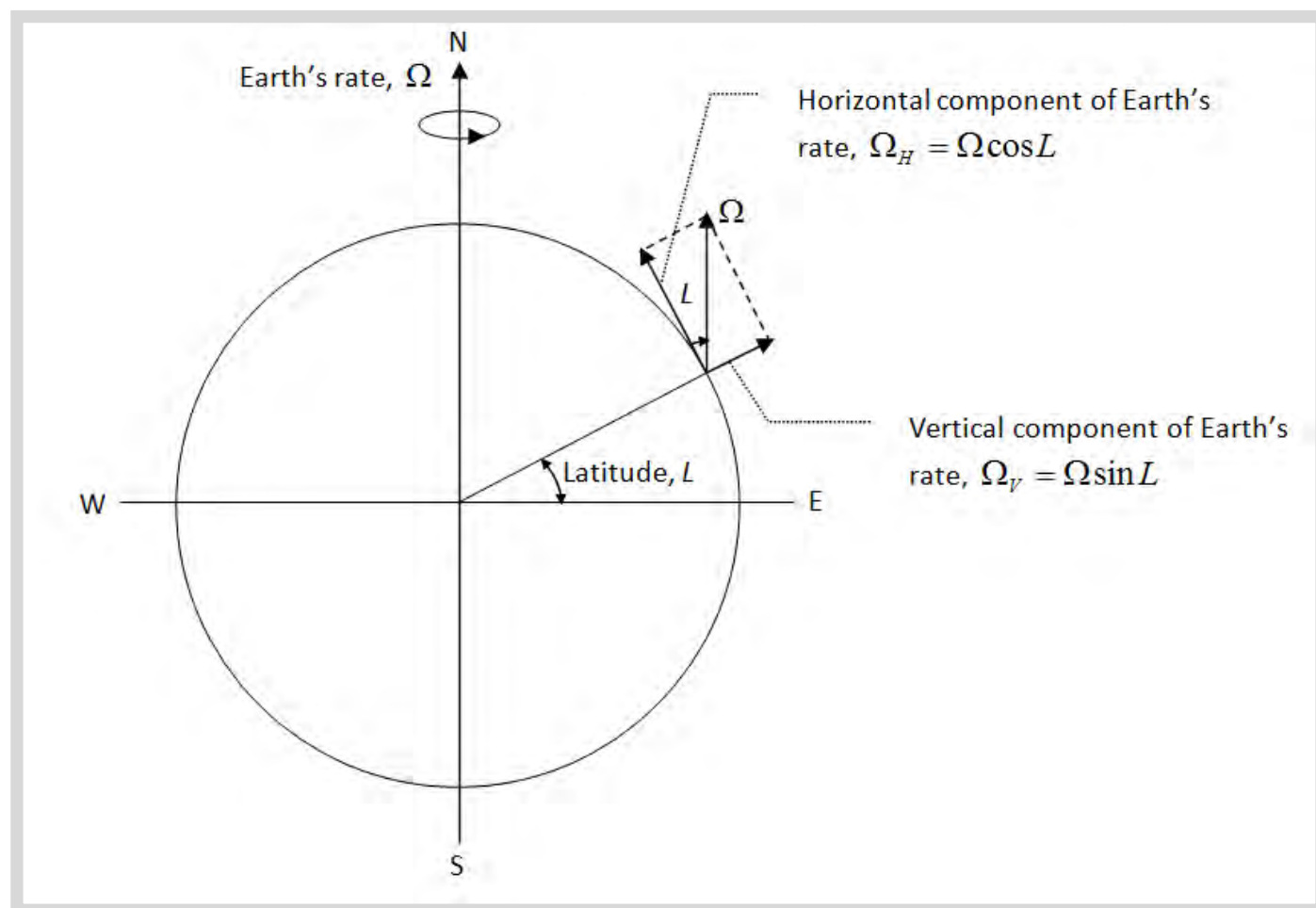


Figure 51: Calculating the Earth's rate of rotation

The horizontal component of Earth's rate always points towards the geographic North Pole and defines a reference direction to which the orientation of the survey tool can be measured using a gyroscope.

## 10.4 How to Measure Azimuth

So how does the ability to measure rates of rotation help us to determine borehole azimuth? For ease of explanation and understanding of the methods used in a gyro survey system, consider first the simple case in which a dual-axis gyro is mounted with its spin axis vertical so that its input axes measure the horizontal component of Earth's rate as depicted in Figure 52.

Calculate the gyro measurement about the axes -

x-axis;  $G_x = \Omega_H \sin \alpha$

y-axis;  $G_y = \Omega_H \cos \alpha$ .

It can be seen that the ratio of the x-axis measurement to the y-axis measurement defines the tangent of the direction ( $\alpha$ ) in which the y axis points with respect to the true north.

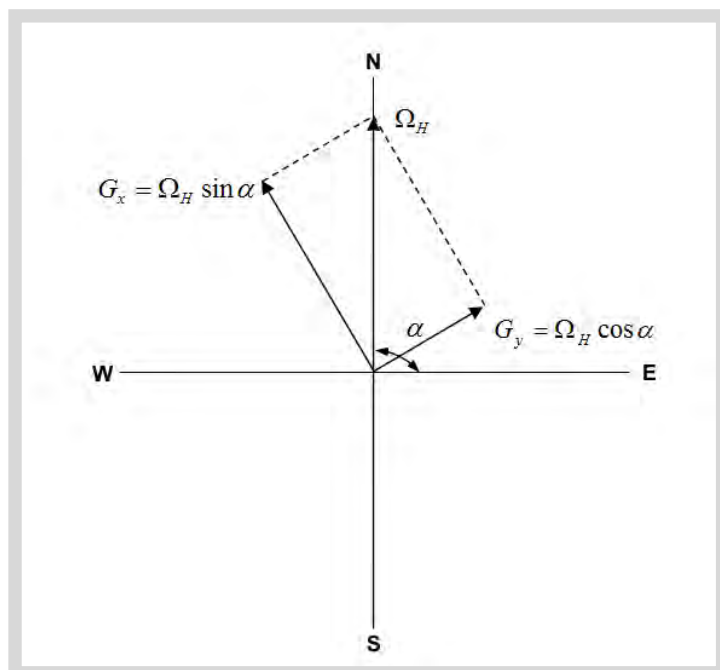


Figure 52: Measuring azimuth

In most practical constructions of rate gyro survey tools, sensors are attached rigidly to the tool with the result that the input axis of the rate gyro takes measurements in the plane perpendicular to the tool axis; not in the local horizontal plane. Therefore, direct measurements of the horizontal components of Earth's rate are only generated when the tool is vertical.

In general, the output from the gyro measures components of Earth's rate which include both vertical and horizontal components.

In order to define the azimuth direction of a borehole in which the tool is located, it is necessary to have knowledge of the direction in which the gyro input axes are pointing with respect to the horizontal Earth's rate vector. This may be specified in terms of the inclination of the well and the orientation of the gyro input axes with respect to the high-side of the borehole. This information can be determined using accelerometers installed in the tool with their input axes aligned parallel to the axes of the gyro as shown schematically in figure 53.

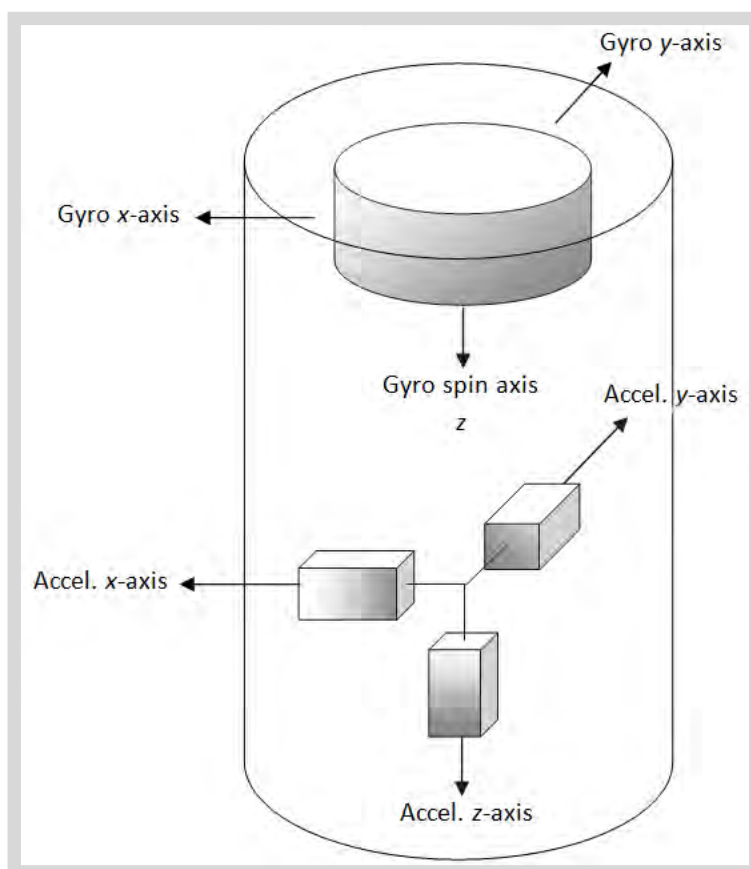


Figure 53: Instrument configuration with accelerometers

The accelerometers provide measurements of the xyz-components of the specific force acting on the tool due to gravity ( $A_x$   $A_y$   $A_z$ ). The outputs from the accelerometer allow the inclination ( $I$ ) to be calculated in accordance with the following equation.

$$I = \arctan \left[ \frac{\sqrt{A_x^2 + A_y^2}}{A_z} \right]$$

The accelerometer outputs are also used to determine the relation between the input axis of the rate gyro at each measurement position and the high-side of the hole, often referred to as the high-side tool-face angle (TF), as follows.

$$TF = \arctan \left[ \frac{-A_x}{-A_y} \right]$$

Given this information, the azimuth angle ( $A$ ) can be computed as a function of the gyro measurements, the inclination and tool-face angles and the vertical component of Earth's rate using the following equation.

$$A = \arctan \left[ \frac{(G_x \cos TF - G_y \sin TF) \cos I}{G_x \sin TF + G_y \cos TF + \Omega_v \sin I} \right]$$

**Summary:** The rate gyro survey tool uses accelerometers to measure components of the specific force due to gravity; these data are used to compute borehole inclination and to determine the position of all the sensors axes with respect to the high-side of the hole. The rate gyro is used to sense and accurately measure components of the Earth's spin rate from which the azimuth can be calculated. The horizontal component of Earth's rate always points to TRUE NORTH.

## 10.5 Sensor Errors

All gyroscopic sensors are subject to errors which limit the accuracy to which the angle of rotation or applied turn rate can be measured. Spurious and undesired torques (caused by design limitations and constructional deficiencies) act on the rotors of all mechanical gyroscopes. These imperfections give rise to precession of the rotor, which manifests itself as a 'drift' in the reference direction defined by the spin axis of the rotor. For a restrained gyroscope, i.e. one operating in a nulling or rebalance loop mode to provide a measure of angular rate as described in Section 3, any unwanted torques act to produce a 'bias' on the measurement of angular rate.

Major sources of error which arise in mechanical gyroscopes include the following:

1. Fixed bias – a sensor output which is present even in the absence of an applied input rotation;
2. Acceleration-dependent (g-dependent) bias – biases in the sensor outputs proportional to the magnitude of the applied acceleration. In this context, mass-unbalance effects are of particular concern, and are discussed further below
3. Anisoelastic (g<sup>2</sup>-dependent) bias – bias proportional to the product of accelerations applied along orthogonal axes of the sensor;
4. Scale factor errors – errors in the ratio relating the change in the output signal to a change in the input rate which is to be measured;
5. Cross-coupling/misalignment errors – errors arising because of gyroscope sensitivity to turn rates about axes perpendicular to the input axes, or is mounted in a position that is physically misaligned with respect to the required measurement axis.

Each of these errors will, in general, include some or all of the following components:

- fixed or repeatable terms

- temperature induced variations
- switch-on to switch-on variations
- in-run variations

For instance, the measurement of angular rate provided by a gyroscope will include:

- a bias component which is predictable and is present each time the sensor is switched on and can therefore be corrected following calibration
- a temperature dependent bias component which can be corrected with suitable calibration
- a random bias which varies from gyroscope switch-on to switch-on but is constant for any one run
- an in-run random bias which varies throughout a run; the precise form of this error varies from one type of sensor to another.

The fixed components of error, and to a large extent the temperature induced variations, can be corrected to leave residual errors attributable to switch-on to switch-on variation and in-run effects, i.e. the random effects caused by instabilities within the gyroscope. It is mainly the switch-on to switch-on and in-run variations which influence the performance of the survey system in which the sensors are installed.

### **Gyro mass unbalance**

The performance of a mechanical gyroscope is extremely sensitive to mass unbalance in the rotor suspension, i.e. non-coincidence of the rotor centre of gravity and the centre of the suspension mechanism. Minute mechanical changes sufficient to affect gyro performance can arise as a result of shock and vibration to which the survey tool may be subjected; either down-hole or at surface as a result of knocks sustained during transport and surface handling. Movements of the rotor centre of gravity with respect to the suspension mechanism of a few nano-metres will produce changes in mass unbalance that are sufficient to give rise to significant changes in measurement accuracy.

**Summary:** Variations in the residual systematic bias components and the g-dependent bias caused by changes in mass-unbalance present the major concern in survey systems incorporating mechanical gyroscopes. Survey correction techniques are implemented, either during or after a survey operation, in order to compensate for survey inaccuracies resulting from the effects of these particular gyro errors.

## 10.6 Survey Tool Calibration



The purpose of calibration is to evaluate the coefficients for the various 'error' terms described above. Having established the performance figures or 'characterised' each sensor, any systematic errors may be compensated thus enhancing its accuracy.

To achieve this, the survey tool is placed on a calibration stand which allows the tool to be rotated between a series of known fixed orientations with respect to the local geographic axis set defined by the directions of true north and the local gravity vector. At each position, the turn rates and accelerations to which the sensors will be subjected in each controlled position are very accurately known. The series of positions are selected to excite each error contribution and so allow each error term to be identified separately and evaluated.

The highly accurate, custom made calibration stands used for this purpose were designed and developed by *Gyrodata*. Each calibration stand comprises a stabilised gimbal system with precisely controlled and instrumented gimbal angles. The stands are mounted on a plinth of granite that has its own foundations separate from, and vibrationally isolated from, the laboratory. The stands are aligned to true north within 0.001 degrees and are able to rotate the tool to any angle of inclination, azimuth or tool-face to an accuracy of 5 arc seconds (5/3600 degrees).



Figure 54: Typical calibration stand

## 10.7 Survey Tool Operating Modes

*Gyrodata* gyroscopic survey tools contain up to three accelerometers and up to two dual-axis gyroscopes installed in various configurations within the survey tool. Systems designed to operate at all attitudes generally require a full complement of gyroscopes and accelerometers in order to provide measurements of both angular rate and acceleration about three orthogonal axes; essential for all attitude operation.

Some systems operate by taking sensor measurements at discrete intervals of depth along the well path trajectory when the survey tool is stationary, in what is described as gyro-compassing mode. Such systems provide estimates of inclination, high-side tool-face and azimuth angle as described above. Other systems can be operated in a continuous measurement mode. Given knowledge of the survey tool orientation at the start of a period of continuous surveying, changes in attitude that occur thereafter can be tracked by effectively integrating the subsequent gyro measurements of turn rate as the survey tool traverses the well path.

### 10.7.1 Gyro-compassing Mode

Gyro biases, which have an unpredictable behaviour, are measured and corrected for directly at each gyro-compassing station through a process of indexing the gyro. This involves mounting the gyro on a rotatable platform and driving it between two positions that are 180° apart. Measurements of turn rate are taken when the gyro is stationary at each index position. Whilst the turn rate to which the gyro is subjected is reversed between the two index positions, any bias which is present in the measurements remains fixed. Hence, an estimate of the measurement bias can be obtained by summing the two measurements and dividing the result by two. Any residual bias which remains can still be significant and must therefore be estimated in the field.

Gyro mass unbalance is stable when the gyro is at rest. However, as discussed earlier, it may change significantly if the gyro is exposed to a mechanical impact, as can occur during transportation or surface handling. The average mass unbalance for the entire survey should therefore be estimated and corrected in the field.

Accelerometer calibrations are usually very stable, but they can change over time or as a result of temperature exposure. It is therefore important that the performance of the accelerometer pack is always verified for every recorded measurement and for the survey as a whole.

*Gyrodata* has developed a method for field calibration while surveying known as Multi-Station Correction (MSC). It is impossible to determine accurately all of the calibration terms in the field, the goal of MSC is therefore to correct those terms that are more likely to change, namely gyro fixed biases and mass unbalance, whilst at the same time minimising the effect of residual errors in other terms. In addition, a MSC accelerometer test has also been included, to check the accelerometer measurements throughout the survey; only applicable for survey tools containing three accelerometers. MSC is a very powerful tool that updates the calibration values of residual biases and direct mass unbalance for the gyro and checks the performance of the accelerometer package. Additionally, since MSC is based on a least-squares adjustment technique, the standard deviations of the x and y gyro biases and mass unbalance are generated. This information is checked against the tolerance defined by the gyro error model and forms an essential part of the quality control (QC) procedure that is implemented each time a survey tool is run.

### 10.7.2 Continuous Mode

Attitude data derived using continuous gyro survey systems have a tendency to drift exponentially with time. In many gyro systems, it is common practice to compensate for this effect by forming estimates of the drift at regular intervals during the survey. This is achieved by holding the tool stationary for short periods of time, and subtracting the estimated components of Earth's rate so which the tool is subjected at the current location. The drift estimates generated by this process are the accumulated effect of all physical errors at the given interval, and are used to implement a real-time re-calibration of the tool. The quality and effectiveness of this re-calibration are dependent on many factors that are difficult to predict, including the change in tool-face. It is almost impossible to keep track of what happens to the different physical sources of error when drift compensation is applied.

Studies of field data, where comparisons of in-run and out-run surveys have been made, indicated that accumulated azimuth error in most continuous surveys can be estimated using four simple empirical parameters. The four empirical parameters are:

- the error of the initial reference
- a term proportional to measured time (gyro drift)
- a term proportional to the square root of measured time (random walk)
- a random error which is irrelevant for position error calculations.

Whilst the use of empirical error sources is a departure from the usual form of error model linked to physical uncertainties, it does allow realistic uncertainty estimates to be produced. *Gyrodata* has developed a new method for final calculation of continuous surveys called Continuous Drift Correction (CDC). It is logically equivalent to averaging in-run and out-run surveys, but adopts a more complex approach which facilitates the estimation of error model terms, including the linear drift and random walk components.

CDC also checks for tool misalignments provided that the in-run and out-run high-side tool-faces are not the same throughout the survey. The misalignment correction compensates for systematic misalignment for the whole survey and provides additional quality control to the data. The use of CDC provides several benefits compared to a simple in-run/out-run comparison. It corrects for linear drift and systematic misalignment and allows QC checks to be implemented by providing estimates of residual errors that can be checked against the tool error model.

### 10.7.3 Summary

Stationary gyro-compassing and continuous survey methods have been outlined along with procedures developed by *Gyrodata* for quality control of the resulting surveys. The powerful MSC and CDC methods provide comprehensive quality control, for stationary and continuous surveys respectively, and tool performance characteristics linked directly to the respective tool error models.



***CONTENTS***

## 11. When to Run Gyros

Running gyro surveys is nearly always a benefit to survey accuracy and provide verification of the MWD surveys, but clearly the benefit has to be worth the cost. There are certain circumstances however, where running gyros are the only option for a safe and adequately accurate survey. Please note that in most of these scenarios apart from a) below, the assumption is that the gyro used is of sufficient accuracy to exceed the accuracy of the MWD. That is not always the case depending on the type of gyro and the expected performance of the gyro must be ascertained by suitable QC to ensure adequate accuracy.

- a) When magnetic interference from nearby steel preclude the use of MWD.

These circumstances include the following;

- Measuring inside casing
- Measuring close to casing shoe
- Measuring close to adjacent wells
- Measuring close to surface or shallow beneath the rig
- Measuring close to a fish or when side-tracking close to original casing.

This would naturally, include conductor surveys after conductors have been driven. This often neglected practice ensures that the collision risk assessment is based on the actual as built positions of the conductors and not an assumption that they landed vertically and parallel. It is not unknown for driven conductors to cross two rows of slots from their original surface position so the slot/ target allocation often has to be reviewed in the light of the conductor survey. When the casing of the nearest well is 50ft or more away it is usually considered to have negligible effect on MWD azimuth accuracy but the effect rises rapidly with proximity so gyros are often prescribed when separation from casing drops to 30ft or so.

- b) When TVD accuracy is required less than 3/1000 on step out. This is very difficult to achieve with MWD in open hole and whilst the accelerometers may be just as accurate as the gyro sensors in the vertical plane, the hole quality and the measurement environment cannot deliver this level of accuracy with confidence.
- c) When the MWD is surveyed every 90 ft but with dogleg severities exceeding 6°/100ft the MWD survey interval will not adequately represent the wellpath. Here the gyro provides a higher resolution survey and can be requested at very small intervals although 25 ft is common.
- d) When the target dimensions are less than 2% of the step out (1% if IFR is employed). This size of target will not leave sufficient room for the directional driller to steer successfully without the reduction in uncertainty afforded by a high accuracy gyro survey for at least part of the well bore.
- e) Anywhere, where the separation factor requirements cannot be met using MWD alone.
- f) In side-tracks where the original hole contains a fish, or casing and the accuracy requirements demand an adequate survey during the side-track section close to the original hole.
- g) When drilling close to leaselines, geo hazards, fault blocks or other 'hard line' boundaries where MWD uncertainty wastes too much pay.



## 12. Correcting for Sag

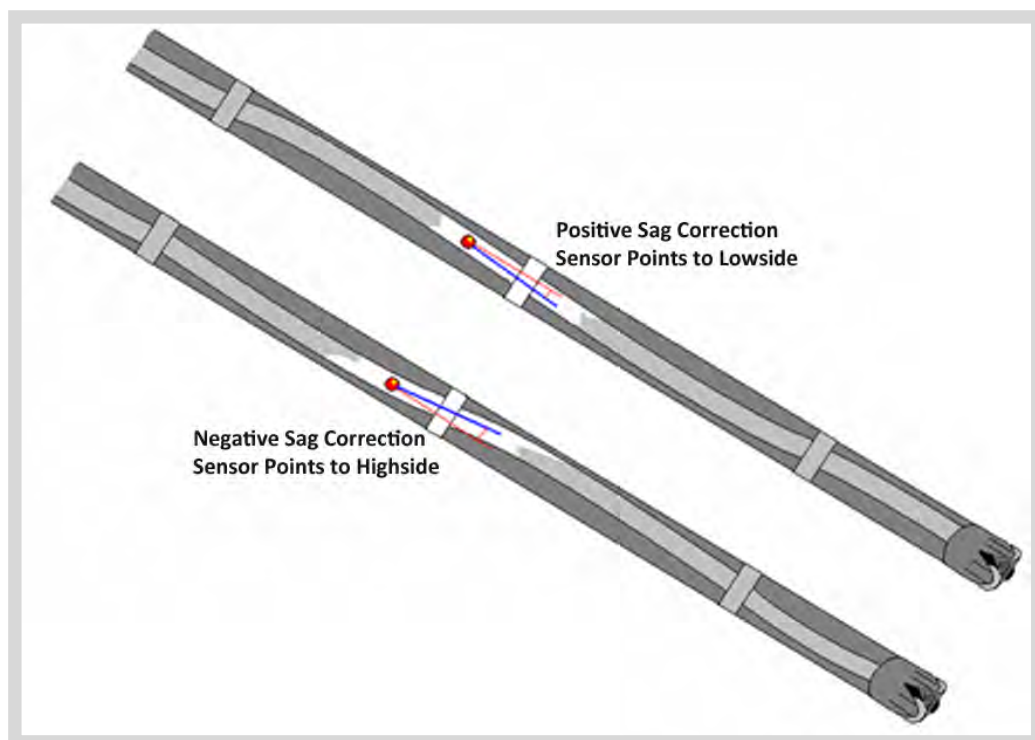


Figure 55: Sag correction schematic

The BHAs used in directional drilling are designed to be flexible enough to drill round curves. Inevitably this leads to deflections in the BHA centreline which is unlikely to remain parallel to the wellbore. As a result, the inclination observed may need to be corrected for the misalignment between the MWD sensor and the wellbore centreline.

### Sag Correction Software

Since finite element software or mechanical beam theory techniques are used anyway to model the side forces and stresses on a BHA as part of its performance design, the same software calculates the deflected shape of the BHA and can predict in advance the corrections needed to apply to the observed inclination. This is often the most important correction required for high angle drilling accuracy for good TVD placement. In the above example, there is also a mechanical bend in the BHA at the bent housing so the sag correction may not be just inclination dependent but may also be toolface dependent if the assembly has a bend that can be oriented.

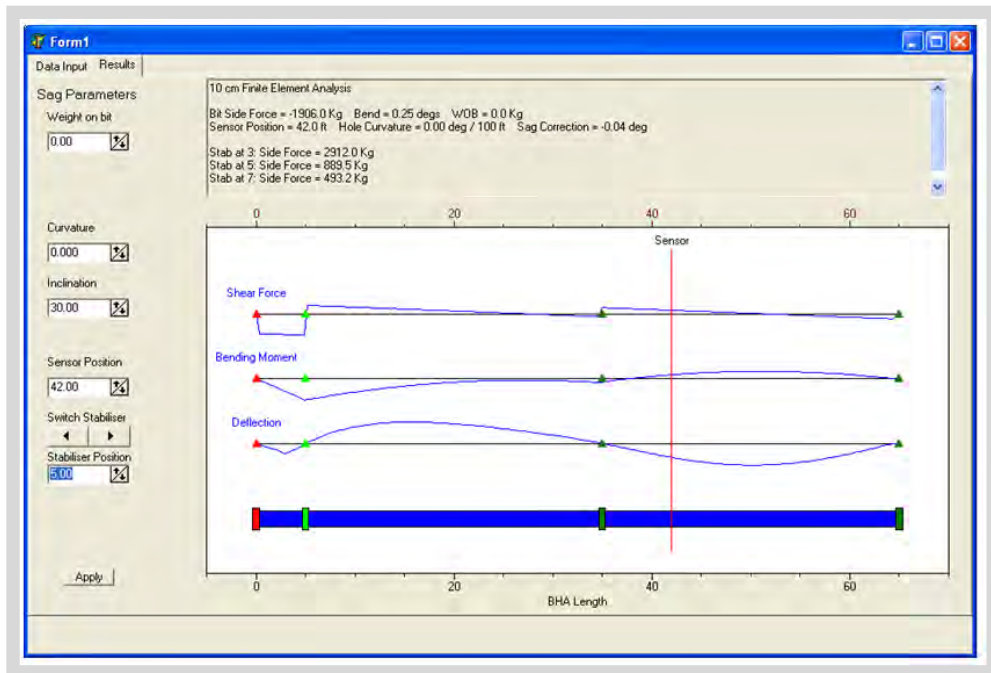


Figure 56: Typical sag correction software output

Generally, at low inclinations sag will be minimal but as it is mainly due to gravity effects, the magnitude is likely to increase with the sine of the inclination. Here is a typical sag sheet with corrections over a range of inclinations.

Sag Sheet

Sensor Position = 55.43 ft

Inc	Sag (deg)	Inc	Sag (deg)
0.0	0.000	60.0	0.177
5.0	0.018	65.0	0.186
10.0	0.036	70.0	0.193
15.0	0.053	75.0	0.198
20.0	0.070	80.0	0.202
25.0	0.087	85.0	0.201
30.0	0.102	90.0	0.201
35.0	0.118	95.0	0.201
40.0	0.132	100.0	0.202
45.0	0.145	105.0	0.198
50.0	0.157	110.0	0.193
55.0	0.168	115.0	0.186
60.0	0.177	120.0	0.177

Care should be taken when using bent housings in the BHA since the sag correction will then be toolface dependent. In such cases, the sag should be calculated on site using software which can include the bend in the finite element analysis when applied at any toolface.

It is recommended that any well that build above 45 degrees at any point should be sag corrected as a matter of course. This is a service that most drilling contractors can easily include and the effect on TVD accuracy is often dramatic.



If we use the approximate rule of thumb that 1 degree of angle produces 2% of distance as an error in position, even a small inclination error like 0.25 degrees will produce 0.5% of step out as an error in TVD. For example, if the step out to a reservoir entry point was 3000 ft, the TVD error would be + or – 15 ft for only a quarter of 1 degree of sag.

In the analysis of misplaced wells identified by poor production or a poor match with expected geological formation depths, the lack of sag correction is the most common cause. The cost of carrying out sag correction is far outweighed by its benefits in terms well positioning particularly at the entry point to the reservoir.



## *CONTENTS*

## 13. Correcting for Magnetic Interference

### 13.1 Drilling Magnetisation

It is well known that the MWD sensors in themselves are extremely accurate but the weak link in the system is the accuracy of the magnetic field in which the azimuth readings are taken. We discussed earlier the effects of local crustal anomalies on the accuracy of our background reference vector but in this section we will look at the effects of the drillstring magnetisation which is always

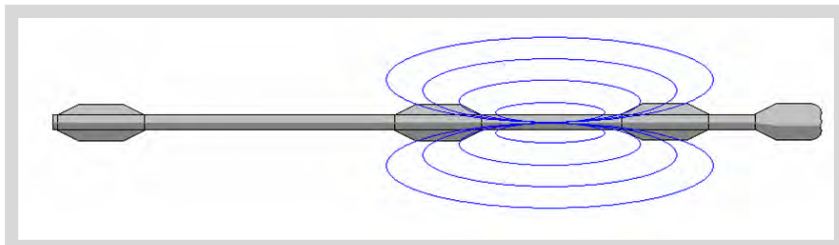


Figure 57: Drillstring magnetisation

present to some degree. It should be noted however that since the sensor pack is always set inside non-magnetic material, the major interference component is likely to be either from below or above the sensor in the drillstring and therefore the z axis interference is usually the major influence on azimuth accuracy.

In the 1990s, Dr Robin Hartman of Shell International developed SUCOP (Survey Correction Program) to implement a technique for measuring and removing the magnetic influence of the drillstring.

If a magnetometer is placed in a magnetic field it will measure the component of the field along its own axis. A good analogy is if a tube with a small flow meter was inserted in stream, the flow through the tube will be the component of flow along the axis of the tube. Clearly if the tube is held perpendicular to the flow there will be no flow in the tube and if it is in line with the flow it will experience the full flow rate of the stream. At any other angle it will experience the flow vector  $\times$  cosine of the angle of incidence. This value is often referred to as the vector dot product. This can be defined as the product of two vector lengths  $\times$  cosine of the angle between them.

In figure 58 the magnetic field is represented by the green arrows and the magnetometers will only measure the component of that field along their own axis.

Now imagine two magnetometers facing in opposite directions at some angle to the magnetic field. Clearly they will read the same magnitude of field but with opposite signs. Hartman realized that if an MWD sensor pack was rotated around the z axis, the x and y magnetometer readings would follow a sine wave which should have an average of zero. If the average was anything else, there must be a component of the observation which is permanent. This will be some combination of a sensor bias or a magnetic field component which is rotating with the sensors and is never going away.

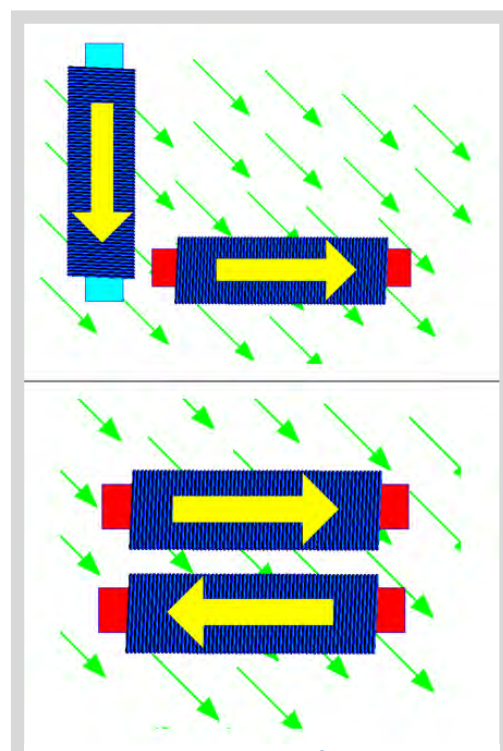


Figure 58: Axis components of magnetometers

*In the field, the driller could observe raw sensor readings at several toolfaces (a rotational shot or cluster shot) and record the values on the x and y axes.*

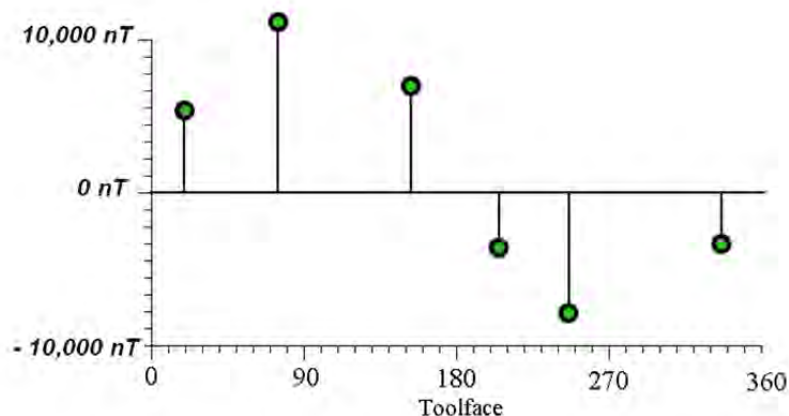


Figure 59: Straight plot of sensor readings

*If a mathematical sine wave was then made to fit this variation, the average value could then be derived as if the readings had been taken evenly around the clock.*

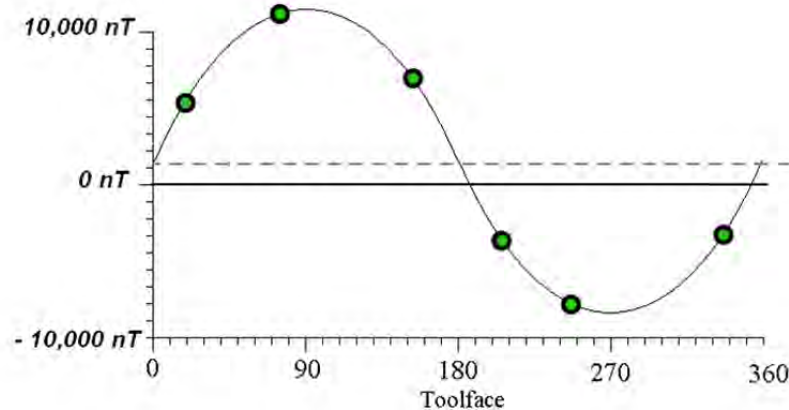


Figure 60: Adding a mathematical sine wave to fit the sensor readings

In this example, the magnetometer is clearly carrying a positive magnetic field value that is not going away.

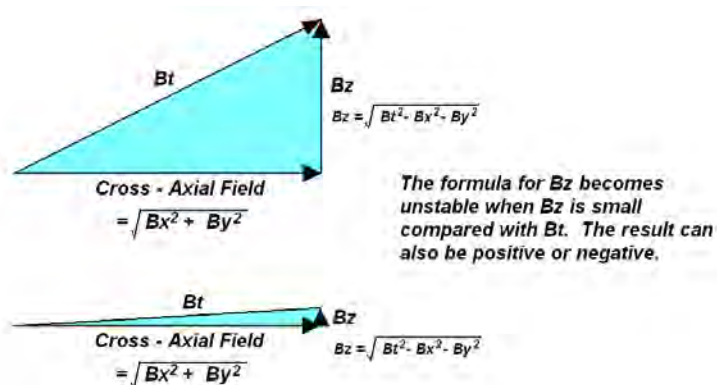
This rotational data can then be used to correct the x and y magnetometer values for this bias. This still leaves the potential for a further magnetic field bias on the z axis. In practice the z axis is often the most significant direction of influence since the significant magnetic material in the drill string is always above or below the MWD sensors. Clearly it is not possible to flip the z axis so the clean z axis is derived from the following formula:

$$\text{Clean } B_z = \sqrt{B_t^2 - \text{Clean } B_x^2 - \text{Clean } B_y^2}$$

In this formula,  $B_t$  means the total background magnetic field strength and  $B_x$ ,  $B_y$ , and  $B_z$  mean the sensor axes readings from the magnetometer. This formula relies on the accuracy of  $B_t$  and ideally should have an IFR survey to accurately measure  $B_t$ . This simple technique allows the surveyor to calculate bias values for all three axes and remove the majority of the magnetic interference from the subsequent observations.

One caveat that should be kept in mind is the stability of the calculation. The value for  $B_z$  is very sensitive to azimuth and inclination.

The formula is identical to a Pythagoras formula for calculating one side of a right angled triangle where  $B_t$  would be the hypotenuse and the base would be the cross axial field as follows.



If the value of  $B_z$  is very small, which will happen when drilling at high angle heading East or West, the resolution of clean  $B_z$  will be extremely sensitive to the accuracy of the other two sides. The slightest error in  $B_t$  can produce a very exaggerated effect on  $B_z$  and, in many cases, produce a value in  $B_z$  more erroneous than the magnetic error. In other words, this technique should not be used in such geometries in case the correction is more erroneous than the original reading.

eg  $B_t = 50,000 \text{ nT}$

$$B_x^2 + B_y^2 = 49800 \text{ nT}$$

$$B_z = \sqrt{B_t^2 - B_x^2 - B_y^2} = 4467 \text{ nT}$$

suppose error in  $B_t$  is  $100 \text{ nT}$  and  $B_t$  appears as  $49900$

$$B_z = \sqrt{B_t^2 - B_x^2 - B_y^2} = 3157$$

So  $100 \text{ nT}$  on  $B_t$  causes  $1300 \text{ nT}$  in  $B_z$  !!

For this reason and because the  $B_z$  value can be positive or negative it is not recommended that this technique be employed in the following 'no go zones' - above 70 degrees inclination within 20 degrees of East / West (magnetic).

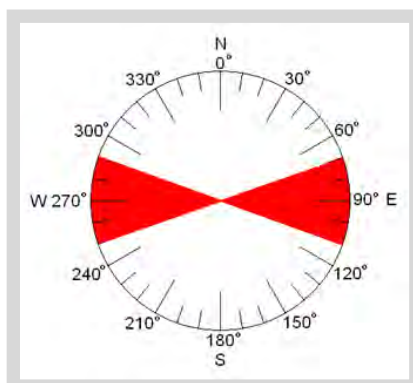


Figure 61: 'No go zone' for axial correction



## 14. Multi Station Analysis

### 14.1 Calculation and Background

A more recent development on the principle of magnetic interference correction is the use of Multi Station Analysis.

This technique is similar to the rotational shot technique described above but makes use of all available MWD data so far collected to 'best estimate' corrections to apply retrospectively. This is heavy on computing time but with modern computers allows a great deal more flexibility in what we analyse for. In the section following the mathematics will be set out but for now, the principles and process steps are as follows.

Earlier we discovered that a magnetometer will read a magnetic field value along its own axis. It is therefore possible to calculate a theoretical value if we know the background field vector and the 'attitude' (Inclination and Direction) of the sensor axis. If we gather a lot of raw data from multiple survey stations (with the same BHA), we can examine the consistency of the data versus the theoretical values and try to find corrections on each sensor that make for the least error.

This is known as Multi Station Analysis and since it is using all the raw data over several stations, in theory, there is no need to carry out a cluster shot since there will be variations in attitude anyway between each survey station. It should be said however, that cluster shots are strongly recommended at the start of the BHA run to produce a strong estimate of corrections before drilling much further on what could be a wrong azimuth.

The steps are as follows:

1. Over several readings observe  $B_x$ ,  $B_y$ ,  $B_z$ ,  $G_x$ ,  $G_y$  and  $G_z$
2. Calculate inclination, direction and toolface as normal
3. Calculate the unit vectors that describe the attitude of each magnetic sensor
4. Calculate the theoretical value that should have been read
5. Record the errors (residuals) on each sensor
6. Calculate the sum of the squares of these residuals
7. Try variations of scale and bias corrections on each sensor until the result of step 6 is minimised
8. Apply these best fit biases and scale factors over the whole survey

**The next section may help the mathematicians amongst you understand the steps more clearly, and for the rest, may offer an alternative to counting sheep.**

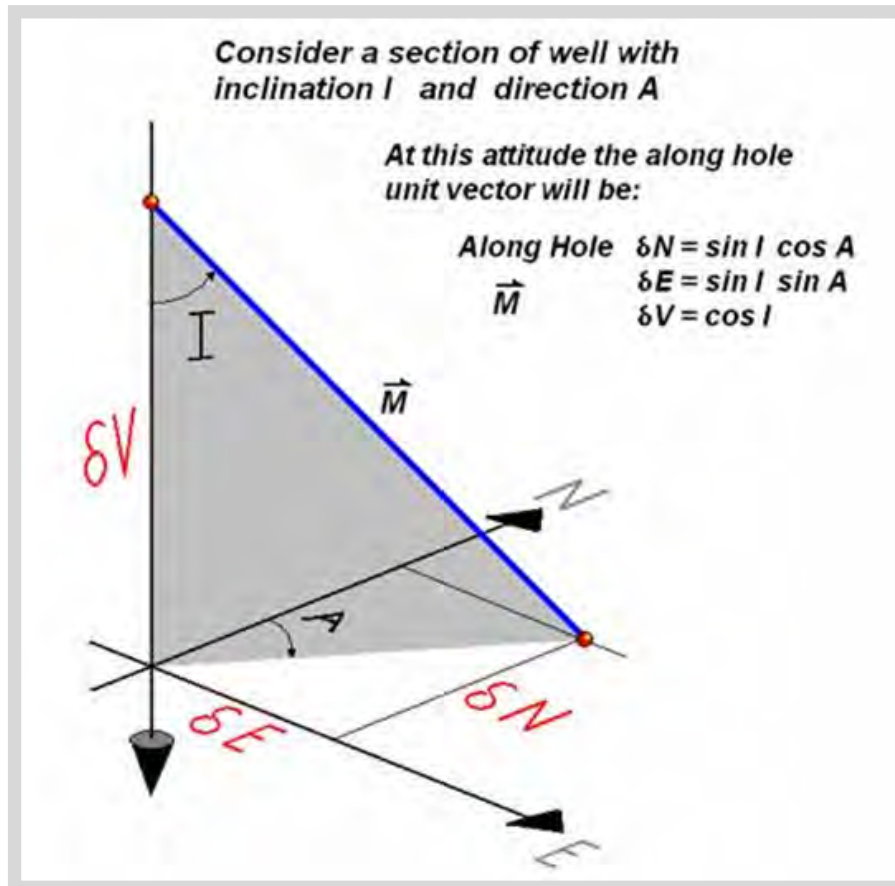


Figure 62: Establishing the unit vectors for each sensor axis



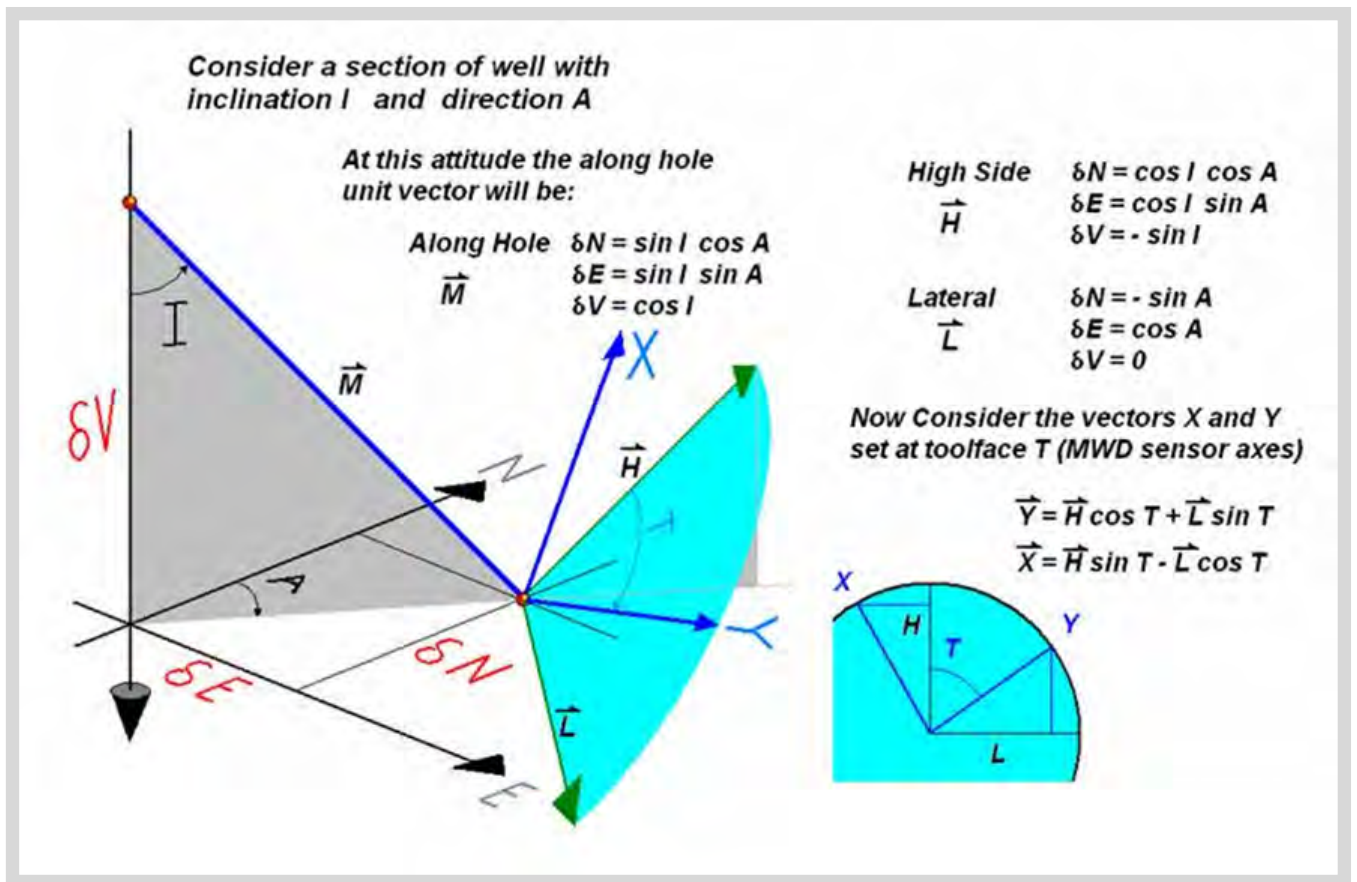


Figure 63: Extending the calculation for the unit vectors for each sensor axis

These formulae describe the high side unit vector and the lateral unit vector from which we can derive the axes vectors when sitting at any given toolface from high side;

*In summary, at Inclination I, Azimuth A and Toolface T*

*The unit vectors of the MWD sensor axes are as follows:*

$$\begin{aligned} \text{Y axis } \delta N_y &= \cos I \cos A \cos T - \sin A \sin T \\ \delta E_y &= \cos I \sin A \cos T + \cos A \sin T \\ \delta V_y &= -\sin I \cos T \end{aligned}$$

$$\begin{aligned} \text{X axis } \delta N_x &= \cos I \cos A \sin T + \sin A \cos T \\ \delta E_x &= \cos I \sin A \sin T - \cos A \cos T \\ \delta V_x &= -\sin I \sin T \end{aligned}$$

$$\begin{aligned} \text{Z axis } \delta N_z &= \sin I \cos A \\ \delta E_z &= \sin I \sin A \\ \delta V_z &= \cos I \end{aligned}$$

If we describe the Earth vector in terms of a north, east and vertical component we can calculate theoretical readings for each axis using the vector dot product. If the Earth's magnetic Field Vector is Mag N, Mag E, Mag V and the Earth's Gravity Field Vector is Gn, Ge and Gv we would expect each sensor to read the vector dot products as follows;

*Y axis*

$$B_y = \begin{bmatrix} \cos I \cos A \cos T - \sin A \sin T \\ \cos I \sin A \cos T + \cos A \sin T \\ -\sin I \cos T \end{bmatrix}^T \begin{bmatrix} \text{Mag}_n \\ \text{Mag}_e \\ \text{Mag}_v \end{bmatrix} \quad G_y = \begin{bmatrix} \cos I \cos A \cos T - \sin A \sin T \\ \cos I \sin A \cos T + \cos A \sin T \\ -\sin I \cos T \end{bmatrix}^T \begin{bmatrix} G_n \\ G_e \\ G_v \end{bmatrix}$$

*X axis*

$$B_x = \begin{bmatrix} \cos I \cos A \sin T + \sin A \cos T \\ \cos I \sin A \sin T - \cos A \cos T \\ -\sin I \sin T \end{bmatrix}^T \begin{bmatrix} \text{Mag}_n \\ \text{Mag}_e \\ \text{Mag}_v \end{bmatrix} \quad G_x = \begin{bmatrix} \cos I \cos A \sin T + \sin A \cos T \\ \cos I \sin A \sin T - \cos A \cos T \\ -\sin I \sin T \end{bmatrix}^T \begin{bmatrix} G_n \\ G_e \\ G_v \end{bmatrix}$$

*Z axis*

$$B_z = \begin{bmatrix} \sin I \cos A \\ \sin I \sin A \\ \cos I \end{bmatrix}^T \begin{bmatrix} \text{Mag}_n \\ \text{Mag}_e \\ \text{Mag}_v \end{bmatrix} \quad G_z = \begin{bmatrix} \sin I \cos A \\ \sin I \sin A \\ \cos I \end{bmatrix}^T \begin{bmatrix} G_n \\ G_e \\ G_v \end{bmatrix}$$

In practice we usually ignore any  $G_n$  and  $G_e$  components and assume that  $G_v$  is the Gravity  $G_t$ ;

$$G_x = -\sin I \cos T G_t$$

$$G_y = -\sin I \sin T G_t$$

$$G_z = \cos I G_t$$

*From these very much simpler formulae we can easily derive the inclination and the toolface*

$$\sin I = \sqrt{(G_x^2 + G_y^2)} / G_t$$

$$\cos I = G_z / G_t \quad I = \tan^{-1}(\sin I / \cos I) \text{ resolved } 0 - 180$$

$$\sin T = G_y / (-\sin I G_t)$$

$$\cos T = G_x / (-\sin I G_t) \quad T = \tan^{-1}(\sin T / \cos T) \text{ resolved } 0 - 360$$

Returning to our magnetic equations, the red numbers are now known;

Y axis

$$B_y = \begin{bmatrix} \cos I \cos A \cos T - \sin A \sin T \\ \cos I \sin A \cos T + \cos A \sin T \\ -\sin I \cos T \end{bmatrix}^T \begin{bmatrix} \text{Magn} \\ \text{Mage} \\ \text{Magv} \end{bmatrix}$$

X axis

$$B_x = \begin{bmatrix} \cos I \cos A \sin T + \sin A \cos T \\ \cos I \sin A \sin T - \cos A \cos T \\ -\sin I \sin T \end{bmatrix}^T \begin{bmatrix} \text{Magn} \\ \text{Mage} \\ \text{Magv} \end{bmatrix}$$

Z axis

$$B_z = \begin{bmatrix} \sin I \cos A \\ \sin I \sin A \\ \cos I \end{bmatrix}^T \begin{bmatrix} \text{Magn} \\ \text{Mage} \\ \text{Magv} \end{bmatrix}$$

Each sensor observation provides one equation;

$$(Magn \cos l \cos T + Mage \sin T) \cos A + (Mage \cos l \cos T - Magn \sin T) \sin A = (By + Magv \sin l \cos T)$$

$$(Magn \cos l \sin T - Mage \cos T) \cos A + (Mage \cos l \sin T + Magn \cos T) \sin A = (Bx + Magv \sin l \sin T)$$

$$(Magn \sin l) \cos A + (Mage \sin l) \sin A = (Bz - Magv \cos l)$$

We can now reduce the bracketed terms to a simple matrix form:

$$\begin{bmatrix} m11 & m12 \\ m21 & m22 \\ m31 & m32 \end{bmatrix} \begin{bmatrix} \sin A \\ \cos A \end{bmatrix} = \begin{bmatrix} B1 \\ B2 \\ B3 \end{bmatrix}$$

These are now a set of oversubscribed simultaneous equations in  $\sin A$  and  $\cos A$  which can be solved by least squares as follows:

$$\begin{bmatrix} m11 & m12 \\ m21 & m22 \\ m31 & m32 \end{bmatrix}^T \begin{bmatrix} m11 & m12 \\ m21 & m22 \\ m31 & m32 \end{bmatrix} \begin{bmatrix} \sin A \\ \cos A \end{bmatrix} = \begin{bmatrix} m11 & m12 \\ m21 & m22 \\ m31 & m32 \end{bmatrix}^T \begin{bmatrix} B1 \\ B2 \\ B3 \end{bmatrix}$$

These equations can be used to solve for  $\sin A$  and  $\cos A$  and thus an unambiguous best fit azimuth can be derived from the observations. The unit vectors can be calculated and the theoretical readings subtracted from the observed readings to produce residuals for each observation and each axis.

A 'Monte Carlo' analysis is then run for variations in scale factor and bias for each sensor until the sum of the residuals squared is minimized. In the following graphs for all 6 corrections, a clear minimum sum squared occurs at the best value for each correction:

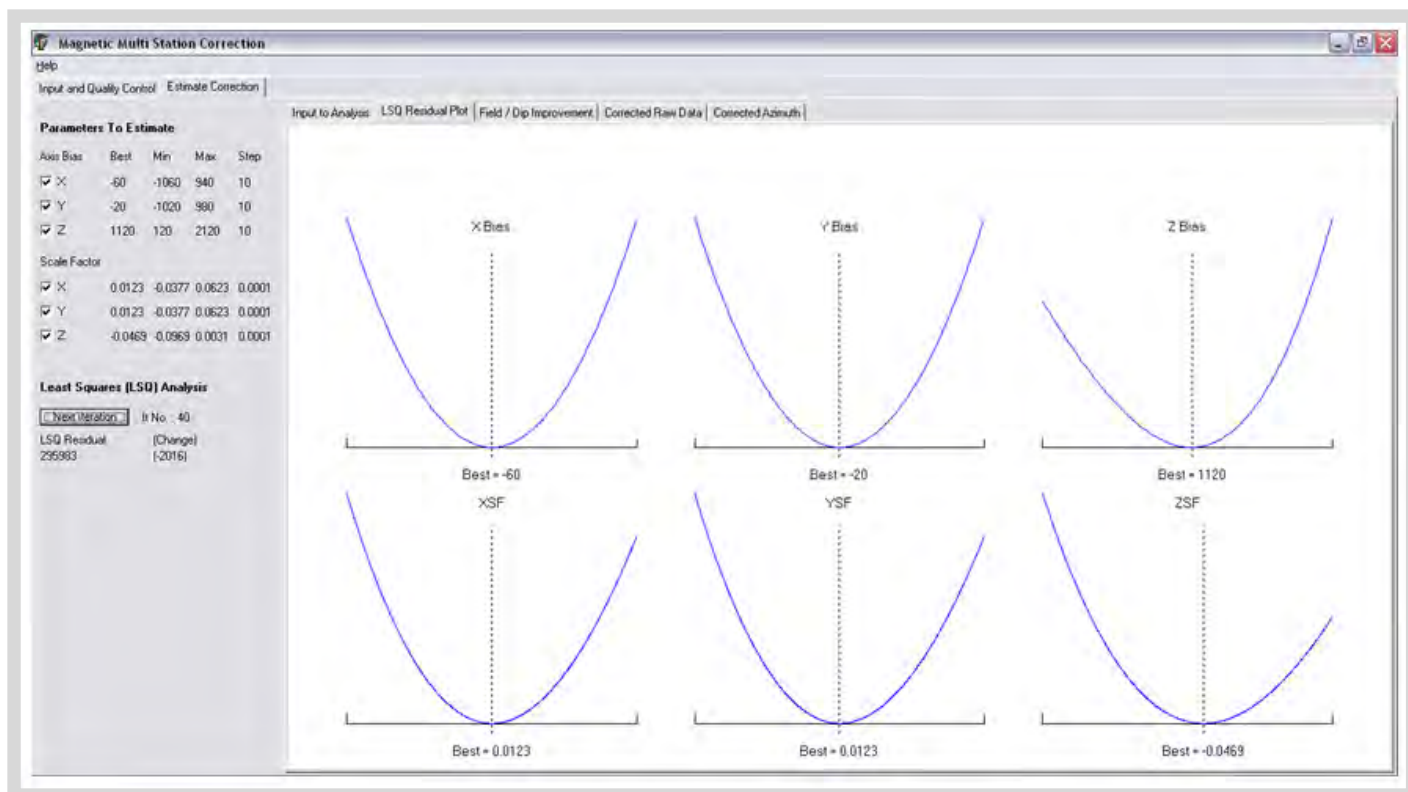


Figure 64: Correcting magnetic station observations

All previous raw surveys up to that point are then corrected with this latest estimate and the azimuths recalculated as if there was no magnetic interference present.

In practice the data will be noisy and often requires some filtering before it can be used. Any bad readings are either weighted low in the least squares calculation or they are removed altogether.



## 15. Correcting for Pipe and Wireline Stretch

### 15.1 Forces on the Drillpipe

It has not been routinely included in survey procedures to estimate and remove the mechanical or thermal expansion of the drillpipe and yet clearly the weight of the BHA itself and the drillpipe suspended below any section of pipe will stretch it, as will any increase in downhole temperature from that observed at surface where the drillpipe length is measured before deployment.

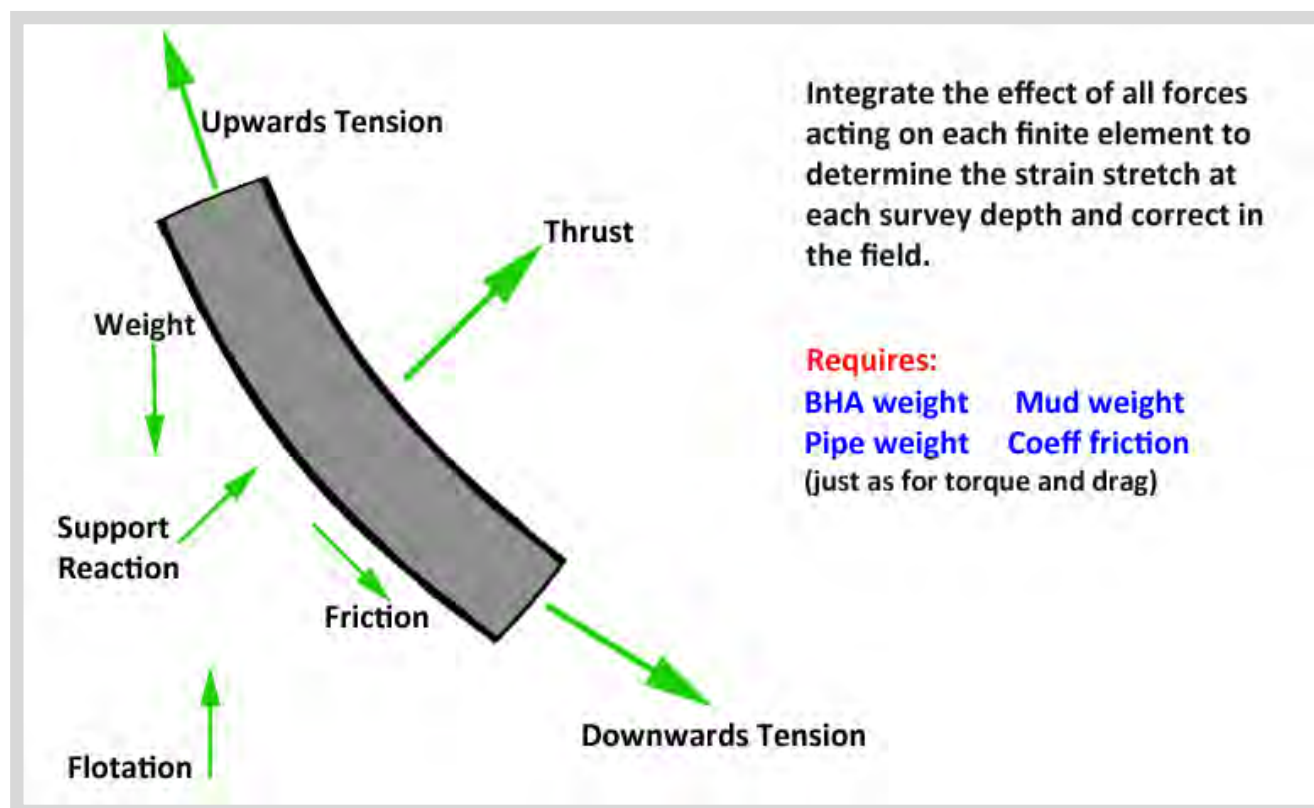


Figure 65: Forces acting on a finite element of drillpipe

This diagram represents a finite element of drillpipe with all the forces likely to be acting on the element. There is an upward tension on the pipe as it is supported by the pipe above and a downward tension as it carries the drillstring below. These tensions will not be in alignment in curved hole producing a 'Thrust' force perpendicular to the wellbore, usually upwards in a build section and downwards in a drop section. There is also the weight of the pipe, countered to some degree by the flotation effect of the drilling fluid, a support reaction and corresponding friction force. If we estimate the coefficients of friction and assume that the survey models the shape of the pipe, we can estimate the mechanical stretch by integrating the axial components of the forces on the pipe and their local strain effects on each element.

$E = \text{Youngs Modulus} = \text{stress} / \text{strain}$  so  $\text{the strain} = \text{stress} / \text{Youngs Modulus}$

This calculation is most useful for high accuracy, absolute TVD measurement. It may seem sensitive to our estimate of the coefficient of friction but in practice this proves to be less than you might anticipate. This is because when the stress most affects TVD, the well is close to vertical and the friction component is small but when friction becomes very significant (i.e. at high angle), the stretch effect in measured depth does not translate to much of an error in TVD.



## 15.2 Thermal Effects

The thermal coefficient of expansion for steel is approximately 1.3 m / 1000 for every 100° C of warming so it is also possible to estimate from an approximate temperature profile, how much additional depth we will gain from thermal expansion. In the following example of a fairly typical well, there is 2 m of mechanical extension plus 5 m of thermal expansion giving a total of 7 m of additional drillpipe you never knew you had!

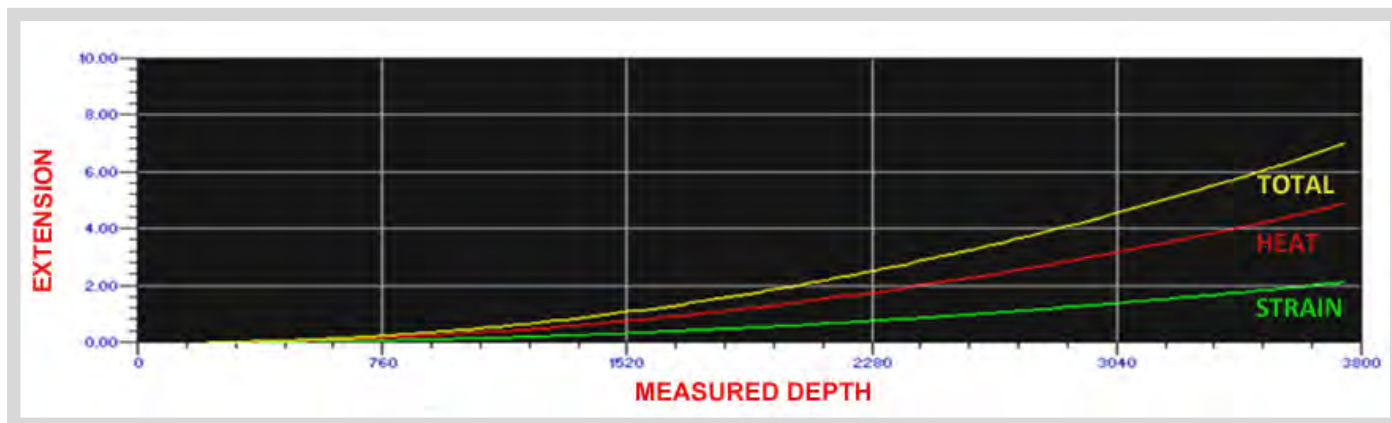


Figure 66: Measuring thermal expansion of a typical drillpipe

This is one of the reasons that wireline measurements and drillpipe conveyed measurements seldom agree. The wireline will stretch much more than steel and when warmed up, oddly, becomes shorter rather than longer due to the lateral expansion of the elastomer within the reinforced sheathing. As a result, wireline is usually corrected for stretch whereas drillpipe almost never is (at the time of writing).

Great care should be taken when using drillpipe depths as they will usually be significantly less than actual depth. One common mistaken assumption is that if we fail to correct for drillpipe stretch in a vertical pilot well, we'll be able to land a horizontal target at the same depth if also ignore the stretch in that. However, in a vertical well the BHA is supported by the pipe whereas the horizontal wellbore will support the BHA on the low side producing a very different stretch profile.

For a more detailed explanation of the issues affecting depth measurement read the following chapter by Harald Bolt, a recognised global expert on the subject.



## 15a Along Hole Depth Measurements

### 15a.1 Discussion: Why Bother

Depth is the most important sub-surface parameter measured. Depth defines the along hole position of all the sub-surface parameters measured, and hence defines the well construction activity, the geologies drilled and the horizons produced. Without accurate, consistent and credible depth measurement the entire database related to subsurface is compromised and the uncertainty associated with any subsurface measurement cannot be reasonably ascertained.

Along hole depth is the key component of TVD, which is the main descriptor in well bore positioning and reservoir geometrical descriptions.

However, there is a great deal of discussion and lack of clarity on how depth is measured. There is a correspondingly significant spread of measurement results that bring into doubt the validity of depth as a measured parameter. The scale of the depth measurement discrepancy has been described by Forsyth et.al.<sup>1</sup> Even operators do not have a common platform for expectations in depth accuracy or requirements for the associated uncertainty.

#### Definitions of terms

The word “depth” is described as commonly understood to refer to the distance from an acknowledged reference point, usually assumed to be at surface (typ. MSL, GL, ORT, etc.), along a described path (e.g. along hole Measured Depth, MD, or True Vertical Depth TVD, from surface) using described units (ft or m). The use of these three descriptors is critical in understanding what “depth” is being referred to.

MD is the basis for TVD. TVD is not usually measured directly and relies on deviation surveys, defining azimuth and inclination along hole to derive the actual vertical depth of any point.

MD is described by any of several quite different types of measurement. These include “Indicated Depth”, “Raw Depth”, “Calibrated Depth” and “Corrected Depth”. Ultimately, the actual along hole depth is referred to as “True Along Hole Depth”, and is provided then with an uncertainty estimate. (See WDDrev4.0 p. 15<sup>2</sup> or Forsyth et.al. for a full definition of commonly referred to depth terms).

#### Defining accuracy expectations

Accuracy expectations vary according to the application of the data. Seismic depth accuracy is limited by the resolution of seismic signals that is defined by the frequency of the acoustic signal. This is typically 10’s of meters at 1,000 M, so can be assumed to be around 5:1,000 at best. For most well construction, accuracies in the order of 1:1,000 are typically sufficient. Most wireline companies quote 5:10,000 to 2:10,000, but few actually achieve this. Forsyth et.al. demonstrated that there is very little evidence to suggest that these accuracies are routinely achieved. For compaction studies where movements of formation boundaries and markers are measured, accuracies of at least 1:10,000 are required.

Table 1, overleaf, illustrates a number of different applications where the accuracy requirements can be seen to be different. As increasing accuracy requires increasing calibration, verification and correction requirements, it is clear that increasing accuracy can only be attained at increased operating cost.

<sup>1</sup> D. Forsyth, H. Bolt and A. Loermans, 2013, Improved Depth Quality Management: Where Old Theory Should Meet (Near) Future Practice, presented at SPWLA New Orleans Conference, New Orleans, 2013

<sup>2</sup> H. Bolt, Wireline Depth Determination Rev 4.0, ICT Europe, 2015, (available via) [www.wirelinedepth.com](http://www.wirelinedepth.com) (WDDrev4.0)

**Table 1: Along hole depth accuracy target “bands” – a proposal (adapted from Bolt et.al. )**

Measurement relevance	Domain relevance	Method	Measurement System	@ 10,000 ft Trueness +/-	@ 10,000 ft Precision +/-
Geological mapping	Major geological events	Seismic	2-way time, depth conversion	100 ft	20 ft
Well construction	Significant reservoir events	Drillers' depth	Indicated depth	50 ft	6 ft
Mechanical service operations	Minor reservoir events	Wireline	Indicated depth	30 ft	5 ft
Reservoir geometry	Major bed events		Calibrated depth	15 ft	3 ft
OWC/GWC mapping	Minor bed events		Calibrated depth	5 ft	1 ft
Detailed OWC/GWC mapping	Minor bed events		Way-point depth	2 ft	0.5 ft
Fracture identification/place ment			Way-point w/ real-time stretch correction	0.5 ft	0.1 ft
Pressure gauge accuracy/resolution	Compaction events				

### Driller's Depth and Wireline Depth

Driller's Depth, attained from the measurement of drill pipe in the well bore, is typically uncorrected, and can at best be described as being “indicated Depth”. The reason for this is that there is not a credible calibration of measurement verification process associated with drill pipe measurement, and typically corrections are not routinely or consistently applied across the industry. The movement of the drill pipe is also irregular, with depth measurements being made under differing pipe loads and pipe stress conditions (torque, pressure support, temperature, rotational and sliding friction, etc.).

Wireline cable can be calibrated in length, and the length measurement made can be verified. The measurement made can be subject to systematic environmental corrections that accounts for temperature, stretch and other influences. The measurement is made only during pull out of hole (POOH) when ascending to surface with an increasing tension regime distributed along the cable from the tool string to surface<sup>3</sup>. This means that the cable tensional regime can be modelled, and hence corrected. The ability of wireline depth to provide a calibrated, verified and corrected measurement is a major differentiator to Drillers' Depth.

### Drillers' Depth and wireline first primary

Driller's Depth is made continuously during the drilling process, and the core and MWD/LWD data is accumulated and presented according to the first measured depth principle. As has been pointed out above, Drillers' Depth measurement usually lacks calibration and verification, and is not corrected. Also, as the drilling process is dynamic, significant changes in indicated depth occur during the drilling process as WOB is increased and decreased, as stand-pipe pressures are varied, and mud flows and mud weights vary as the pipe is rotated and slid along the hole. There are a multitude of other factors, such as BHA assembly and drill pipe string composition that also affect the actual bit and LWD/MWD sensor positions.

<sup>3</sup> Some depth data providers provide depth defined while running in hole (RIH), so called “log-down” depth. The stretch correction is then applied at hold up depth (HUD) and then it is assumed to be linearly distributed over the length of the well. Solie & Rodgers and Fitzgerald & Pedersen describe this process. See also Lubotzki .... <http://fesaus.org/webcast/2010/05/HLubotzki/Member0922/index.htm>. However, there are a number of issues that limit the validity of this approach. See WDDrev4.0 Section 28, pp. 78-79 and Sections 40 & 41, p. 96 – 100. This approach is not recommended for definitive TAH determination, and specifically not in wells with deviation or significant borehole wall friction.

Wireline Depths are usually measured more consistently, but current practices are varied between logging companies – see Table 2. These variances include whether or not calibrated cable length is made available and what (if any) verification processes are deployed. There are also fundamental differences in the application of correction, with few companies having a comprehensive, credible and published correction determination and application process.

By convention, the wireline “First Primary” is when the along-hole depth is defined by wireline for the first time. It is self-evident that this measurement should be scrutinized for the applied calibration, the measurement results verification and judicial application of the corrections. By convention, all subsequent wireline depths are synchronized to the First Primary to assure that the depths of wireline logs results correspond. For this reason, it is critical that the processes used to define First Primary log depths are closely scrutinized. This includes detailed QC of the utilized measurement methodologies (including calibration, verification and correction). It is also important that the First Primary log is accompanied with an uncertainty statement that then defines the accuracy of the depth measurement provided.

### Review of practices

Different companies log depth in different ways, and they result in different measurements. Table 2 gives a summary of 4-different wireline companies surveyed in the same location and illustrates that very different methodologies are used in depth measurement as well as totally different correction mechanisms.

**Table 2: Depth determination methodologies deployed by a number of logging companies. This highlights different ways of making depth measurements, but with differing outcome**

Company	Method description
○	Dual-wheel measurehead with fastest wheel algorithm to provide cable length. Tool zero defined at surface with return-to-zero used as depth measurement verification. Correction determined at/near HUD by observing log-down/-up depth differences. No other correction or adjustment applied in the return to surface.
■	Tool zero determined at surface, but depth synchronized to any downhole defined depth datum. Magnetic mark determined calibrated cable length. Although equipped with a dual wheel measurehead, only a single wheel is used to define logging depth. 2 <sup>nd</sup> wheel used to detect slippage. 3 <sup>rd</sup> party algorithm used to define elastic stretch. HUD correction applied with along-hole adjustment as needed to magnetic mark depth to adjust for 3 <sup>rd</sup> party defined stretch.
□	Magnetic marks used in combination with 3 <sup>rd</sup> party software to define cable length. Dual-wheel measurehead with fastest wheel algorithm used to define depth when magnetic marks were compromised. Stretch chart used to provide HUD correction despite more advanced 3 <sup>rd</sup> party correction software being available. No correction or depth adjustment is made other than that at HUD.
❖	Calibrated depth provided ostensibly by magnetic marks, but in practice depth is derived from 3 <sup>rd</sup> party dual-wheel measurehead with fastest wheel algorithm. Depth synchronized to defined depth when possible. Stretch charts used to determine HUD correction. Unclear methodology for correction tracking.

## 15a.2 Calibration – Principles and Practice

Calibration is the determination of the instrument response relationship to the calibration standards applicable to the measurement

In the case of drill pipe, there is no real calibration other than the measurement of the pipe length, usually determined on the pipe racks. This is often done by hand using a steel tape measure, but is also done using laser, measuring from shoulder-joint to shoulder-joint along the pipe length.



Figure 67: Drill pipe strapping in defining drill pipe length



Figure 68: Drill pipe length measurement using laser (image courtesy of Digi-Tally)

The pipe tally is then used to define the pipe length in the hole, with interpolation of pipe length providing the continuous length measurement. When pipe length is environmentally corrected, various factors may be taken into account, and these should be detailed in the correction information. But invariably, these corrections are not applied, and scant attention is paid to them.

Some wireline companies rely on calibrated measureheads to provide line length, but unfortunately the measurement provided is then not corrected for existing line stretch, and the error can be significant. Other companies use calibrated line length defined by magnetic marks with gives a far more robust line length measurement that can be verified through observation of the actual magnetic mark tally.

Figure 69, overleaf, illustrates the role of magnetic marks used when pulling out of hole. It can be seen that under varying tension conditions the magnetic marks define the length of cable between the surface and the tool string, and that this can then be corrected for stretch according to the surface and downhole cable head tension.

It is important to note that without a credible calibration process the application of corrections is questionable.



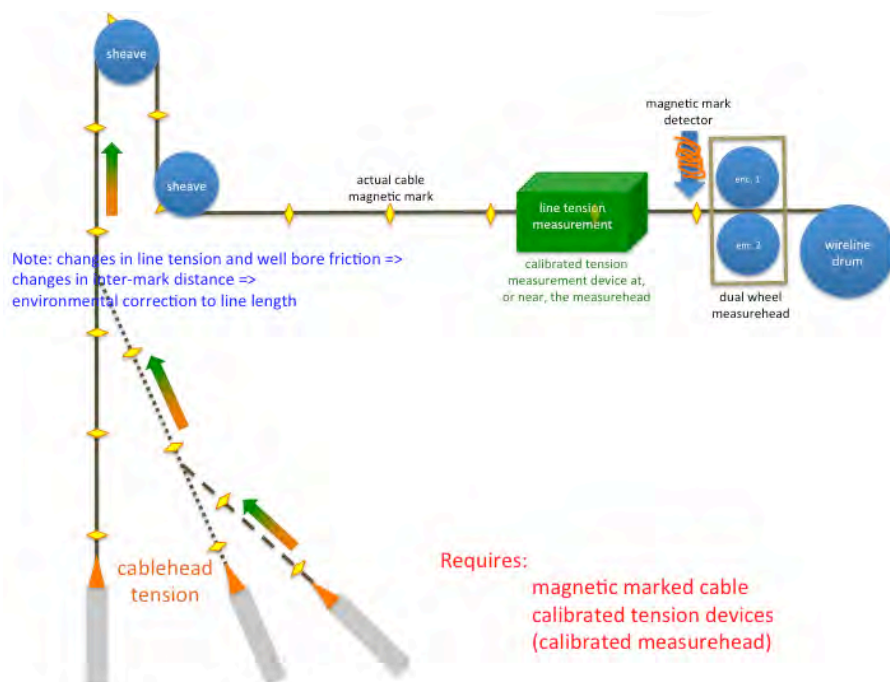


Figure 69: Role of magnetic marks in calibrated cable length measurement (from WDDrev4.0)

### Verification

Measurement verification of depth can be provided for Drillers' Depth by logging the out-coming pipe depth, and for wireline logging the magnetic mark positions. Note that when logging wireline using a measurehead only (i.e. without marks) there is no realistic measurement verification.

The objective of the verification process is to quantify the compliance of the measurement to the calibration process. This is shown by the conformance of the measurement to a known standard as well as stability of the measurements provided.

In the case of depth, this is difficult as a number of issues are not well defined. This includes the robustness and relevance of the calibration standards as applied to the depth measurement, the influence of environmental and measurement conditions on the measurements made, and the availability of a credible verification process and standard.

For drill pipe, the measurement made is based on the measured length of the drill pipe. Usually the temperature of the measurement process is not recorded, so that the relevance of temperature correction is at doubt. Also, the calibration process itself, including both systematic and well as random error induced by the rack-based pipe length measurement, is often not well defined.

### Role of corrections

Corrections are designed to adjust the measurements made back to calibration conditions so that the accuracy of the calibration can be adhered to. The correction process should take into account all effects that materially affect the validity of the measurement compared to the calibration conditions.

The most common corrections on drill pipe include hydraulic pressure ballooning, thermal expansion, torque and in-hole buckling, tension and compression of the pipe along the well bore, rotational and sliding pipe frictional forces, weight support due to contact with the borehole wall, mud-weight buoyancy, mud movement frictional effects, pressure support at the bit.

Wireline corrections for first primary open hole logging are typically limited to thermal expansion and elastic stretch. Corrections for cased hole services are usually related to compensation to line tension related to pressure. Typically this involves pressure support through wellhead control (GIT and stuffing box effects on surface tension) and measurement inaccuracies through sheave angle when using lower sheave wheel tension.

Stick&Pull affects wireline measurements, and can affect both first primary as well as cased hole. It can be either corrected real-time or post operationally.



## 15a.3 Pipe Properties Versus Cable Properties

Drill pipe and wireline have fundamental differences, and are subject to totally different measurement influences. It is clear from Fig. 70 that the measurement systems used and the applicable corrections are different and will lead to different results unless there is meticulous application of calibration methodologies and corrections. It is also clear from the diagram that the correction coefficients between various sizes of pipe, tubing, coiled tubing, e-line, braided line and slickline will vary considerably. Hence the medium used to create the measurement must be understood and characterized before a Raw Depth can be developed through to a True Along Hole Depth.

A major different in how Driller's Depth and wireline depth are defined is inherent in the role that the measurement process plays. Drill's Depth (and hence LWD/MWD depths) is defined while drilling, going down the hole, with the drill pipe in a combination of tension and compression, typically rotating and sliding. Wireline depth is defined while measuring the hole, going up with increasing tension along the line. Drill pipe MWD measurements are made in-situ, while drilling.

During the drilling process the drill pipe is subject to various changes in associated stresses, such as changes to WOB, sliding and rotating, pressure fluctuations in the pipe, changes in mud density inside and outside of the pipe, torque of the drill pipe, temperature variances due to mud versus formation temperature, etc. This means that when Drillers' Depth (and hence LWD/MWD depth) is defined the associated corrections are highly complex and variable, and most importantly, not repeatable. This is a major difference with wireline where the tension regime is repeatable as are the depth determination conditions.

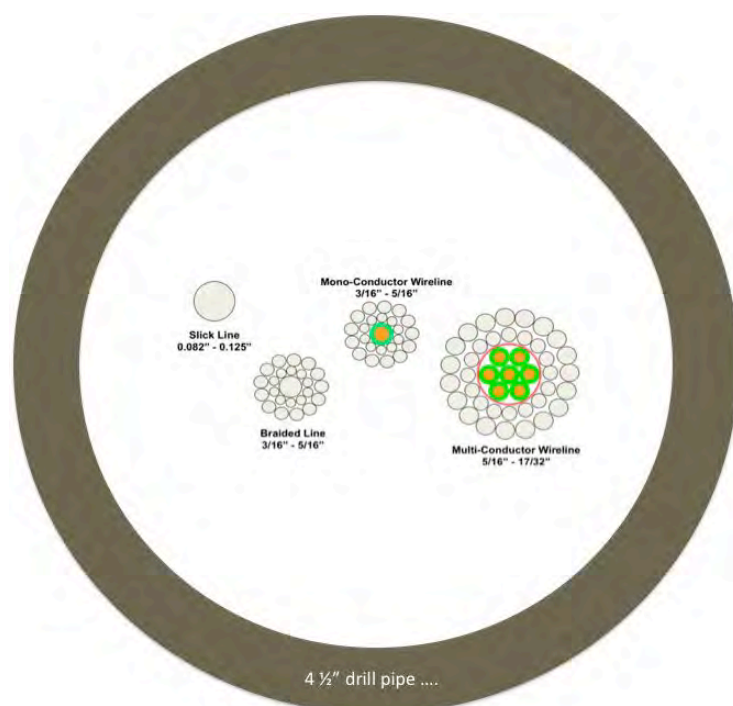


Figure 70: Comparison of depth measurement mediums (not to scale)

### Thermal expansion

Thermal expansion affects the measured depth by adding depth to the measured value with increasing temperature. Knowledge of the thermal expansion coefficients is required to provide a credible thermal

expansion correction.

What is important to realize is that the temperature is a gradient along the well, and the thermal expansion should be calculated as of the calibration temperature of the pipe or wireline. For this reason, the calibration temperature should be recorded as part of the pipe length or cable length calibration record.

The relationship for the thermal expansion correction is:

$$Th. Exp. Corr = Th. Exp. Coeff \times Length \times \left( \left( \frac{T_{HUD} + T_{Surf}}{2} \right) - T_{Calb} \right)$$

where  $Th. Exp. Corr$  = thermal expansion

$Th. Exp. Coeff$  = thermal expansion coefficient

$Length$  = calibrated along hole length (either drill pipe or wireline)

$T_{HUD}$  = temperature at HUD

$T_{Surf}$  = surface temperature

$T_{Calb}$  = temperature at which the Calibrated depth is defined (typ =  $T_{Surf}$ )

Thermal correction for drill pipe is a constant based on material properties of drill pipe steel. This is usually taken as being ~8.6 E-6 ft/ft/degF. Table 3, overleaf, gives a series of thermal expansion coefficients for steel used in drill pipe.

Table 3: Example (units/deg F) thermal expansion coefficients

Material	Mean Expansion Coefficient - $\alpha$ - ( $10^{-6}$ in/in $^{\circ}F$ )							
	Temperature Range ( $^{\circ}F$ )							
	- 32	32 - 212	32 - 400	32 - 600	32 - 750	32 - 900	32 - 1100	32 - 1300
Alloy Steel (1% Cr. 1/2% Mo)	7.7	8.0	8.4	8.8	9.2	9.6	9.8	
Mild Steel (0.1 - 0.2% C)	7.1	7.8	8.3	8.7	9.0	9.5	9.7	
Stainless Steel (18% Cr. 8% Ni)	10.8	11.1	11.5	11.8	12.1	12.4	12.6	12.8

Being simply solid steel, slick line has a similar thermal expansion coefficient to drill pipe. This means that drill pipe and slick line undergo the same expansion in the same well.

Table 4: Example (units/deg F) thermal expansion coefficients for slickline (table courtesy of Sandvik)

### Sandvik CS-9A for wirelines (Wire)

#### Thermal expansion

20 - 100  $^{\circ}C$        $11 \cdot 10^{-6} / ^{\circ}C$

68 - 210  $^{\circ}F$        $8 \cdot 10^{-6} / ^{\circ}F$

E-line (typ. larger 7-conductor) have different thermal expansion coefficients to that of drill pipe and steel because of the internal architecture and materials used in the core. Generally, as the wireline diameter increases the thermal coefficient decreases and is even negative, as the line length is effectively shortened with increasing

temperature. But the thermal expansion coefficient is very dependent on the exact line being used, and care has to be taken in assuming any one coefficient as being valid for a different type of line of the same size. What is also important is that electric wireline can have different thermal expansion coefficients at different temperatures, further complicating the exact correction applicable. Table 5, below, gives a table of typical expansion coefficients for different sizes of wireline.

**Table 5: Example (units/deg F) thermal expansion coefficients**

Line type	Th.Exp.Coeff units	
(CS-9A, all sizes) slickline	8 E-6	ft/ft
(undefined) monocable	6 E-6	ft/ft
(7H42RP) heptacable	5 E-4	ft/kft/klbs
(undefined) heptacable	5 E-4	ft/kft/klbs
(7-46P) heptacable	-3 E-6	ft/ft
(undefined) heptacable	-6.7 E-6	m/m
(7-46ZV) heptacable	-8.36 E-6	ft/ft
(new type 0.5") heptacable	-9.921 E-6	ft/ft

When determining the correction, it is important to be sure that the coefficient units correspond to the units being corrected for.

### Surface versus down-hole tension

Tension measured at surface is often seen as a representation of the tension along the hole to TD. However, this is really only the case is a straight vertical well with negligible frictional influences. In this case, only, the tension at surface can be envisaged as being distributed evenly along the length of medium in the well to the BHA or tool string. In this case, changes in tension are representative of changes in the effective length of the pipe or line in the well and changes in the BHA or tool string friction.

In a real borehole, these changes in tension can be due to a multitude of other effects, including friction along the well bore, differential sticking, key seating, sloughing of formation, pipe or line weight supported by the borehole wall, hydraulic pressure changes, etc. In other words, the tension at surface is a complex composite of numerous factors.

However, specifically in the case of wireline, surface tension during POOH is repeatable at given speeds, and across specific well bore increments is also repeatable. This means that a logging tension measured at e.g. 1,000 m will repeat with the same value at the same speed.

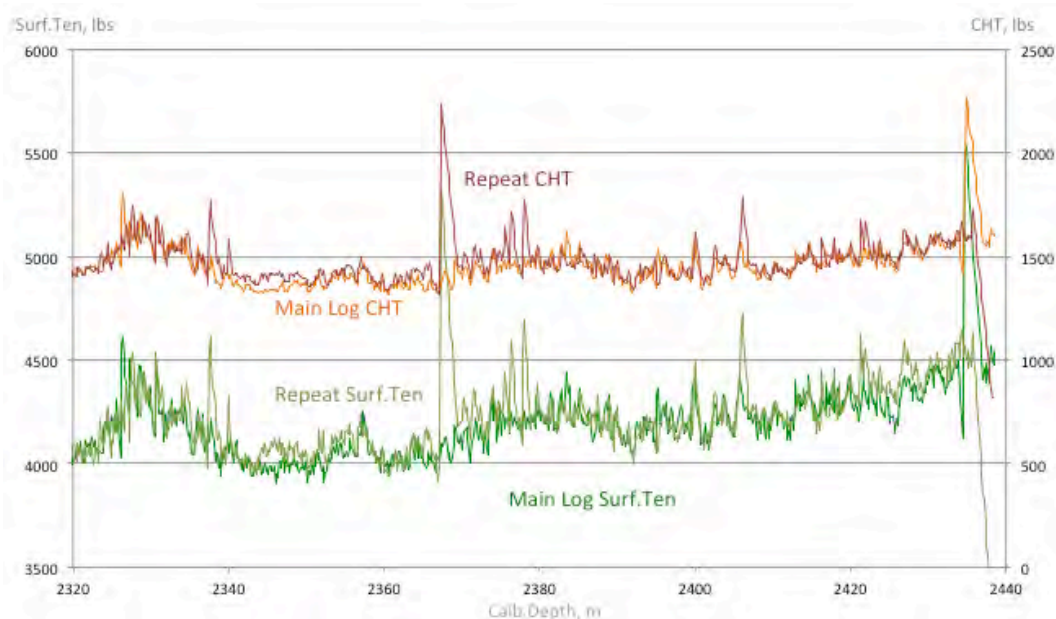


Figure 71: Example of wireline logged tension repeatability

When measuring from surface, during POOH the tension in the wireline can be seen as incrementally decreasing between any two points such that any change in the tension can be corrected for according to the elastic correction coefficients valid between these points. This means that not only the tension but also the elastic stretch for a wireline is repeatable. This also means that corrections can be incrementally introduced between individual measurement points when using wireline.

For drill pipe this is not true, as the WOB and drilling parameters (mud pressure, density, flow rates, sliding/rotating, torque, etc.) change during the drilling process, such that the effective position of the BHA is not the same during the drilling and subsequent ascents and then descents in the hole. As the LWD and MWD measurements are defined using drillers' depths, it is clear that there is significant opportunity for inconsistency between the measurements made during first drilled descent and subsequent ascents and descents. For this reason it is also obvious that first drilled depths cannot be expected to correspond to wireline depths.

### Tension and stretch regimes

A tension regime is a description of the changes in tension with depth that the wireline undergoes during descent and then the ascent. Under normal conditions, the tension regime during pull out of hole (POOH) at logging speeds is repeatable, creating the ability to determine incremental corrections between points that are repeatable and hence predictable.

A stretch regime is the elastic stretch associated with a given tension regime. As the tension regime is repeatable and the parameters for elastic stretch are known, the stretch regime is then also repeatable and predictable between points.

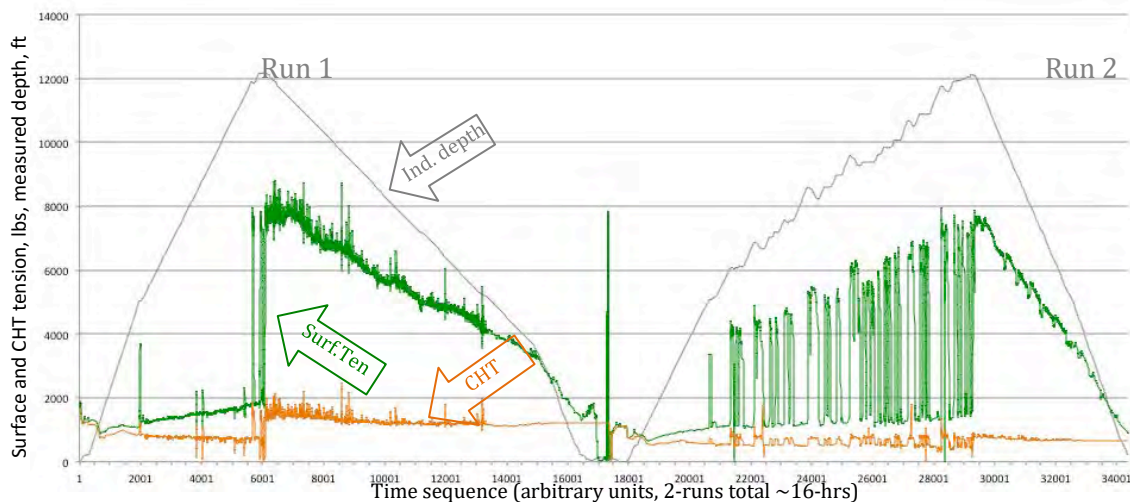


Figure 72: Tension regime differences between two sequential logging runs (Y-axis = logged surface tension, CHT (lbs) and depth (ft), X-axis = data sequence number)

In the case of drilling, the tensions measured are not repeatable as, by definition, the hole is being drilled. This means the measurements made cannot be repeated, for verification purposes. Obviously, any subsequent descent and ascent of the drill pipe over a drilled interval will have a totally different tension characteristic.

### Elastic stretch equation

Hooke's Law describes the elastic deformation of both pipe and wireline. From this an environmental correction for stretch (or compression in the case of drill pipe) can be made based on the elastic stretch equation insofar that the deformation is elastic and linear in character. In the case of well bores, the tension decreases going downhole because of there is increasing less line or pipe weight at any point through to the end of the line or pipe where the tool sting or BHA is.

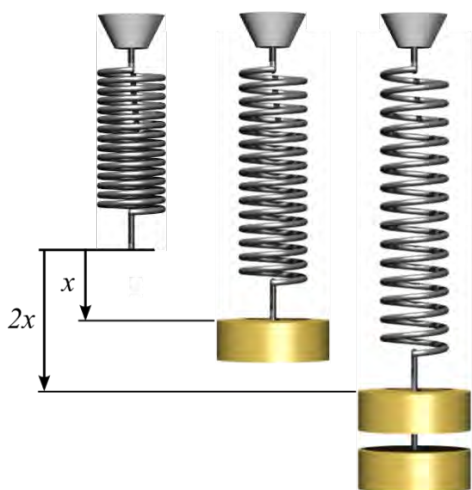


Figure 73: Hooke's Law Principle (from en.wikipedia.org)

The equation used to determine drill pipe stretch is based on the calculated stretch constant based on the pipe dimensions. Elastic stretch is then given<sup>4</sup> as:

$$\Delta L = F \times L \times S.C.$$

where  $\Delta L = \text{stretch in inches}$

$F = \text{pull force, in thousands of pounds}$

$L = \text{length, in thousands of feet}$

$S.C. = \text{charted Stretch Constant, in inches of stretch per thousand pounds of pull per thousand feet of length}$

The equation used to provide wireline stretch correction in a borehole environment includes both surface and cablehead tension. This is then:

$$\text{Wireline.Stretch} = \left( \left( \left( \frac{\text{Surf.Ten} + (\text{CHT})}{2} \right) - \text{Ten}_{\text{calb}} \right) \times \text{Length} \times \text{St.Coeff} \right)$$

where  $\text{Wireline.Stretch} = \text{elastic line stretch}$

$\text{St.Coeff} = \text{elastic stretch coefficient*}$

$\text{Length} = \text{calibrated along hole length}$

$\text{Surf.Ten} = \text{line tension measured at surface}$

$\text{CHT or BHA} = \text{tension measured at the cable head or BHA}$

$\text{Ten}_{\text{calb}} = \text{Calib.Length defined tension}$

It is important to note the role of Calb.Ten, and when the length calibration is made this should be included (even if this is “zero”, such as is the case when strapping pipe on the pipe rack).

### Stretch coefficient

The stretch coefficient is a major parameter in the stretch correction, and must be accurately known.

The stretch coefficient for drill pipe is based on the cross sectional area of the pipe and the material properties of the pipe. The general equation for stretch constant (S.C.) is:

$$S.C. = \frac{0.4}{a_s}$$

where  $a_s = \text{pipe wall cross-sectional area in square inches}$

Common drill pipe sizes are tabulated below. Note that it is stated (by BakerHughes): “It is a common misconception that the rate of stretch for oil field tubular material is also affected by the grade of steel (J-55, N-80, etc.). This is not true. Higher grades of steel have greater elastic limits and can therefore be stretch further before reaching their elastic limits than can lower grades, but the rate of stretch is the same for all grades....”

<sup>4</sup> TechFact Engineering handbook, Baker Hughes Incorporated, 2011

<http://assets.cmp.bh.mxcloud.com/system/v1/f631836b7905345b0ce8c49e3c45f2c6/Tech-Facts-Book-2011-Rev-A.pdf>



Table 6: Example elastic stretch coefficients for various drill pipe sizes

OD	Nominal Weight	ID	Wall Area	Stretch Constant
in.	lb/ft	in.	in <sup>2</sup>	in./1,000 lb/1,000 ft
2-3/8	4.85	1.995	1.304	0.30675
	6.65	1.815	1.843	0.21704
2-7/8	6.85	2.441	1.812	0.22075
	10.40	2.151	2.858	0.13996
3-1/2	9.50	2.992	2.590	0.15444
	13.30	2.764	3.621	0.11047
	15.50	2.602	4.304	0.09294
4	11.85	3.476	3.077	0.13000
	14.00	3.340	3.805	0.10512
4-1/2	13.75	3.958	3.600	0.11111
	16.60	3.826	4.407	0.09076
	18.10	3.754	4.836	0.08271
	20.00	3.640	5.498	0.07275
5	16.25	4.408	4.374	0.09145
	19.50	4.276	5.275	0.07583
5-1/2	21.90	4.778	5.828	0.06863
	24.70	4.670	6.630	0.06033
6-5/8	25.20	5.965	6.526	0.06129

This is also true for slickline.

For braided and e-line this is not so, as the elastic stretch coefficient of the line is then also affected by the lay- and internal architecture of the wireline. The stretch coefficient also increases with higher tension. OEM values for stretch coefficient are often quoted, but these values relate to specified (near maximum pull) levels and refer to new lines after initial permanent deformation has been worked out of the line.

Table 7: Example OEM stretch coefficients for various e-line cables (adapted from WireWorks)

Cable	OD-inches	3/16	7/32	1/4	9/32	5/16	3/8	7/16	15/32	0.49
St.Coeff	ft/kft/klbs	3.0	2.2	1.9	1.6	1.2	1.0	0.70	0.77	0.60

Actual stretch coefficients applicable to logging conditions are often lower than the OEM values. Stretch coefficient for wireline can be estimated from in-situ measurements made during HUD pick up and verified at stick and pull events.

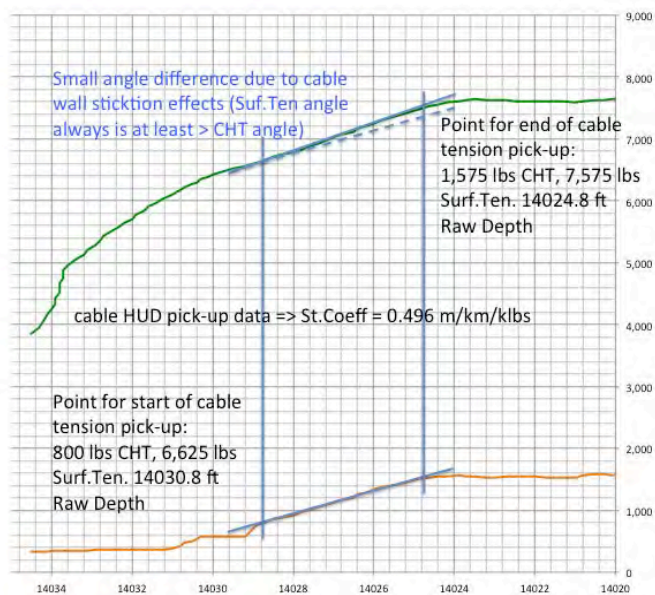


Figure 74: HUD stretch coefficient example for a 7-conductor cable

### Wireline – initial permanent deformation

E-line is subject to initial permanent deformation (IPD) when new. IPD does not affect drill pipe or slickline. This phenomenon is caused by compression of the cable core (composed of copper conductor, insulation and packing material) and intrusion of the core insulation material into the bedding of the inner armour wire layer. There is also a settling of the armour wires into a lay pattern that allows minute, but critical, abrasion of the outer and inner armour wire layers. IPD continues through till when the stabilized core and armour wire spatial configuration is achieved. The progression of IPD over any length of cable depends on the temperature, the tension that the line is subject to and the number of pull cycles and the length of time of temperature and tension exposure. As a rule, the effect of IPD has manifested itself after 6 to 10 runs in the well. Correction for IPD has the effect of increasing measured depth, and is only applicable to POOH depths.

### Drill pipe – specific corrections

Corrections for drill pipe depth measurement are varied, and complex. This comes because the pipe during drilling is at varying levels of tension, and compression, and the neutral point changes during the drilling. Further complication is the frictional losses along the drill pipe, and then torque that affects the amount of pipe in the hole. Drill pipe buckling will also affect the amount of pipe in the hole that is not reflected in the position of the bit (see Fig. 9). Ballooning of the pipe caused by mud pressure will shorten the pipe, but this varies with mud pressure and mud density. The WOB will also be affected by bit nozzle pressure.

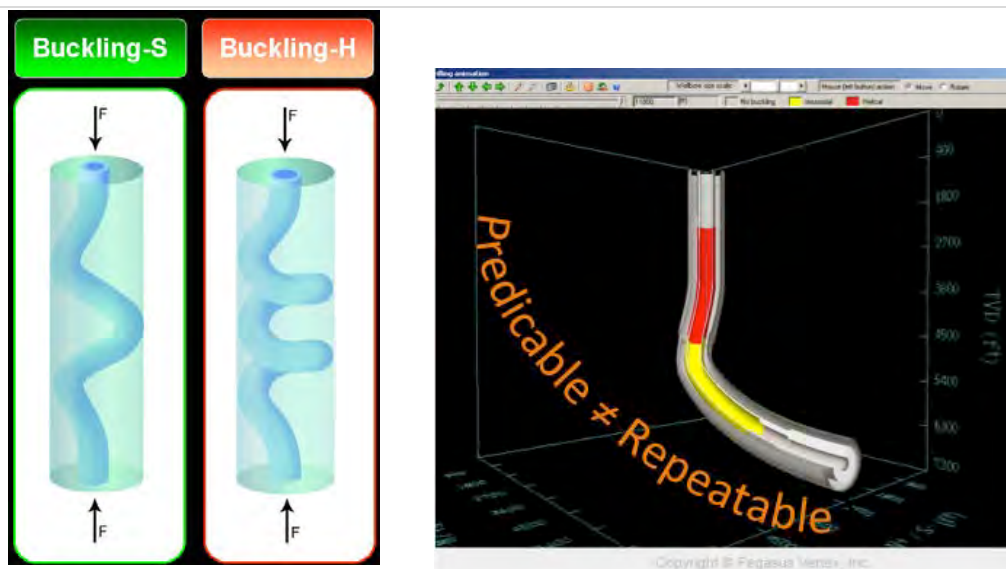


Figure 75: Sinusoidal and helical buckling of drill pipe causing measured Driller's Depth to be greater than along hole length (images courtesy of Pegasus Vertex)

### Dealing with Stick&Pull

Stick&Pull is usually a wireline depth data quality issue that manifests itself at short, but sudden, irregular build-ups of tension at surface – often caused by the tool string being momentarily stuck and the suddenly releasing<sup>5</sup>. When these build-ups correspond to build-ups of CHT, then the cause is tool sticking. When caused by the tools string sticking, the build up of the line tension has the same (or almost the same) build-up as is experienced at TD.

Stick&Pull can also be caused by differential sticking and sometimes by key seating of the wireline cable. When the Stick&Pull is caused by long-hole cable sticking, the tension build-up angle is higher than that at TD.

Stick&Pull affects not only logged depths, but also in particular the responses of array instruments that use adjacent depth responses to calculate actual values. For this reason, the logged depth data should be made available for eventual recalculation of array data. One of the problems with this is the sudden tool movement at the time of release can mean that a relatively large logging interval is passed by without the data being properly sampled through the interval.

In cased hole, Yo-Yo can occur as a function of simple harmonic oscillation of the line tension during POOH ascent of the tool string. This can usually be solved simply by changing the logging speed.

Stick&Pull does not affect the overall logged depth given that calibrated line is used. When measurehead-only depth is used, the measured depth data can be severely affected and the validity of the logged depth data is compromised.

When Surf.Ten, CHT and stretch coefficient data is available, Stick&Pull can be corrected real-time. The advantage of real-time correction is that array instruments are able to provide processing based on a corrected depth. This may require very fast processing, as much of the released depth movement occurs in a very short time. Stick&Pull can also be corrected post-operation, and be dealt with as an environmental correction. This should be done after all the other corrections have been applied<sup>6</sup>.

### Other correction factors

There are numerous other influences, usually minor, that can affect along hole depth measurement by both drill

<sup>5</sup> F. Witteman and Y. Karpekin, 2013, Effect of Irregular Tool Motion on Log Responses – a Case Study, Petrophysics, Le Log, Feb 2013

<sup>6</sup> H. Bolt, Letter to the Editor, Petrophysics, p. 12-13, Feb 2014, Vol 55(1)

pipe and wireline. These are not listed here, but most of these relate to the validity of the measurements of length, surface and downhole tension. The main corrections that affect wireline are thermal and elastic stretch correction. The main effects on drill pipe measurement are thermal and elastic stretch, and then a host of further drilling parameters as mentioned above. In any case, when corrections are made, these should be detailed in the depth data log, and should be so that they can always be reversed and re-calculated.

### Correction determination process

The main correction process includes thermal and elastic stretch correction.

The important thing is that the correction is applied over logical intervals where the most obvious changes occur. These are usually identified by the tension regime and will correspond to changes in well geometry and major changes in drilled geology.

It is recommended that, per tension regime interval, the thermal correction is made and then the elastic stretch (followed by evt. other corrections) is applied over each individual interval sequentially.

### Way-point depth navigation

Way point navigation is a wireline process sequence that allows the tension regime and hence stretch regime to be determined while running in hole, and then using this to correct for elastic stretch real-time during the ascent. The method relies on the repeatability of tension, as earlier described.

At points along the well bore while running in hole, and specifically at significant geological boundaries and know dog legs and other places where tension events are anticipated, the tool string is stopped and moved upwards at logging speed. The surface and cablehead tension values are noted.

It can be expected that these values will be repeated on the logging ascent, and yet each of the measured point values can be considered as incremental. That means that the tension and also stretch between any two points can be compared to arrive at a stretch contribution valid between these points. By adding these contributions up the total stretch applicable to the ascent can be mapped prior to pick up at HUD.

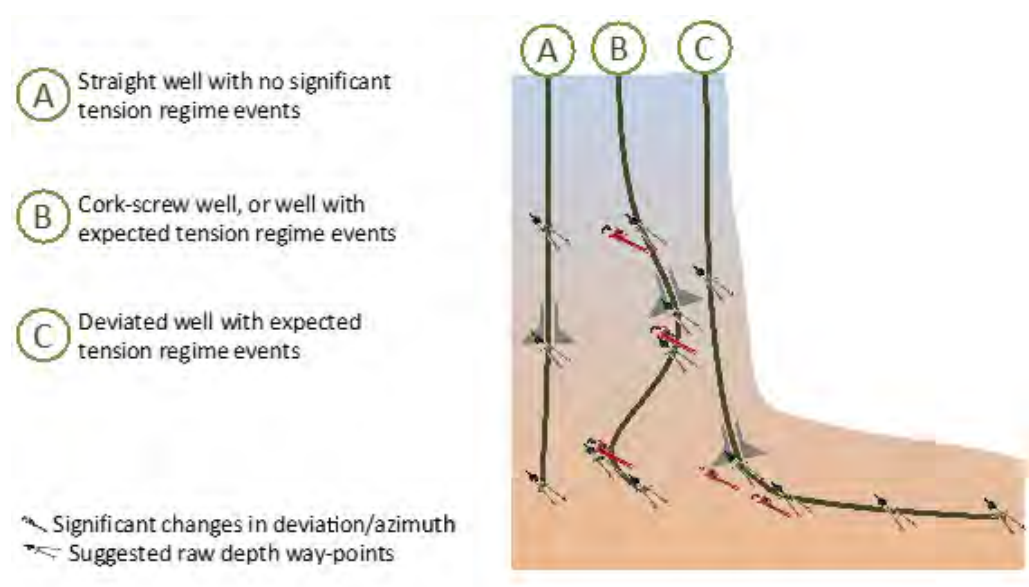


Figure 76: Example of how to apply way-points in different types of wells

The way-points are selected as points where a tension check is made of surface and cablehead tension such that an approximation can be developed of the expected tension regime.

### Measurement uncertainty determination

As has been elsewhere and earlier discussed, errors can be classified as systematic and random <sup>7</sup>.

Systematic errors in well depth measurement abound. They include errors related to well datum referencing, tool zero definition, incorrect measurement techniques or human error in procedure and reporting. They also include errors arising from operations performed outside the recommended performance envelope (over-pull, stick & pull, stuck line/tools, etc.). Problems of this nature are not dealt with in this paper even if, as individual incidents, they can have serious consequences. When unrecognized, systematic errors can be repeated and can become an ingrained error source, as there is no means of identifying them.

Driller's Depth error has been described elsewhere.

Wireline random – non-systematic – measurement uncertainty can be described as:

$$\sigma_{depth}^2 = \sigma_{line}^2 + \sigma_{corr}^2$$

where:

$\sigma_{depth}$  = depth measurement uncertainty

$\sigma_{line}$  = line length measurement uncertainty

$\sigma_{corr}$  = correction uncertainty

Calibration error is often described by logging companies as the measurement error, and a survey of various companies results in Table 8, overleaf:

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<sup>7</sup> For other examples of systematic and random errors, see V. Lindberg, Uncertainty and Error Propagation, Rochester Institute of Technology, Jul 2000  
<http://www.rit.edu/cos/uphysics/uncertainties/Uncertaintiespart1.html#systematic>

Table 8: Various depth measurement accuracy claims

Methodology	Supplier	quoted "accuracy"
single wheel measurehead	(OEM)	none available
dual wheel measurehead	(OEM)	3:10,000
dual wheel with fastest wheel algorithm	(major well logging company)	5:10,000 <sup>8</sup>
dual wheel measurehead	(OEM)	3:10,000
magnetic mark	(major well logging company)	1:10,000
magnetic mark	(OEM)	1:10,000

The error model for the correction is then defined by the exact relationship used. This can vary, but is usually a function of the measurement error of the tension devices, the temperature measurement and the stretch and thermal expansion coefficient errors. In any case, per interval it is a single figure.

When a straight-line model is assumed for correction, this then leads to the following example of error (assuming a correction model error of +/- 2.39 ft/10,000):

Table 9: Straight-line model depth uncertainty variances

10,000 ft well	$\sigma_{\text{line}}$	$\sigma_{\text{corr}}$	$\sigma_{\text{depth}}$
Raw depth - 1:1,000	10 ft	2.39 ft	10.28 ft
Calb.measurehead - 5:10,000	5 ft		5.54 ft
Mag.mark calib. - 1:10,000	1 ft		2.59 ft

When the way-point model is used, the correction error is significantly affected, as the corrections per interval are smaller, albeit more numerous. The error is defined by:

$$\sigma_{\text{HUD}}^{\text{surf}} = \sum_{\text{HUD}}^{\text{surf}} \sigma_{\text{corr}}$$

But the total correction error is diminished (in this example, it will be assumed to be 1.46ft/10,000 ft). In this case, the uncertainty is then:

Table 10: Way-point model depth uncertainty variances

10,000 ft well	$\sigma_{\text{line}}$	$\sigma_{\text{corr}}$	$\sigma_{\text{depth}}$
Raw depth - 1:1,000	10 ft	1.46 ft	10.11 ft
Calb.measurehead - 5:10,000	5 ft		5.21 ft
Mag.mark calib. - 1:10,000	1 ft		1.77 ft

<sup>8</sup> The stated performance specifications refer to "repeatability" and "reproducibility" (whereas "accuracy" is clearly implied) as being of 5:10,000. While the accuracy is not stated as such, internal (not publically available) documentation goes on to further imply a line measurement accuracy of 1:10,000.



Tables 9 and 10 illustrate that uncertainties can be determined per logged depth data set. The differences between the uncertainties shown in tables 7 and 8 indicate that significant differences, and improvements, in measurement uncertainties can be achieved through the choice of the various available measurement methodologies.

### **Sources of error before measurement**

There are a variety of potential error sources, the most important being calibration error and referencing error. Mundane – but critical: is a clear and unequivocal referencing of the surface reference points. This can be defined in a number of different ways, but it is absolutely necessary that whatever reference is used that it is applied consistently across all measurements made. When the rig moves off location, it is important that a sustainable referencing system is in place that allows the originally defined reference system to be applied.

Offshore, an important source of potential error is accounting for wave and tide error. This can be compensated for with wave compensation, but needs to be watched carefully.

Calibration error can, and does, occur. If the error is systematic, then given that the calibration parameters have been adequately noted, it may be possible to post-operationally recreate a calibrated length. If the effort is random, this is not possible.

### **Sources of operational error**

Operational error is usually down to process error and this is invariably related to engineering and operational training and management. A critical element of pre-job preparation is assurance that the right skills are in place to provide the correct process and being able to deal with variances as they occur.

Mechanical error can also occur (measurehead error or failure, tension load cell failure, etc.), but the depth data provider should have in place a back-up system to allow the error to be identified and in any case allow a safe recovery to surface.

### **Meeting accuracy expectations**

Table 1 proposes a series of accuracy requirements that can be considered as being applicable to the various tasks listed. It is not to say that this table is what it should be, but it does illustrate that different accuracy expectations are applicable to different stages of exploration, well construction, production and asset management. What is also important to recognize is that at the well site, during the depth data acquisition process, the depth data acquisition requirements may not be cognizant to the well site operations. For this reason it is of critical importance that these requirements are considered as part of the data requirements statement, and that the QA and QC functions are tuned to this.

Once the requirements are stated, it is up to the data provider to put in place the calibration, verification and correction processes that facilitate the required accuracy to be provided.

### **QA & QC check points**

QA and QC have to be designed to assure that the data to the accuracy requirements are met, and verify that the processes and procedures followed are consistent and in accordance with the stated procedures of the depth data supplier. Given that this is the case, and given that the equipment and personnel involved in the depth data acquisition are able to perform the tasks, then the consistency, and accuracy, of the depth data provided will result in a manageable error margin.



## 16. Human Error v Measurement Uncertainty

When surveyors refer to error models they are usually referring to the inaccuracies of instruments or measurement systems. Clearly these cannot compensate for bad practice and human error such as using grid North instead of True or GPS on the wrong datum. The instrument inaccuracies are often referred to as modellable errors whereas the practical mistakes are referred to as unmodellable errors. Great care has to be taken when using industry standard error models to ensure that best practice has been adopted before assuming that the calculated uncertainties are representative. The following section points out a few common mistakes.

### 16.1 Common Human Errors

#### Common Pitfalls

The following common well planning pitfalls are listed to raise awareness. Past experience has shown that these are likely errors that can be overlooked. Best policy is to review this list after producing a new well plan.

#### Missing Data

The most frequent reason for collision is not poor surveying but rather that the object well came as a “surprise”. It is essential that the well planner ensures that he has all the data needed to plan a safe well path. Always check a list of wells with the client to ensure that nothing was lost in migration.

#### Using Gyro Error Models for Undrilled Sections

It may well be that a gyro survey is planned in for example, 9 5/8 casing. But prior to this gyro survey “confirming or more accurately describing” the well path of the well, this section will usually be a 12 ¼ inch hole which will be drilled with MWD. It is important during well planning that the anticipated survey program as each well section is drilled, is used. The updated or most accurate survey and error model should be entered and used for anti-collision purposes right before a new section is drilled. But during the initial planning the as drilled error models should be used to the total depth of the well to confirm the entire well can be drilled conforming to required separation factor rules.

### 16.2 Misapplication of Uncertainty in Top Hole

There are two common problems in applying uncertainty in the top-hole section.

Top-hole uncertainty must include the radius dimension of the well. This is unlike deep sections where the measurement uncertainty dimension is so great that the radius dimension component of the uncertainty is a very small percentage. In the top hole when measurement uncertainty is just beginning to accumulate, the well radius dimension is a significant component in anti-collision.

If the area being scanned includes multiple sites (platforms or surface locations from which wells have been drilled) then the uncertainty as to the actual coordinates of the surface site must be determined and included in the calculations.

#### Caging

“Caging” is the term for the condition where a new well can no longer be drilled due to the poor positioning of previously drilled wells. This usually happens later in the development cycle of pad or platform drilling. It is useful to include all future planned wells in the collision scanning at the planning stage and during drilling operations so that, whilst not safety critical, sensible avoiding action can be taken so that the potential for future caging is minimized.

**Overly Conservative Targets**

Small targets cost a large amount of money to drill as the directional driller in the field will not be afforded much flexibility from the planned trajectory and will have to spend more rig time steering to the “line”.

**Curved Section Close Approaches**

Interpolating at long intervals when scanning can completely miss a close approach to approach another well. It is recommended to always perform a 3D visualization run down the planned well to visually sense the effects all close approaches.

Initial numerical scan reports should always be run at 100 ft or 30 m intervals. Then refine localized zones with searches using 15 ft or 5 m intervals to better characterize the near close approaches.

**Long Parallels**

It is almost impossible to keep a well straight, so the situation of having two wells with long parallel vertical sections before very deep kick offs should be avoided. (Even if it were possible to maintain a straight well, the survey uncertainty will be growing and with it the risk of collision). Where this happens the planner should include a ‘nudge’ to raise the inclination to around 5 degrees and return to vertical once enough separation had been achieved to compensate for the uncertainty at the deep kick off point.

**CONTENTS**

## 17. Understanding Error Models

### 17.1 Error Models and Instrument Performance Models

Historically four error models have been commonly used in the industry (including one special model developed by Shell for internal use only). These error models define how various error sources affect the observations in the well and thus the positional uncertainty along the wellbore. The mathematical relationship between for example, a bias error on the y axis accelerometer and the positional error at a given survey point is a complicated formula but easily established by these error models. The key to their ability to successfully represent the positional uncertainty is not usually the mathematics but rather the coefficients used to define the numerical accuracies for various tools and how they improve with corrections such as sag, IFR, stretch, interference corrections and so on.

The error models are:

**The Cone of Uncertainty Model**  
**The Wolff and De Wardt Error Model**  
**The SESTEM Error Model**  
**The ISCWSA Error Model**

A brief explanation of each follows.

**The Cone of Uncertainty** was a simple model applied in the early versions of COMPASS introduced by Angus Jamieson in the early 1980s. It consisted of a simple ratio with measured depth that applied over a range of inclinations. For example, an MWD survey might provide uncertainty of 7ft/1000ft at up to 15° of inclination, then 10ft/1000ft at up to 30° degrees of inclination and so on. This model was widely used but is very conservative and probably not suitable for close drilling situations.

**The Wolff and De Wardt Error Model** was published in 1981 and used 5 separate sources of error. These are: a compass reference error; a drillstring magnetization error; an inclination error; a misalignment error; and a relative depth error. All tools were classified as either “gyro” or “magnetic” and either “good” or “poor” quality. A set of values (coefficients) were chosen for each tool and the mathematical model produced an ellipse of uncertainty around the wellbore that could be used for anti-collision calculations. These coefficients were only meant to be used for North Sea operations and were reference to the quality of tools available at the time.

In 1987 the **Shell Extended Systematic Tool Error Model (SESTEM)** was developed in The Hague by Robin Hartman. It provided a significant improvement on the earlier models. This model considers the equipment running conditions, the location of the well, the background magnetic field accuracy, and considers the measurement error sources at their individual component levels.

Around the same time, a group of industry wellbore surveying experts formed the **Industry Steering Committee for Wellbore Survey Accuracy or ISCWSA** under the leadership of Hugh Williamson. Under the auspices of ISCWSA a sophisticated model recognized as the industry standard has been developed.

An ‘IPM’ is an ‘Instrument Performance Model’ and describes the error sources, their magnitudes and how they propagate. It is these IPMs that determine how big the uncertainty envelope will be. The temptation is often to use IPMs that are overly optimistic. That is not a best practice. A good guideline is that the IPM values should be a realistic representation of the errors in the entire system and be able to be demonstrated by good quality control in the field or in the calibration process. In all cases the error models and IPMs should be agreed with the client during the well planning stage in order that subsequent changes do not render a planned well undrillable.

## 17.2 Modelling Uncertainty

Uncertainty modelling provides a method of determining how far out we might be when we estimate something. This can be very useful in all sorts of fields. If for example I were to take a bet on the height of the next person to walk down the street, I would want to know, first of all, what was the normal range of heights for people and even then I would not bet on the average. I would be much safer to bet that they fall between say 0.2 – 3.0 meters high so that I am confident that my bet is 'safe'.

In order to establish a 'safe' bet I need to know both the average and the range of the measurement I am trying to estimate. The German mathematician, Gauss described the 'Normal Distribution' of naturally occurring measurements (of which our heights are one). In this graph the x axis is height and the y axis describes the number of people in a given sample that might fall in a given height range.

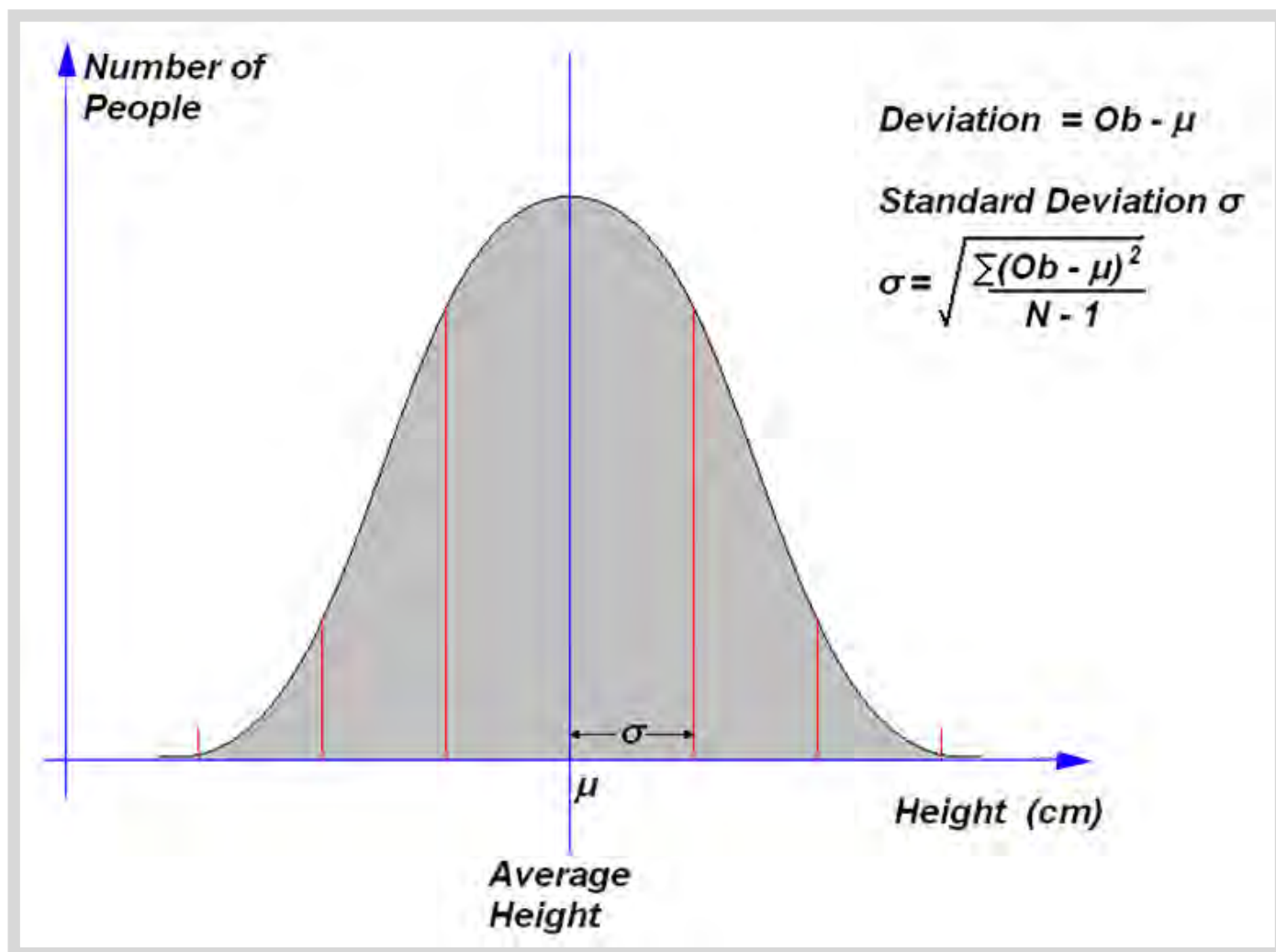


Figure 77: Modelling deviation graphically

In Figure 77 the average height is in the centre and it can be seen that most people fall close to the average. The deviation of any observation is just how far it is from the average. For example, if I am 1.80m tall and the average is 1.50m, my height "deviation" would be 0.3m. Notice that the greater the deviation from the average, the fewer people there will be.

The formula shows a useful parameter, the “standard deviation” which is the square root of the sum of all the deviations squared, divided by  $N-1$  where  $N$  is the number of the sample. This number is used a great deal in uncertainty modelling and serves as a measure of the distribution around the average.

We usually use the Greek letter sigma ( $\sigma$ ) for standard deviation.

For naturally occurring measurements Gauss showed that about 67% of observations will fall within 1 sigma, 95% within 2 sigma and 99.7% within 3 sigma. So if sigma is 0.2m and the average was 1.50m, I could bet on the next person to be between 1.3 and 1.7m and my “confidence” would be 67%. I am a Scotsman, not known for being overly generous so I may decide to bet at 2 standard deviations and say that the next person will be between 1.1m and 1.9m. Now my “confidence” goes up to 95%. If I am still worried, I could bet between 0.9m and 2.1m and now I would only be wrong 3 times in 1000 or 99.7% confident. Clearly with a critical estimate we would want a confident result. In theory it is not possible to obtain 100% confidence with the Gaussian model so we have set the limits somewhere. This is often referred to as “setting the sigma levels” and the higher the sigma levels, the lower the risk.

It should be noted that in nature nothing follows the Gaussian Model exactly. For example, we know that there are no people 3m high in the world so very low risk values are often ignored.

### 17.3 Probability in Two Dimensions

Something interesting happens when we try to guess two parameters at the same time and still need to be confident of our estimates. Let’s say we now guess the person’s height and their intelligence. First, it is important that we understand that these parameters are not “correlated”. In other words, despite what your taller friends might like to think, there is no relationship between height and intelligence. If we were measuring height and weight, we might expect some “correlation” since taller people are probably going to be heavier than shorter people in general.

Watch what happens when we plot the normal distribution curves for the two parameters at once. In this diagram I have drawn the distribution curves on IQ for two height groups on either side of average height. Note that the average IQ for the small group is the same as the average IQ for the tall group.

This demonstrates no correlation between height and intelligence. The average intelligence of all height groups remains the same.

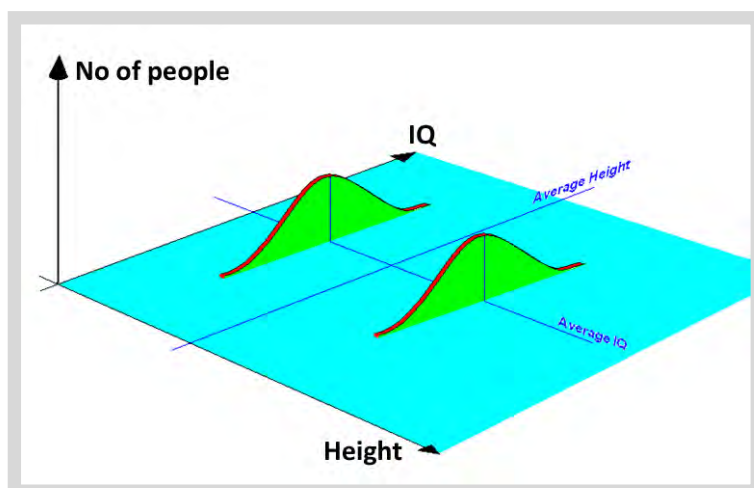


Figure 78: Plotting two normal distribution curves at once



Now we shall plot all the normal distributions for all the height groups.

This normal distribution “mountain” describes the probabilities of two parameters whose ranges are not the same. Any probability “contour” on the slopes of this mountain will therefore be elliptical in shape since the IQ range and the height range have different values.

Now we shall apply this to a section of wellbore. Let us imagine that the well section is straight and has an inclination “I” and an azimuth “A” but both are potentially in error.

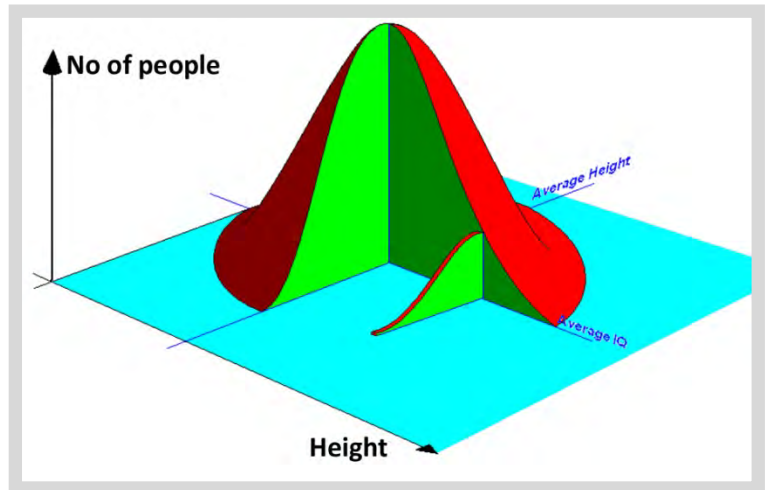


Figure 79: Plotting the normal distribution curves for two parameters

An ellipse of uncertainty is formed around the wellbore where the lateral dimension is proportional to the azimuth error and the high side dimension is proportional to the inclination error. If the azimuth was more accurate than the inclination, the ellipse would be thinner across the wellbore. This example is more typical with the azimuth less certain than the inclination, creating an ellipse with a larger lateral dimension. The final shape is like an almond, elliptical in all three orthogonal planes.

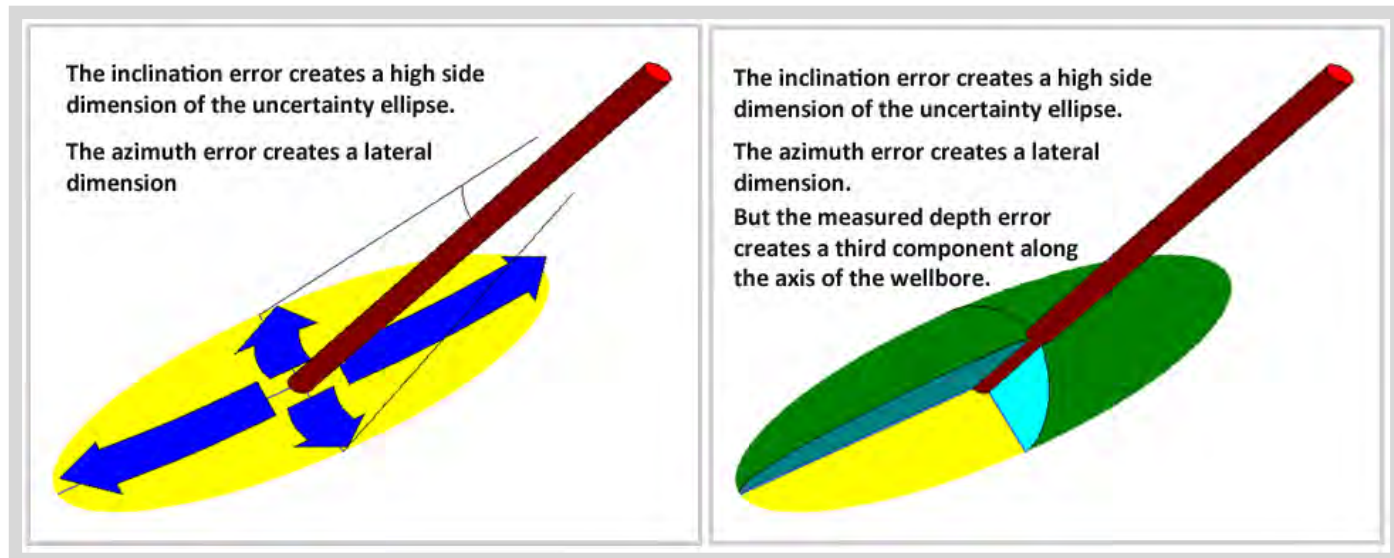


Figure 80: Applying normal distribution modelling to a section of the wellbore

## 17.4 How Can We Determine the Size and Shape?

In reality this is a complex calculation best left to computer software but a very simple rule of thumb can estimate spatial error from an angular error as follows:

1 degree in angle creates about 2% in distance.

For example; if a line of 1000 m was measured on a bearing of 90 degrees plus or minus 1 degree, the final point would be in error by approximately +/- 20m.

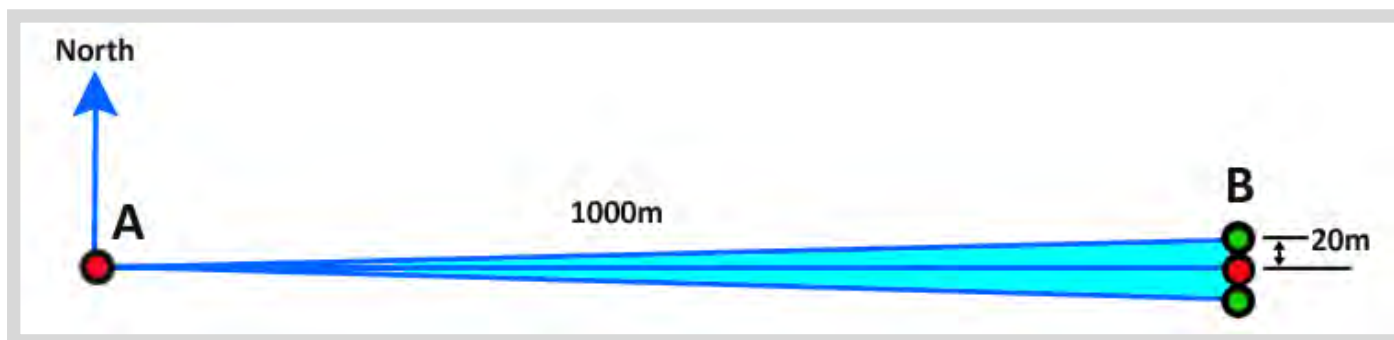


Figure 81: Trajectory error calculations

The correct answer would be closer to  $1000 \sin(1^\circ) = 17.45\text{m}$  but as a conservative estimate the 2% per  $1^\circ$  rule is easy to calculate.

It is not true that errors are proportional to measured depth. In surveying, systematic (i.e. unchanging) errors propagate in proportion to how far you are from your origin. A compass reference error for example may pull you to the right as you walk away from the origin but will still pull you to the right as you return effectively

cancelling out the positional error. A scaling error may underestimate your distance from the origin but equally it will be proportional to the distance and will cancel out on the return. When estimating the likely positional error, we can use this simple fact and the assumption that the dominant errors are systematic. Clearly though, not all errors are. Some errors like gyro drift are time dependent and therefore continue to get worse, the longer the route and others are random like the effects of inadequate survey intervals but we can still come up with a rough estimate that will allow us to assess the realism of any quoted error models and the likelihood of hitting a target.

In this example a target is to be drilled with MWD with the following typical accuracies: measured depth is good to 2m/1000m, inclination to +/- 0.3° and azimuth to +/- 1°. Let's try to work out the approximate ellipse of uncertainty by the time we reach the target.

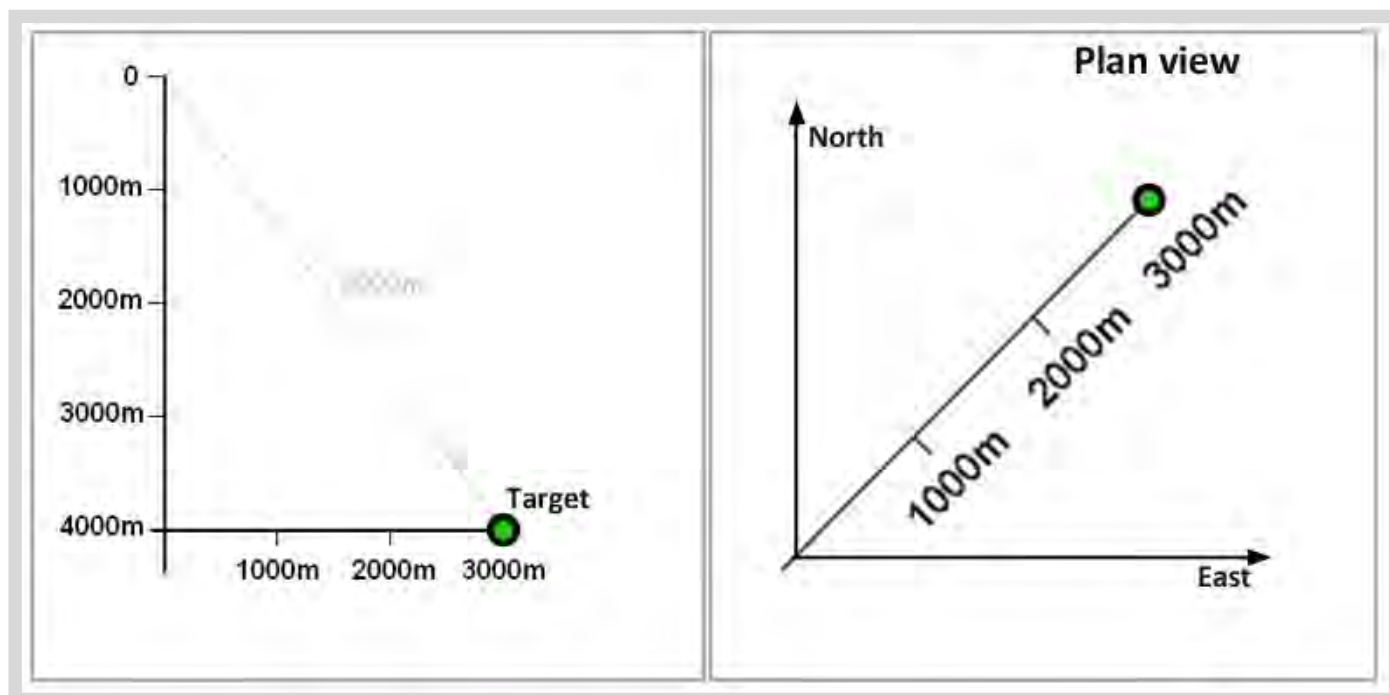


Figure 82: Plotting the uncertainty

Firstly, let's determine the effect of the measured depth error of 2 m/1000. In this simple example, this can be determined without knowing the planned trajectory. The accumulated error at the target will be the same no matter what path we take to get there. This is not necessarily obvious. Using the fact that survey error propagates with distance from origin we can draw the uncertainty axis created by depth error as a line of 10 m ( $2\text{m}/1000\text{m} \times 5000\text{m}$  distance) towards and away from the origin.

By way of example, if the well was drilled as a horizontal well with 4000 m vertical drilling and 3000 m horizontal drilling after a sharp build to horizontal, the total MD would be 7000 m. Let's say that the depth was overshooting by 2 m/1000 m.

In this case, the depth error would be  $2\text{m}/1000\text{m} \times 7000\text{m} = \pm 14\text{m}$ . If this had been a straight vertical well our depth could actually be anywhere between 6986 m and 7014 m.

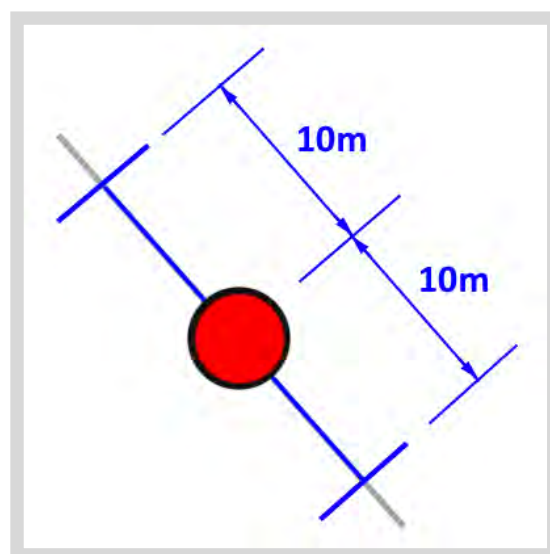


Figure 83: Calculating positional error

But in this case when we are only 5000 m from our origin our depth error at our presumed position is  $2\text{m}/1000\text{m} \times 5000\text{m} = \pm 10\text{m}$ . Traveling to our target position would be to over/under shoot the vertical by 8 m and over/under shoot the horizontal by 6 m creating a positional error of 10 m on the axis shown above.

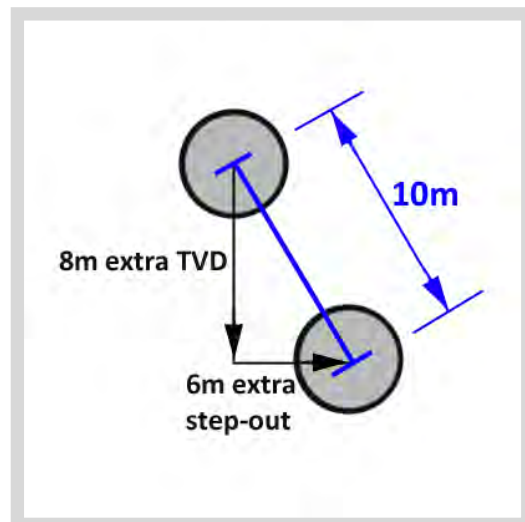


Figure 84: Calculating positional error

The effect of the inclination error can similarly be calculated using our simple rule. Inclination only affects the vertical plane and we are 5000 m from the origin in this plane so the positional error will be at right angles to our space vector and will have a magnitude of 0.6% of 5000 m or 30 m.

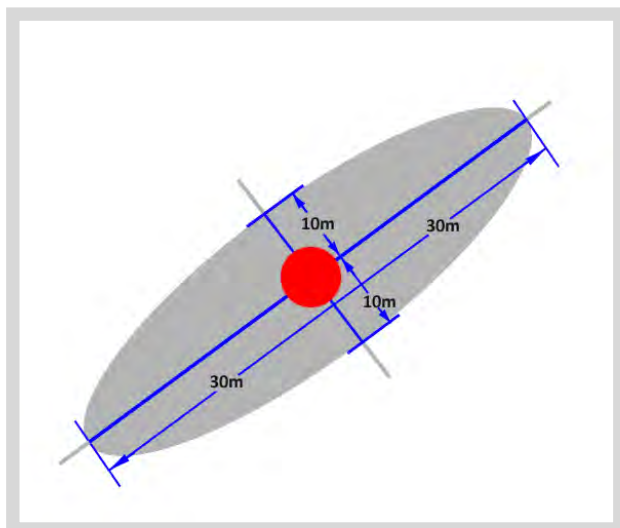


Figure 85: Calculating positional error

The third axis will be in the horizontal plane and is due to the azimuth error of 1°. This will produce an ellipse axis across the wellbore of approximately 2% of 3000 m which is 60 m. It is quite common for the azimuth error to be the dominant error in a 3D ellipse of uncertainty. These ellipses are not to scale but show the orientations and relative sizes.

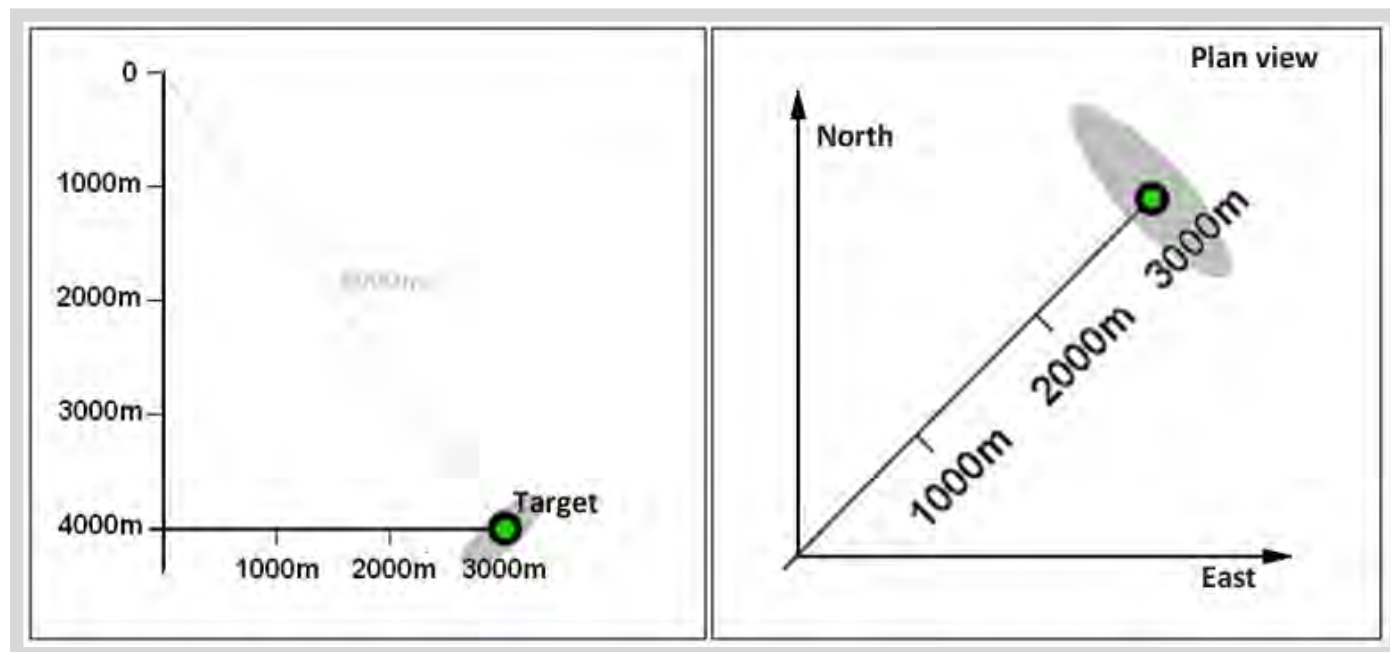


Figure 86: Plotting the ellipse uncertainty



**CONTENTS**

## 18. The ISCWSA Error Model: Introduction

*For a detailed description of the ISCWSA error model, please see [Chapter 19](#) by Dr Andrew McGregor.*

### 18.1 Some Background to ISCWSA

The Industry Steering Committee on Wellbore Survey Accuracy (ISCWSA) is seeking to dispel the confusion and secrecy currently associated with wellbore surveying and to enable the industry to produce consistent, reliable estimates of survey-tool performance in today's wells. They believe this will be achieved through the production and maintenance of standards covering the construction and validation of tool error models.

Work focused initially on MWD systems. They provide a large proportion of the total directional survey data world-wide and, because of their similarities between suppliers, are more amenable to specification standardisation than other types of survey tool. The results of the work on an error model for a basic directional MWD service has been presented in SPE 56702 'Accuracy Prediction for Directional MWD' by Hugh Williamson, at the 1999 SPE Annual Technical Conference and Exhibition in Houston, Texas, held from the 3-6 October 1999.

An updated version of this paper (SPE 67616) has been published in the December 2000 edition of SPE Drilling and Completion (Volume 15, Number 4, pages 221 to 233).

A gyro error model has been produced and published in paper SPE 90408 'Prediction of Wellbore Position Accuracy When Surveyed with Gyroscopic Tools' by Torgeir Torkildsen, Stein Havardstein, John Weston and Roger Ekseth.

Depth issues have been investigated and the results published as SPE 95611, "Quantification of Depth Accuracy", which was presented at the SPE Annual Technical Conference, Dallas, 9-12 October 2005.

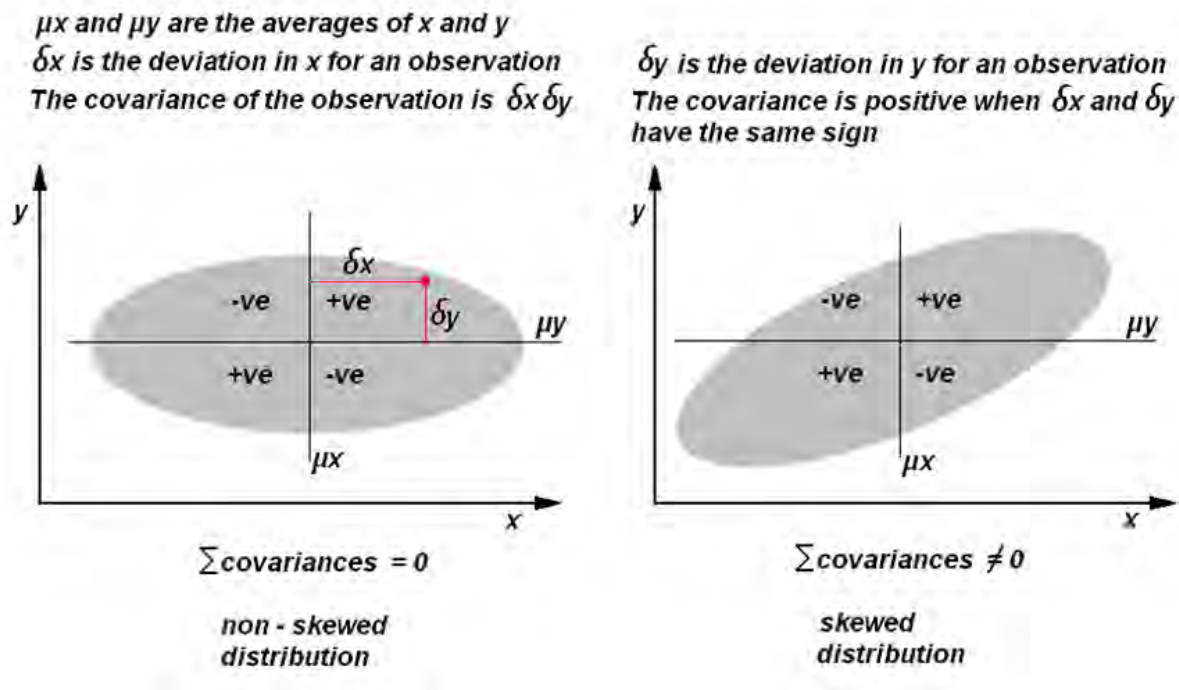
Up till now, the process has been explained very simply to demonstrate how angular errors combine to produce elliptical uncertainty envelopes. In practice there are several sources of error all affecting the wellbore position in different ways and the ISCWSA error model provides a rigorous mathematical approach to combining these various sources into one 3D ellipse.

LINK [ISCWSA website](#)



## 18.2 Covariance

First we have to introduce the idea of “covariance”.



As the name suggests it is a measure of how parameters vary together. Recall that we discussed how height and weight might vary together (correlate) but height and intelligence do not. If we measure the variance of an observation, it is simply the square of the deviation but the covariance is the product of the deviations of two parameters. The covariance helps us to measure the correlation which shows up as a “skew” in the ellipse.

The above figure shows this, but it is also true in 3D and if we can build up a matrix of covariances in northings, eastings and TVD we can derive an ellipsoid, its dimensions and orientation in 3D space.

In order to build up this matrix we need to know how each error source affects the observations and how the observation error will move the wellpath in North, East and vertically in TVD.

### 18.1.1 How the Errors Affect the Observations.

These error sources are multiple and varied. In the ISCWSA error model there are dozens of error sources. Each will affect a given survey station in different way. For example, the accuracy with which we know our magnetic north would be a simple azimuth effect. This will not have any effect on either inclination or measured depth observations. “Weighting Functions” are used to determine the effect any error source will have on MD, inclination and azimuth respectively. We say that the weighting functions for a compass reference error are (0, 0, 1) i.e. they have no effect on MD, no effect on inclination and a full effect on azimuth.

However, a tool misalignment due to a bent housing in the assembly might affect inclination or azimuth depending on the toolface. In this case the weighting function would be (0,  $\cos(\text{Toolface})$ ,  $\sin(\text{Toolface})$ ). A drillpipe stretch error would have a weighting function of (1, 0, 0) as you might expect and a BHA sag correction error would have a weight function of (0, 1, 0). The ISCWSA error model SPE paper 67616 (from the ISCWSA website – [iscwsa.org](http://iscwsa.org)) details all the weighting functions for all the error sources.

The next step is to determine the effect of the observation error on the well path position. In this diagram you can see that a measured depth error could affect North East and TVD.

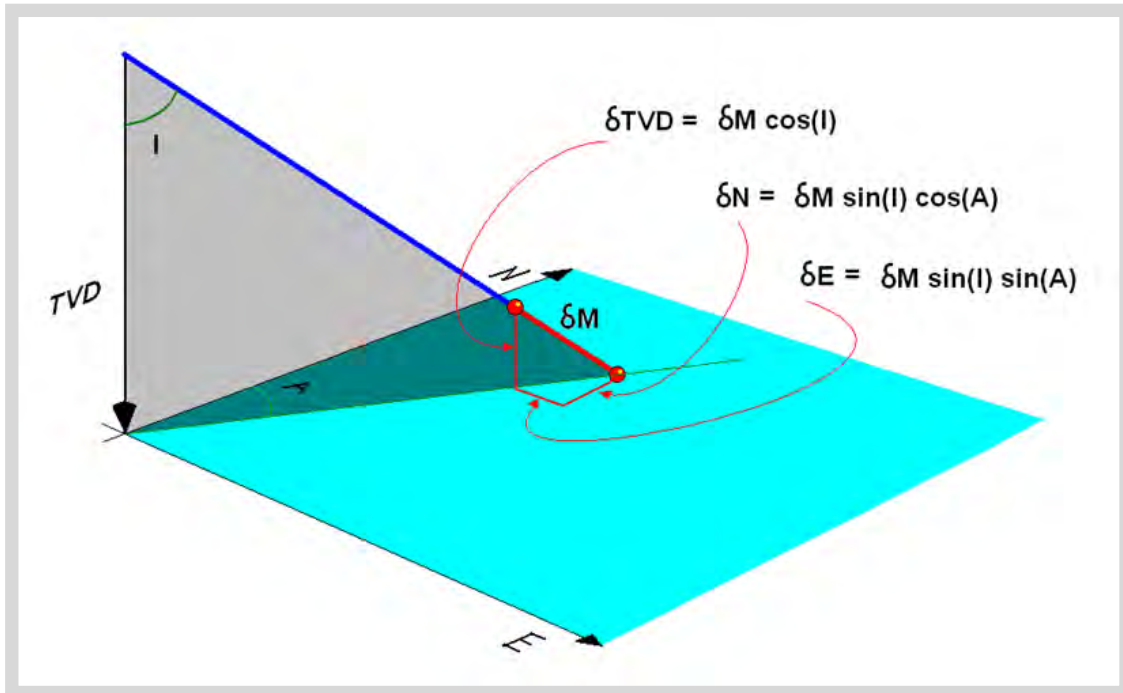


Figure 87: Showing that a measured depth error could affect North, East and TVD

But an azimuth error only affects North and East, so we get the following:

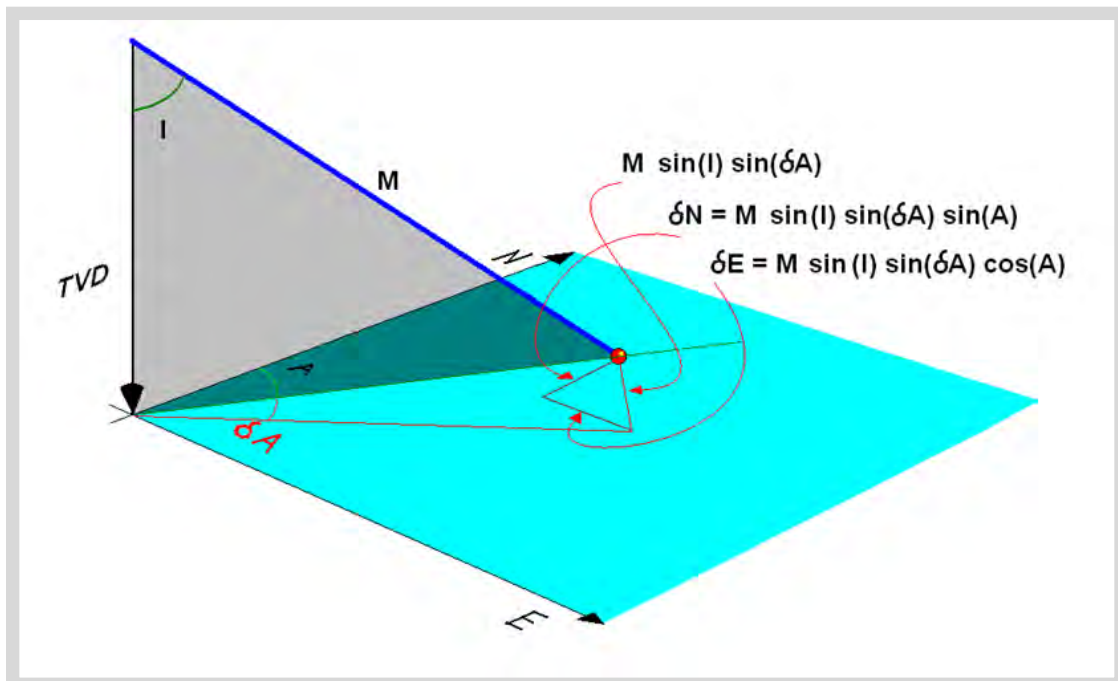


Figure 88: Effect of azimuth error on North and East elements

## 18.3 The Variance Covariance Matrix

<b>The Variance Covariance Matrix</b>		
$\sum \delta N^2$	$\sum \delta N \delta E$	$\sum \delta N \delta V$
$\sum \delta E \delta N$	$\sum \delta E^2$	$\sum \delta E \delta V$
$\sum \delta V \delta N$	$\sum \delta V \delta E$	$\sum \delta V^2$

When accumulating the matrix, care has to be taken to ensure that errors that correlate from one survey station to the next are added to the delta values directly before summing but errors that can vary from one survey to the next are summed in their product form. This ensures that random and systematic effects are propagated correctly. Some errors also continue from one survey leg to another and some even from one well to another such as the error in magnetic north.

Once the matrix is complete a technique is required to derive the size and orientation of the three main axes.

## 18.4 Eigen Values and Eigen Vectors

Imagine looking at an almond which you are holding in your hand. You can choose to look at it from above, in front or any other direction in space. However, no matter how the almond is oriented there will always be three orthogonal viewing vectors that let you see the ellipses of the almond at their full size. In other words, if you line up your eye on one axis, you will see the ellipse formed by the other two with no foreshortening effects.

Eigen vectors provide a way to derive the best viewing angles to see the 3 uncertainty ellipses. The Eigen vectors of the Covariance Matrix describe the “attitude vectors” of the three axes and the Eigen values tell us their length. The mathematics of converting a 3 x 3 Covariance Matrix to its Eigen vectors and Eigen values is very straightforward and provides us with the dimensions and orientation of our uncertainty ellipsoid. It is a matrix manipulation that finds the ‘viewing’ vectors that leave the main dimensions of the ellipse on the leading diagonal with zeros for all the covariances when seen from these axes.

By accumulating these ellipsoids along the wellbore, we create an “uncertainty envelope” like a funnel around the wellbore which we can then use to ensure a safe passage when drilling close to other wells.

## 18.5 Collision Risk

It would be wrong to think that if two uncertainty envelopes were touching there was always a high risk of collision. We often use between 2 and 3 standard deviations when determining the size of our ellipses which means that probability of being outside the ellipse is very small.

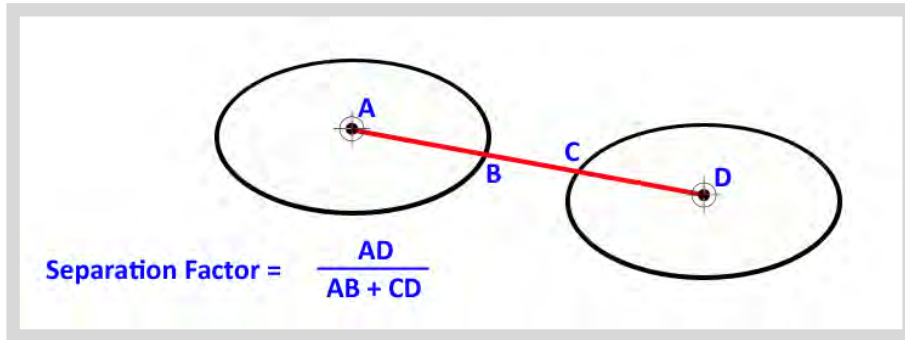


Figure 89: Calculating and plotting the collision risk

When considering collision risk, we often use the separation factor calculated in a plane at right angles to the offset well. This simple formula is one method of calculating separation factor. A separation factor of one would indicate that the ellipses were just touching. By way of example, if the hole size occupied one third of the ellipse and the ellipse was set at 3 standard deviations, the probability of these wells colliding would be less than 1 in 300,000 but the risk rises rapidly as the ellipses overlap. The separation factor is an excellent way of drawing attention to high risk areas quickly then more detailed analysis may be needed to determine the safety of continuing to drill.

## 18.6 Definition of Ellipse Axes

There is no recognized industry standard for defining the dimensions of the ellipse of uncertainty. The axes can be either the true 3D axes length or a projection usually in the horizontal plane or the perpendicular plane (looking down the wellbore). TVD Spread is always the vertical TVD occupied by the ellipse of uncertainty.

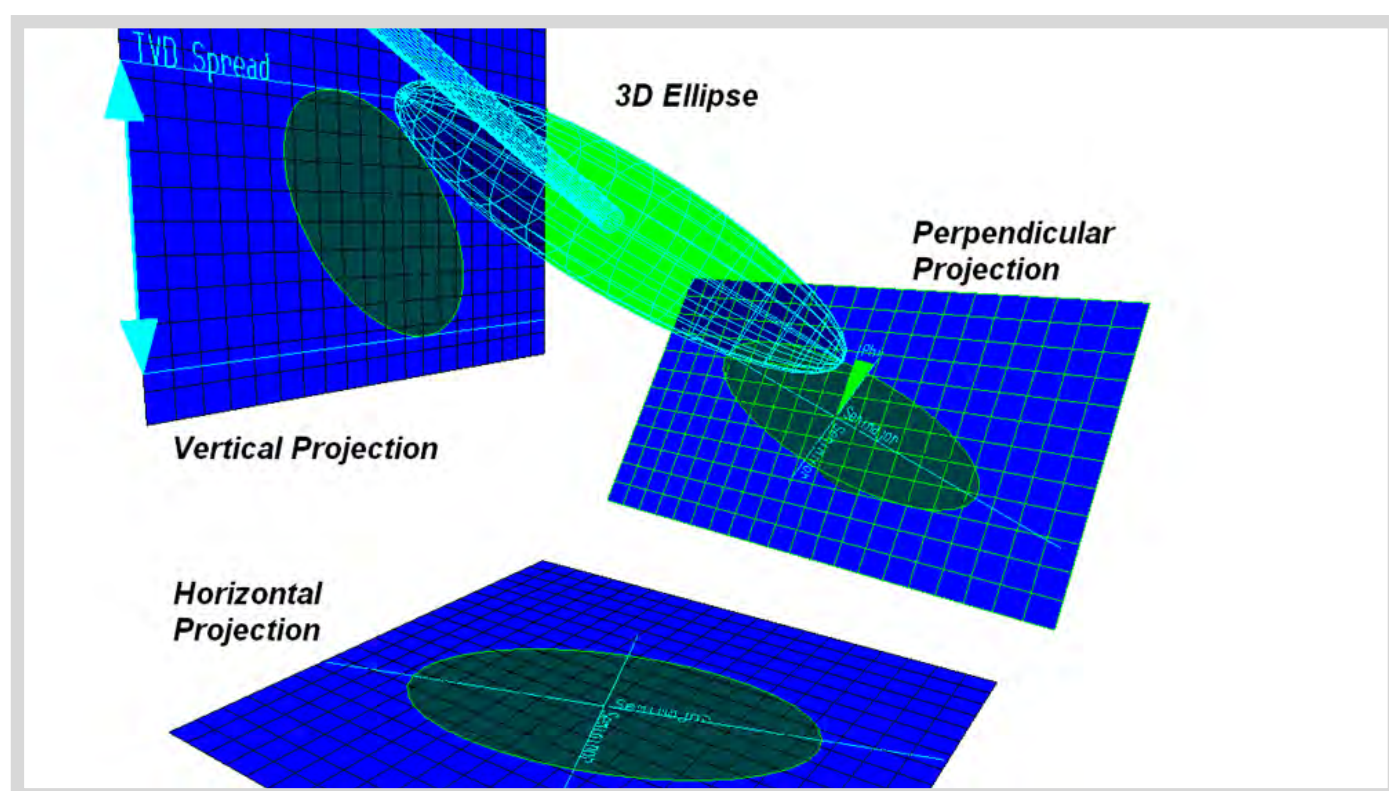


Figure 90: Calculating and plotting the collision risk

Care should be taken when interpreting an ellipse of uncertainty report. Different companies report different definitions of the ellipse. The real uncertainty envelope is a 3 dimensional body and most software applications project this into a plane. In the graphic above, it can be seen that the plane may be vertical, horizontal or perpendicular to the wellpath. As a result, the quoted semi major and semi minor axes (and possibly orientation) may mean any of the following;

- The 3D dimensions of the ellipse closest to the lateral and high side vectors.
- The horizontal projected ellipse major and minor axes and orientation from north.
- The perpendicular projected major and minor axes and orientation from high side

TVD Spread nearly always means the TVD occupied by the ellipse but can be quoted as a plus or minus number or an enclosing value.

Historically there has been no standardization of these terms but clearly they will produce different results for the same well path with the same error model.



## 18.7 How Errors Propagate

Errors in measurement systems can propagate randomly or systematically. The random errors tend to have a cancelling out effect over multiple observations as their effect can be positive or negative from observation to observation. The systematic errors are the ones that generally expand to dominate the error envelope since their effect is the same from observation to observation.

As an example of a systematic error, the azimuth error in MWD is largely created by the uncertainty of the magnetic field direction (declination). Clearly this does not change from one observation to another and can be taken as a systematic shift in azimuth. A misalignment error on the other hand would be considered random since its effect is toolface dependent and the surveys will have a scatter of tool faces throughout the survey.

Some errors, like declination, are referred to as 'global' in that they affect every survey in every well in the same field where the declination is uncertain. Others vary from one well to another such as vertical reference and others vary from one survey leg to another such as sensor errors. When we accumulate the uncertainties in a formal error model, the propagation effects of each error source are correctly accumulated so that global errors are always present and random errors are accumulated with RMS values across the boundaries where they become randomized. For a misalignment that is every survey station, for a sensor error, that is every survey leg, for a reference error that is for the whole well and for declination error that would be applied to every well in the field.

**The next chapter describes the ISCWSA error models in more detail.**



## 19. The ISCWSA Error Models: Explanation and Synthesis

This chapter is included courtesy of Andrew McGregor of Tech21 Engineering Solutions, from a paper produced for ISCWSA. The text and associated appendices are taken from the paper:

**The ISCWSA Error Models: An Explanation and Synthesis, version 11.**

### 19.1 Introduction

Like all measurements, borehole surveys are subject to errors and uncertainties which mean that a downhole survey result is not 100% accurate. For many applications, such as anti-collision and target sizing, it is very important to be able to quantify the position uncertainty around a wellbore trajectory. However, since many different factors contribute to the final position uncertainty it is not a trivial matter to determine these bounds.

The Industry Steering Committee for Wellbore Survey Accuracy (ISCWSA) has produced an error model in an attempt to quantify the accuracy or uncertainty of downhole surveys. The error model is a body of mathematics for evaluating the uncertainty envelope around a particular survey.

Originally the error model dealt with only MWD surveys, but it has later been extended to also cover gyro surveys. This document sets out to provide an overview and understanding of these models. The full details can be found in two SPE papers; SPE-67616 and SPE-90408 (see references below). There have also been successive revisions to both models, details of which can be obtained from the ISCWSA website [iscwsa.org](http://iscwsa.org)

The error model identifies a number of physical phenomena which contribute to borehole survey errors and provides a mathematical framework for determining in numeric terms the uncertainty region around a particular survey. Typically, this error model will be implemented in directional drilling software. The user will select the appropriate tool model for the survey tool that will be or has been run and the error results will be used in anti-collision or target sizing calculations.

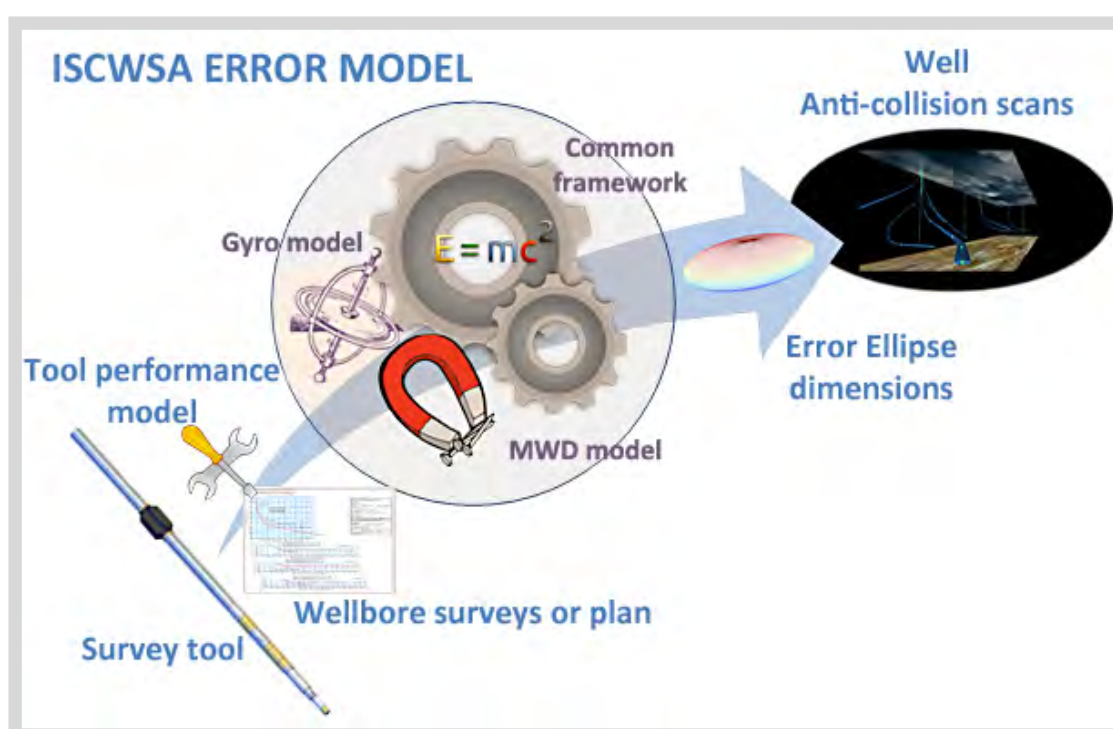


Figure 91: ISCWSA error model schematic

In simple terms, the error model is a means to start from a gyro drift specification in deg/hr or a tool misalignment in degrees and evaluate how that error affects the borehole survey measurements of inclination, azimuth and measured depth at a particular survey station. The model then propagates and combines these error contributions, taking into account all of the important physical errors, at all of the survey stations from all of the survey runs within a well. The final results are error ellipse dimensions, in metres or feet, within which the actual wellbore is expected to be found to a specified level of confidence.

It is common to talk about the MWD model and the gyro model, but in fact these both of these models share a common framework for describing and propagating the errors. This document will present some of the background information on the ISCWSA models before presenting this basic mathematical framework on which they are based. The MWD model is described in some detail, followed by a discussion of the gyro error model. There follows a section which is concerned with implementation details, which will mainly be of interest to software developers. The last section discusses standardisation of the model.

There is some maths in these early sections but it should still be possible to follow the thread of the discussion without worrying too much about the details of the equations. For those with a thirst for more, three appendices present in detail the mathematics of the framework and all of the weighting function equations.

To follow the discussion, the reader should at least be familiar with the basic concepts of borehole surveying. A good starting point would be an understanding of chapters 5 and 10 of this book which describe the principles of MWD and gyro tools and also chapters 18 and 20 which present an introduction to error modelling and error propagation.

### **19.1.1 Assumptions and Limitations of the ISCWSA Model**

The error model is designed to be a practical method that can be relatively easily implemented in software and then used by well planners and directional drillers. It is intended to be applied to a range of tools, used worldwide and accordingly attempts to give good representative survey uncertainties, without the need to model every single variation of tool or running conditions.

The model only applies to surveys run under normal industry best-practise procedures which include:

- a. rigorous and regular tool calibration,
- b. a maximum of 100ft survey intervals.
- c. field QC checks, such as total magnetic field, gyro drifts, total gravity field and magnetic dip angle on each survey measurement,
- d. the use of non-magnetic spacing for MWD surveys according to industry norms,
- e. for MWD, surveys taken in a magnetically clean environment away from casing and adjacent wells.

It should be recognised that the model cannot cover all eventualities and works on a statistical basis and so does not say anything specifically about any individual survey. The results can be interpreted as meaning that if a well was properly surveyed a number of times by a variety of different tools with the same specification, then the results would be expected to be randomly distributed with a range of values corresponding to the error model uncertainty results.

The model cannot cover gross blunder errors such as user error in referencing gyros, defective tools or finger trouble entering surveys into a database. The model does not cover all variations and all possibilities in borehole surveying, for example survey data resolution is not modelled.

To qualify under the assumptions, the survey interval should be no more than 100ft. If the survey interval is greater than 100ft then strictly the model is not applicable. Hence, the error model does not include penalty terms for intervals greater than 100ft, nor does it model any improvements for shorter survey spacing.

MWD surveys which are subject to external magnetic interference will generally fail QC checks. The effect on survey accuracy of magnetic interference from adjacent wells or from casing, can vary enormously and in many instances are impossible to quantify. The error model does not attempt to determine the size of the error for any surveys which are subject to this kind of interference.

Finally, a major misconception is that the ISCWSA provides certified error models for specific survey tools. The published ISCWSA papers only define the process and equations to work from a set of error model parameters to an estimate of position uncertainty. The ISCWSA committee does not define, approve or certify the tool codes containing the actual error model magnitudes which drive the error model. These should be obtained from the survey contractor who provides the tool, since they are the ones best placed to understand the specifications and limitations of their tools.

Only in the specific cases of a standard MWD tool, or a MWD tool with an axial (short-collar) interference correction applied does the ISCWSA specify any parameter values.

### 19.1.2 References in this Chapter

1. Accuracy Prediction for Directional Measurement While Drilling  
Hugh Williamson, SPE-67616
2. Prediction of Wellbore Position Accuracy When Surveyed with Gyroscopic Tools  
Torgeir Torkildsen, Stein Harvardstein, John Weston, Roger Ekseth, SPE-90408
3. Quantification of Depth Accuracy  
A. Brooks, H. Wilson, A. Jamieson, D. McRobbie, S.G. Holehouse SPE-95611
4. ISCWSA MWD Error Model Revisions  
S. Grindrod, rev6 8/10/09 available at [www.iscwsa.org](http://www.iscwsa.org)
5. MWD Toolface Independent Error Terms  
S. Grindrod CDR-SM-03 Rev4 November 2009 available at [www.iscwsa.org](http://www.iscwsa.org)
6. Confidence Limits Associated with Values of the Earth's Magnetic Field used for Directional Drilling  
Susan Macmillan, Allan McKay, Steve Grindrod SPE/IADC-119851
7. A Comparison of Collision Avoidance Calculations  
Shola Okewummi, Andrew Brooks SPE/IADC-140183
8. Borehole Position Uncertainty; Analysis of Measuring Methods and Derivation of Systematic Error Model  
Chris J.M. Wolff and John P. DeWardt SPE-9223

### 19.1.3 Abbreviations

BGGM	British Geological Survey Global Geomagnetic Model
HLA	Highside – Lateral – Alonghole Co-ordinate system
IFR	In Field Referencing
IPM	Instrument Performance Model
IGRF	International Geomagnetic Reference Field
ISCWSA	Industry Steering Committee for Wellbore Survey Accuracy
MWD	Measurement Whilst Drilling
NEV	North – East – Vertical Co-ordinate system
RSS	Root Sum Square
SPE	Society of Petroleum Engineers

### 19.1.4 Nomenclature

The following variables are used in the weighting functions:

$A_m$	magnetic azimuth
$A$	true azimuth
$B$	magnetic total field
$B_H$	horizontal component of magnetic field
$D$	along-hole depth
$\Delta D$	along-hole depth between survey stations
$G$	Earth's gravity
$I$	inclination
$\alpha$	toolface angle
$\Omega$	Earth's rotation rate
$\phi$	latitude
$\Theta$	magnetic dip angle
$\gamma$	xy-accelerometer cant angle
$f$	noise reduction factor for initialisation of continuous surveys
$k$	logical operator for accelerometer switching
$V_d$	gyro drift
$V_{rw}$	gyro random walk
$W_{12}$	misalignment weighting term
$W_{34}$	misalignment weighting term

### 19.1.5 Definition of Axes

For clarity the following axes sets are used in the error model:

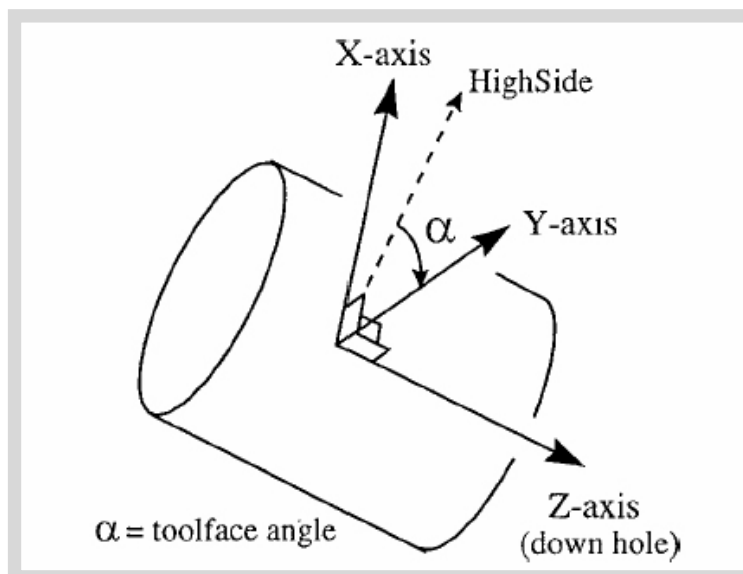


Figure 92: Error model axes definition

#### Body Reference Frame (tool axes);

The z-axis is coincident with the along hole axis of the survey tool and the x and y-axes are perpendicular to z and to each other. This is axes set used to describe orientations of the various sensors.

#### Earth Centred Reference Frame (nev);

The x-axis is in the horizontal plane and points toward true north, the y-axis is also in the horizontal plane and points towards true east. The z-axis points downwards.

**Borehole Reference Frame (hla);**

The z-axis is aligned along the borehole axis. The x-axis is perpendicular to z and points toward the high side. The y-axis perpendicular to both of these and hence is laterally aligned across the borehole.



## 19.2 Framework of the Error Model

### 19.2.1 Overview of the Error Model

The basic purpose of the error model is to combine the effects of the various different physical factors which lead to survey errors in order to determine the 3-dimensional position error ellipse at any particular survey station. The same basic mathematical framework is used for both the MWD and gyro error models.

To do this,

- i) the model identifies a number of **error sources** which effect downhole surveys. These are identifiable physical phenomena which will lead to an error in the final wellbore position; for example, the residual sensor error after calibration.
- ii) each error source has an **error code** string such as ABZ or MSZ. This is simply a shorthand identifier.
- iii) each error source has a set of **weighting functions**, which are the equations which describe how the error source effects the actual survey measurements of measured depth, inclination and azimuth.
- iv) Each error source also has a **propagation mode** which defines how it is correlated from survey to survey; this is used in summing up the errors.
- v) for a particular survey tool, each error source has an **error magnitude**.

Before we discuss each of these items in detail, here is an example of how the error model works which should help to illustrate what these terms mean.

#### **Example 1: Declination error**

Downhole MWD tools measure magnetic azimuth and in order to calculate the true (or grid) north azimuth values, the declination term has to be added to the downhole data:

$$A_{true} = A_m + \delta$$

Usually, declination is determined from a global magnetic model like the BGGM or IGRF models. However, these work on a macro scale and may not be totally accurate in an oil field. So there is some uncertainty (or error bounds) on the declination value and this is clearly a possible source of survey error.

Therefore, the MWD model identifies an **error source** with the mnemonic **code** DEC which can be used to model declination uncertainty. From the above equation we can see that a declination error will lead directly to an error in the true azimuth, but it has no effect on inclination or depth measurements. Hence the DEC **weighting functions** are [0,0,1] (i.e. md=0, inc=0, az=1).

The standard MWD model gives the DEC error source a **magnitude** of 0.36°. If an In-Field Reference survey was carried out in the field, then the declination uncertainty would be smaller and there could be a different tool model for MWD+IFR with a smaller magnitude for this error source.

If we assume that, whatever the value, the declination is constant over the whole oil field then all MWD surveys, with all different survey tools and in all BHA used in all the wells in the field will be subject to the same error. Hence then DEC term has a global **propagation mode**.

Declination error is a function of the Earth's magnetic field and has no influence on gyro survey tools, so the gyro model doesn't need to include a declination error term.

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(N.B. In fact to model the variation in declination over the global the MWD model uses both the constant DEC term described here and also a second DBH term which is inversely proportional to the horizontal component of total field, but that complication can be ignored for the sake of this discussion.)

### 19.2.2 Error Sources

An error source is any physical phenomenon which contributes to the overall positional measurement error.

Examples of error sources include residual sensor errors after calibration, misalignment of the survey tool with the borehole axis, uncertainties in the Earth's magnetic field, which is the reference against which MWD measurements are made, deflection of the survey tool under gravity, stretch of drillpipe or wireline under the weight of the BHA or survey tool etc.

Between all versions of the MWD and gyro models, some ninety-eight individual error sources are identified. These are not all applicable to each survey tool, but are dependent on the type of tool in operation and how it works. A typical tool model (or IPM file) defines which of these error sources are invoked to model that tool.

### 19.2.3 Error Magnitudes

For a particular tool model, each error source has an error magnitude. The error magnitude is essentially the standard deviation of the range of values which the error source might be expected to take over a statistical sample of survey data under normal field operating procedures. For example, if you consider a large number of MWD runs, what are the statistics for the range of tool misalignments to the borehole?

The values may change depending on what survey techniques or corrections are being applied to the job in hand. So as previously mentioned, using an IFR survey to measure the declination value in the field reduces the magnitude of the declination error term. There is still a declination error source, and the weighting functions remain the same, but compared to the MWD tool model, the MWD+IFR tool model will have a smaller magnitude for the declination term.

The MWD paper gives values for these for 'normal' MWD surveying. However, beyond that initial set error magnitudes are not set by the ISCWSA.

For the gyro error model, it is expected that error magnitudes will be supplied by the gyro contractor. Test cases are defined in the gyro paper but these are not considered to model any particular survey tools.

The error magnitudes defined in the MWD paper are all at one standard deviation (1-sigma). If the user requires final error ellipses at two standard deviations (or three) then the 1-sigma ellipses can simply be multiplied up and typically drilling software has a user control to define at what level error ellipses are to be output. There are two provisos to this – some drilling software packages allow the user to enter error magnitudes at different defined confidence levels (e.g. 1-sigma or 2-sigma etc.) Also, changes to the MWD at revision 4 may require the user to define the required output confidence level first so that certain magnetic field reference terms can be correctly calculated (for further details see section 19.3.4).

### 19.2.4 Weighting Functions

Each error source has a set of weighting functions which define how that error source effects the actual survey measurements of measured depth, inclination and azimuth. These weighting functions are simply the equations that link the error source to the survey measurements, e.g. the weighting functions enable us to take a z-magnetometer bias uncertainty in nano-Teslas and calculate a survey azimuth uncertainty in degrees at a particular survey station in a particular wellbore.

The actual survey inclination and azimuths are obtained from the sensor data via a set of survey equations. So for example for a standard MWD tool the inclination and azimuth are determined from the following equations:

$$I = \cos^{-1} \left( \frac{G_z}{\sqrt{G_x^2 + G_y^2 + G_z^2}} \right)$$

$$A_{true} = \tan^{-1} \left( \frac{(G_x B_y - G_y B_x) \sqrt{G_x^2 + G_y^2 + G_z^2}}{B_z (G_x^2 + G_y^2) - G_z (G_x B_x - G_y B_y)} \right) + \delta$$

Similar survey equations exist for gyros tools and these MWD equations change if axial interference corrections are made.

The weighting functions can be derived from these equations by taking the partial derivatives of the survey equations with respect to the error source. Examples of the derivations can be found in the SPE papers, whilst all of the error sources and weighting functions for both models are given in the appendices. We now consider another example to illustrate this point:

### Example 2: Sensor error - Z-Accelerometer Bias

If we consider the effect of a z-accelerometer bias error; instead of reading the correct value of  $G_z^{true}$  the tool will actual give:

$$G_z^{measured} = (1 + G_z^{scalefactor}) G_z^{true} + G_z^{bias}$$

where  $G_z^{bias}$  and  $G_z^{scalefactor}$  represent the residual errors of the survey tool after calibration.

This equation represents a fairly standard, first-order method for modelling the output of a sensor (almost any type of sensor), when we know that it will not give perfect output.

The MWD model has an error source, coded ABZ for the z-accelerometer bias which corresponds to this  $G_z^{bias}$  term. From the MWD survey equations above, we can see that the  $G_z$  term appears in both the inclination and azimuth equations.

However, the accelerometer readings don't have any effect on measured depth. So the MD weighting function is 0, but the inclination and azimuth **weighting functions** are determined by taking the partial derivatives of these survey equations with respect to  $G_z$  i.e. for ABZ the weighting functions are:

$$\left[ 0, \frac{\sin I}{G}, \frac{\tan \Theta \sin I \sin A_m}{G} \right]$$

Since we are assuming that this z-accelerometer bias is due to residual tools errors, this error source will have the same value for each survey taken with that tool. However, if we change tools, the error will change. Hence the **propagation mode** is systematic (the same at each survey station in a run, but different for different legs and wells).

The model gives ABZ a **magnitude** of  $0.004 \text{ ms}^{-2}$ , meaning that for a number of properly calibrated tools if we ran a number of tests, we'd expect to get a Gaussian distribution of results with a standard deviation of  $0.004 \text{ ms}^{-2}$ .

Gyro tools can be designed a little differently – some systems also have a cluster of three accelerometers and the inclination weighting function will be the same as the MWD case (this is the gyro XYZ-ZB term). Other gyro tools only have x and y-accelerometers and use the assumed total gravity value, and therefore these tools would be modelled without a z-accelerometer bias term. We can see that the error sources which are included in any particular survey tool model depend on the design of that tool.

### 19.2.5 Error Propagation

The core equation for the propagation of the errors from the error source through to the survey position error is:

$$e_i = \sigma_i \frac{dr}{dp} \frac{\partial p}{\partial \varepsilon_i}$$

Where:

$e_i$  is the size of the error in NEV axis due to error source  $i$  at the current survey station  
(a 3x1 vector)

$\sigma_i$  is the magnitude of the  $i$ th error source (a scalar)

$\frac{\partial p}{\partial \varepsilon_i}$  are the weightings functions, the effect of the  $i$ th error source on the survey measurements; md, inc and azimuth. (a 3x1 vector)

$\frac{dr}{dp}$  is the effect of the survey errors in md, inc and az on the wellbore position in the NEV axis, (i.e. a 3x3

$$\text{matrix} \begin{pmatrix} \frac{dN}{dMd} & \frac{dN}{dInc} & \frac{dN}{dAz} \\ \frac{dE}{dMd} & \frac{dE}{dInc} & \frac{dE}{dAz} \\ \frac{dV}{dMd} & \frac{dV}{dInc} & \frac{dV}{dAz} \end{pmatrix}$$

Wellbore positions are calculated using one of the standard methods such as minimum curvature or balanced tangential, so over an interval, the  $\frac{dr}{dp}$  matrix depends on the surveys at either end of the interval. The derivation of the  $\frac{dr}{dp}$  matrix equations is given more detail in [Appendix A](#).

The tool model for any particular survey instrument will usually include a number of different error sources, and we must consider all survey legs in the well and all the survey stations in each leg. So for a well we must add the error contributions over all survey legs in the well; each survey station in each leg and the contributions from each error source.

### 19.2.6 Summing Error Terms and Propagation Modes

Once we have calculated the contribution to the error ellipse from each error source, at each survey station in each leg of our well we have to sum up all the contributions.

There are two basic cases:

**1) The contributions are directly linked** (correlated in mathematical terminology).

For example; the z-axis magnetometer bias error. If we are using the same tool and BHA, then we would expect this error source to have the same value from survey station to survey station and the effects of the error will build all the way down the wellbore.

In this case the error contributions are added in the usual arithmetic way:

$$e_{total} = e_1 + e_2$$

## 2) The contributions are not linked at all (statistically independent).

For example; if we have two independent error sources, then they could both cause a positive inclination error and add together but it is also possible that one might create a positive inclination error and the other a negative error.

In which case we are taking a random value from pot 1 and a random value from pot 2 and the error contributions must be root sum squared (RSS) together:

$$e_{total} = \sqrt{e_1^2 + e_2^2}$$

In fact, it is an assumption of the model that the statistics of the various different error sources are independent so they must be RSS'd together – for example, there is no reason why sag error would be connected to z-axis magnetometer bias or to declination error etc.

However, if we take the example from 1) above, although we can see that the z-axis magnetometer bias should remain the same throughout a survey leg, if we go to another leg, using a different tool or to another well then we would expect that error source to be independent over that range.

So far, the error sources are independent from each other, but a given error source might be independent at all times, or correlated from station to station within a survey leg or from survey leg to survey leg with a well or from well to well within a field.

Therefore, the model defines four **propagation modes** for the errors:

Random	R	always independent
Systematic	S	correlated from survey station to survey station
Well by Well	W	correlated from leg to leg
Global	G	correlated over all wells

The propagation mode is a property of the error source and is defined in the tool model. In practise, most error sources are systematic or random and only a limited few well by well or global sources have been identified.

To combine all the error sources, we need to create a sum over all survey legs, survey stations and error sources which apply to a particular well. When doing this summation, the propagation mode is used to define at what step in the summation arithmetic addition is used and at what stage RSS addition is required.

$$total\ error = \sum_{l=1}^{Survey\ Legs} \sum_{i=1}^{Survey\ Station} \sum_{k=1}^{Error\ Source} e_{l,i,k}$$

The mathematical details of this process can be found in [Appendix A](#). The final output of the summation is a 3x3 covariance matrix, which describes the error ellipse at a particular station. In the *nev*-axes, the covariance matrix is:

$$[C]_{nev} = \begin{bmatrix} \sigma_N^2 & \sigma_N\sigma_E & \sigma_N\sigma_V \\ \sigma_N\sigma_E & \sigma_E^2 & \sigma_E\sigma_V \\ \sigma_N\sigma_V & \sigma_E\sigma_V & \sigma_V^2 \end{bmatrix}$$



Here  $\sigma_N^2$  is the variance in the north-axis and the uncertainty in north axis (at 1-standard deviation) is  $\pm\sqrt{\sigma_N^2}$ . In the same way, the other terms on the lead diagonal are uncertainties along the other principle axes. The  $\sigma_N\sigma_E$ ,  $\sigma_N\sigma_V$  and  $\sigma_E\sigma_V$  terms are the covariances and give the skew or rotation of the ellipse with respect to the principle axes.

### 19.2.7 Transformation to Borehole Axes

The covariance matrix above is expressed in the earth-centred *nev*-axes, this can be transformed to the borehole reference frame, *hla* by pre- and post-multiplying the covariance matrix with the *nev*-to-*hla* direction cosine matrix,  $[T]_{hla}^{nev}$ .

$$[C]_{hla} = [T]_{hla}^{nevT} [C]_{nev} [T]_{hla}^{nev}$$

The direction cosine matrix can be obtained a rotation in the horizontal plane to the borehole azimuth, followed by a rotation in the vertical to the borehole inclination and is given by:

$$[T]_{hla}^{nev} = \begin{bmatrix} \cos I \cos A & -\sin A & \sin I \cos A \\ \cos I \sin A & \cos A & \sin I \sin A \\ -\sin I & 0 & \cos I \end{bmatrix}$$

### 19.2.8 Bringing It All Together

The effect of a particular **error source** on the survey results (md, inc or az) is found by multiplying the **error magnitude** by the appropriate **weighting function**. It is an implicit assumption of the model that all the error statistics are Gaussian (see section 19.3.4 on the MWD error model revisions for the one exception to this rule).

Furthermore, the error sources are assumed to be statistically independent of each other so the effects of the **different** error sources are summed by taking the square root of the sum of the squares (RSS). (N.B: this should not be confused with the effects of the **same** error source across different survey stations and survey legs.)

The effects of the error sources are all assumed to be linear (the weighting functions are all calculated to first order), so doubling the size of an error magnitude will in turn double the size of the error caused by that error source at any particular survey station. That error contribution will then be RSS'd with the other error sources, so that the effect on the final survey uncertainty will not be a simple doubling.

Then uncertainty in md, inc and az is converted to a positional uncertainty in the Earth-referenced co-ordinate frame. The equations for doing this are derived in [1] and are determined from the balanced tangential method of determining the borehole trajectory.

The positional values can then be converted to an uncertainty in the borehole referenced co-ordinate frame by multiplying by a direction cosine matrix dependant on the inclination and azimuth of the borehole.

The output of the error model is a covariance matrix describing the magnitude of the survey errors in the chosen co-ordinate frame. From this covariance matrix it is then possible to generate an error ellipse showing the estimated survey uncertainty in 3-d space. This error ellipse may be displayed in 3d or it may be sliced in a plane of interest, e.g. perpendicular to the well and displayed as an error ellipse. (Note to software implementers: this step is not given in the SPE paper but the axes of the error ellipsoid are the eigenvectors of the 3x3, real symmetric covariance matrix and the axes magnitudes are the eigenvalues of the covariance matrix.)

In the SPE paper the error sources are quoted at one standard deviation and hence the final error ellipse dimensions are the 1-sigma ellipse dimensions. There is then a probability that the actual well is contained with an ellipse of this size, centred on the obtained survey results. It is common practise in anti-collision calculations to use 2-sigma results – the 2-sigma ellipse is twice as large as the 1-sigma ellipse along each of the principle axes.

It is normal for directional drilling software such as 5D or Compass to be used to determine error values either for survey results for well planning or survey design. Usually the user can select whether results are reported at 1, 2 or 3 sigma. In some instances, the magnitudes of the error sources are always quoted at 1-sigma, in others the software allows the 2 sigma values to be entered. You should check with company anti-collision policy, survey focal point or software vendor if you are uncertain how reporting is applied to the wells which you use.

### **19.2.9 Bias Terms**

The error magnitudes discussed above are essentially the standard deviations of the range of values that error source can be expected to take. Many of these error sources will have zero mean and hence the standard deviation is all that is required.

However, the formulation of the model also allows for error sources which have a non-zero mean. These are known as bias terms and lead to error ellipses which not be centred on the survey point, but are offset in a particular direction.

The most obvious application for this would be for measured depth errors, where it is well known that drill pipe is measured on surface but when downhole expands with temperature and stretches under tension from the weight the drill-string. So the true measured depth will be longer than the sum of the drillpipe lengths on surface. However, after discussion at ISCWSA meetings, the committee took the view that biased models should are not encouraged. If biases are present these should be corrected where possible, and if not the error ellipses should be large enough to encompass the expected actual location of the wellbore.

## 19.3 MWD Error Model

### 19.3.1 MWD Tool Types

Most modern MWD tools are very similar and comprise six sensors - three orthogonal accelerometers to measure the inclination and toolface of the tool relative to the Earth's gravity vector and three orthogonal magnetometers to measure the azimuth of the tool.

### 19.3.2 MWD Error Sources

The MWD error sources were originally set out in [reference \[1\]](#). Although there have been subsequent revisions to the details of modelling the same basic physical errors still apply.

The original paper identified 34 error sources and at the current state of the model (revision 3) 41 separate MWD error sources have been identified. These can be split into five groups:

#### 1) Sensor errors (This gives a total of 26 MWD sensor error sources)

Bias and scalefactor terms are modelled for the accelerometer and magnetometers.

In the original derivation of the paper there was essentially one bias and one scalefactor term for each sensor, however that formulation of the mathematics required an estimate of the toolface angles which couldn't be reliably determined at the planning stage. The later revisions introduced toolface independent terms and now the effects of the x and y sensors are lumped together and are not explicitly separated out. For the biases there are still two terms for the x and y directions, however the scalefactors are now modelled using three error sources for these two axes.

So for standard MWD surveying there are 14 terms:

	Accelerometers	Magnetometers
<b>Bias</b>	2 xy-terms 1 z-term	2 xy-terms 1 z-term
<b>Scalefactor</b>	3 xy-terms 1 z-term	3 xy-terms 1 z-term

The model also covers the situation where an axial interference (or short-collar) correction is applied used to remove the axial effects of BHA magnetic interference. This changes the form of the MWD survey equations and hence the weighting functions and therefore needs to be modelled with a further set of sensor error sources. For axial interference corrections, the z-magnetometer reading is not used and hence a further 12 error sources are defined (14 – (z-mag-bias and z-mag-scalefactor)).

#### 2) Reference Field Errors (4 error sources)

All MWD survey results are measured relative to the Earth's magnetic field and uncertainty in this reference leads to survey errors. The magnitude and direction of the Earth's magnetic field is characterised by its total field strength, declination angle and dip angle and these values are normally obtained from a mathematical model, such as the IGRF or BGGM models, implemented in directional drilling software.

For standard MWD operations, only the declination is important. In order to give an accurate description of the declination uncertainty over the globe, the MWD paper models the declination error with a constant term and with a term which is inversely proportional to the horizontal component of the Earth's field.

When axial interference corrections are applied to MWD surveys, the reference total field and dip angle terms need to be considered and a further two error sources are identified for these.

#### 3) Interference Errors (2 error sources)

The BHA itself will generally be steel and will have a magnetic field associated with it. Even when non-magnetic drillpipe is built into the BHA, according to industry standard spacing calculations, there will still be a residual

effect on the survey results. This is modelled with two error terms, one for constant axial interference and one for direction dependent effects, since constant magnetic interference from the BHA will have an increasing effect on survey azimuth as the wellbore gets closer to a horizontal, magnetic east/west attitude.

#### 4) Misalignment errors (5 error sources)

Following some work done for the gyro error model, the misalignment of the survey tool to the wellbore is now modelled with four misalignment terms. A further term is used to account for sag – the deflection of the BHA under gravity, which leads to an inclination error since the centreline of the survey tool will not be orientated parallel to the borehole axis

#### 5) Depth errors (4 error sources)

A total of four error sources are used to model the errors in measured depth, due to both random and systematic errors, scale factor errors on the depths and drillpipe stretch under tension from the weight of the BHA.

In this modelling some physical error sources may be lumped together into one error source if in practise it is difficult or unnecessary to separate them. So for example, the misalignment error sources that are identified are for the misalignment of the tool itself to the borehole, not the sensors to the tool. The misalignment of the sensors themselves to the tool axes are accommodated within the sensor bias and scalefactors and are not explicitly separated out.

### 19.3.3 MWD Weighting Functions

As described in the example in section 19.2.4 the MWD weighting functions are determined by taking the partial derivatives of the survey equations with respect to the error sources. All of the MWD weighting functions are detailed in [Appendix B](#).

Even a quick glance shows that many of the weighting functions are zero. Of the total list of error sources, only the four depth terms have any influence on measured depth. Some of the functions such as the effect of the declination errors on azimuth or sag error on inclination are relatively simple equations. However, other sources such as the accelerometer error sources may influence both the inclination and azimuth measurements and, particularly in the azimuth case, lead to relatively complex equations to be evaluated at each survey station.

### 19.3.4 MWD Error Magnitudes

The MWD model is the only case for which the ISCWSA defines error magnitudes and provides complete tool models, if only for a limited number of situations. This is because it is considered that the performance of most modern MWD tools is quite similar and a generic model is valid.

Much of the MWD paper [1] is given over to a justification of error magnitudes for the MWD error sources and a complete tool models are given both standard MWD surveys and for surveys which are corrected for axial-interference for the combinations situation where the tools are run from a fixed land rig with fixed depths and for an offshore floating platform.

So effectively there are four defined tool models:

- i. MWD-Fixed Rig
- ii. MWD-Floating Platform
- iii. MWD + Axial Correction – Fixed Rig
- iv. MWD + Axial Correction – Floating Platform

The application of survey correction techniques to improve the accuracy of MWD surveys will generally change the magnitudes of one or two error sources. So for example, running sag-correction software will reduce the magnitude of the sag error term; conducting an IFR survey will improve the knowledge of the Earth's magnetic

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field and lead to reduced magnitudes for the four reference field error terms. The use of the error model as implemented in directional-drilling software is the appropriate way to evaluate the effect of these techniques and to determine an appropriate survey program for a well. However, the ISCWSA has not defined or standardised values to be used to model these.

### 19.3.5 Relative Contribution of the Various Error Terms

For the ISCWSA#1 test well (typical North Sea Extended reach well), the plots below show the relative contribution of the various error sources to the overall ellipse dimensions. The values below have been calculated based upon revision 2 of the MWD model. All the values here are quoted in Earth referenced (NEV) frame and it must be remembered that being independent the terms are summed by the RSS method.

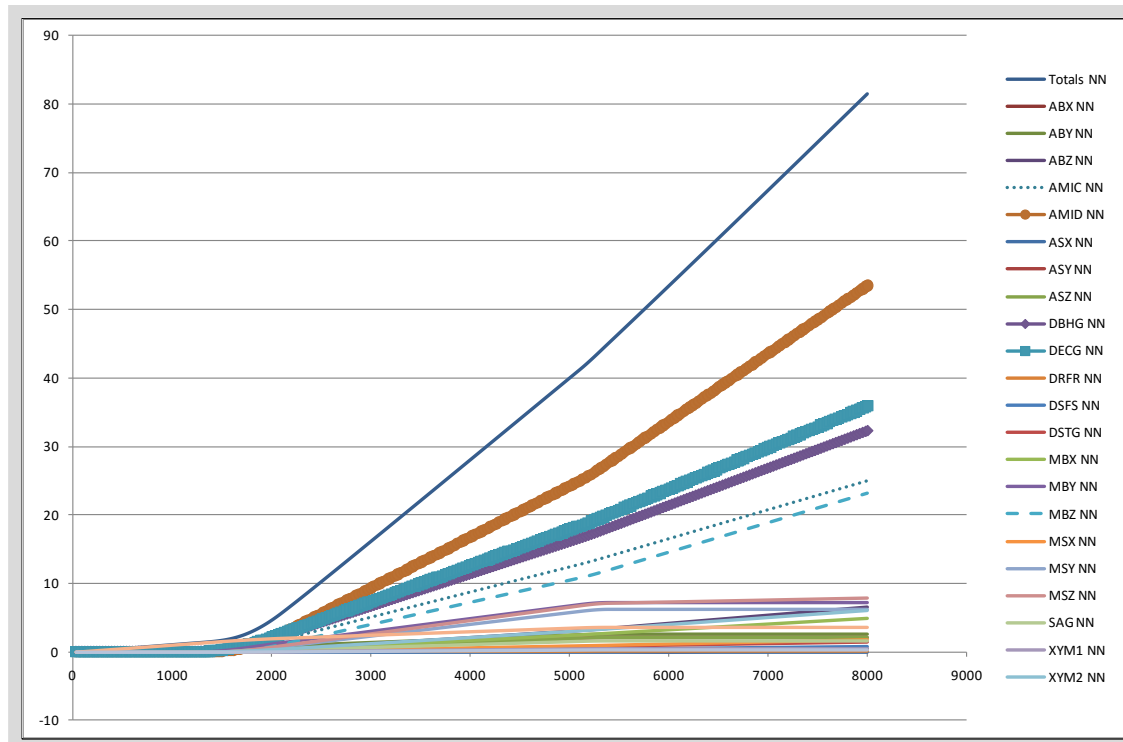


Figure 93: North Axis Errors

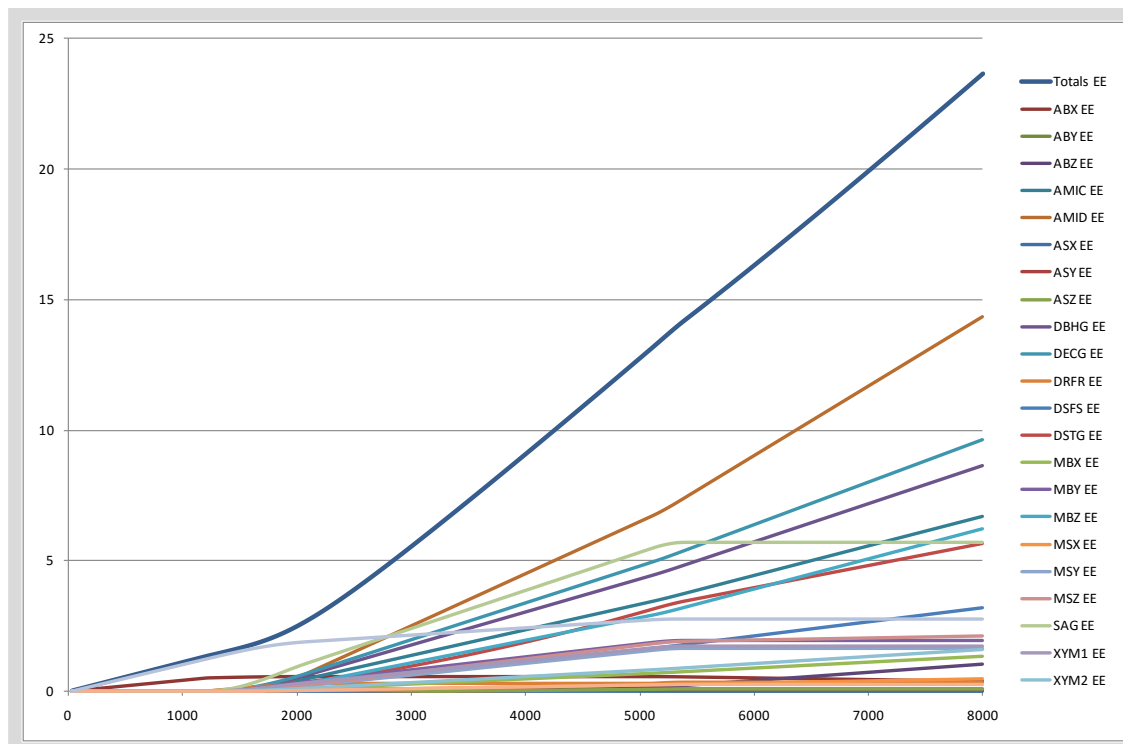


Figure 94: East Axis Errors

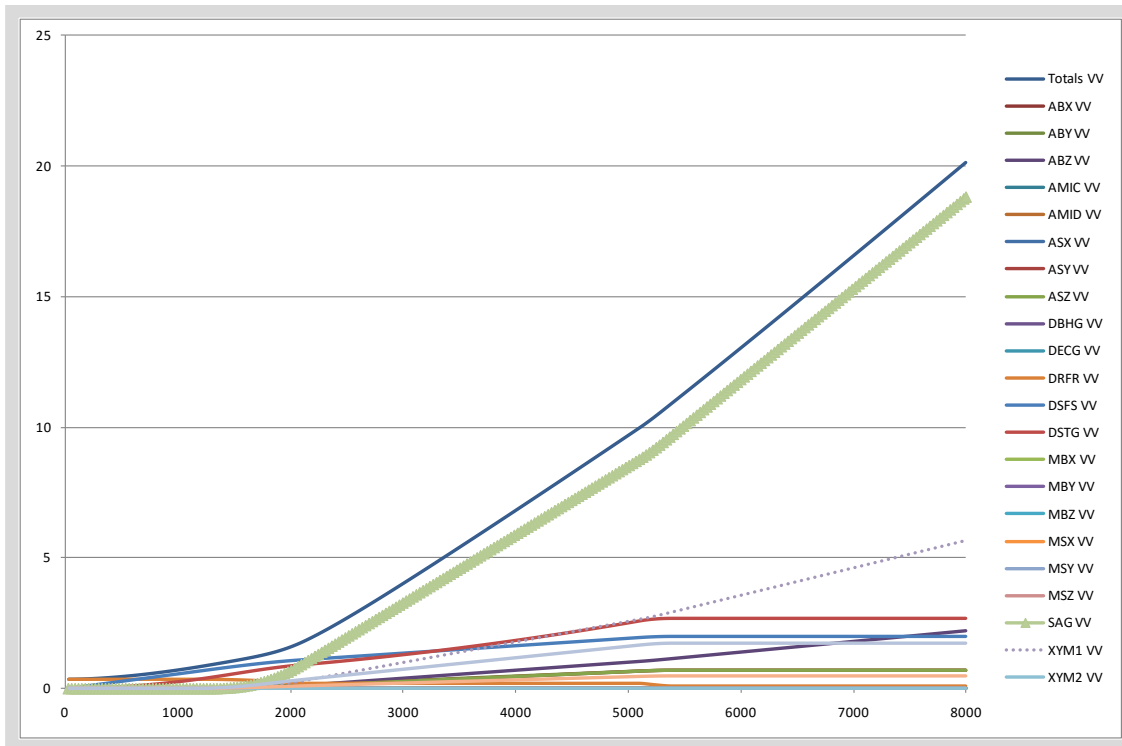


Figure 95: Vertical Axis Errors

From these graphs it is easy to see that as expected, the biggest error contribution in the vertical is from SAG. For this well the north and east errors are dominated by axial interference, followed by uncertainty in the magnetic model (i.e. declination uncertainty).

### 19.3.6 Revisions to the MWD Error Model

The reprinted MWD paper [1] by Hugh Williamson covers three distinct areas. It lays out the framework of the ISCWSA error model as discussed in the previous section, it defines the error sources applicable to MWD tools and it provides error magnitudes for these values, complete with a technical justification.

However, work on the ISCWSA error models is on-going and to date several revisions have been made to the basic model as defined in [1]. A summary of the revisions is presented here. More details can be found in [4,5,6].

The revisions to the MWD Error Model are:

<b>Rev 0</b>	As per SPE 67616 together with a number of typographical corrections [4]
<b>Rev 1</b>	Changed to the gyro style misalignment with 4 terms and calculation options [4]
<b>Rev 2</b>	Changes to the parameter values for the depth scale and stretch terms [4]
<b>Rev 3</b>	Replacement of all toolface dependant terms. [5]
<b>Rev 4</b>	Look up table for BGGM uncertainties. [6]

Revisions 0 and 2 make some relatively minor corrections and changes to the original paper. However, revisions 1 and 3 are more major and replace all if the toolface dependant terms misalignments. Combined these constitute a large change to the model. Between them these two revisions replace 18 of the original 33 weighting functions, including the misalignment terms, the x and y axis sensor biases and scalefactors. 24 new sources are added to model these.

Revision 0 consists of some relatively minor typographical and parameters corrections.



Revision 1 introduces a new method of calculating the effect of tool misalignment to the borehole axis. This avoids the complication of toolface dependency in the misalignments and is considered to handle certain geometries, such helix-shaped, vertical boreholes better than the original MWD terms. This replaces the two existing misalignment terms MX and MY and introduces four new terms and three possible calculation options which are handled via two weight parameters.

The calculation options are:

	$W_{12}$	$W_{34}$
<b>Alternative 1</b>	1	0
<b>Alternative 2</b>	0	1
<b>Alternative 3</b>	<i>sinI</i>	<i>cosI</i>

Alternatives 1 and 2 have their own strengths and weaknesses, whereas Alternative 3 is designed to combine the best of both options and is the preferred calculation option. This is discussed in detail in Appendix B of [2] and in [4].

Revision 2 makes some corrections to the depth error magnitudes.

Revision 3 replaced the remaining 16 toolface dependant weighting functions with 20 new ones, following a method developed for the gyro error model. This removes the need to either include survey toolfaces, or use methods to evaluate at the planning stage which toolfaces might be observed, a process which can give rise to unexpected results. The new terms replace all the existing x and y accelerometer and x and y magnetometer bias and scalefactor terms, for both the standard MWD and MWD with Axial correction cases. The new terms lump together the x and y effects, and the propagation mode varies from either random, where the toolface varies between survey stations and systematic for sliding between survey stations with constant toolface. In practise for MWD the random propagation would normally be considered at the planning stage. The details of revision 3 are dealt with in [5].

Revision 4 brings in lookup tables for the uncertainty in the BGGM model which will change how the error magnitudes are determined for the reference field terms. This revision does not may any changes to the weighting functions.

As discussed in section 19.2.3, the error model assumes that all the errors are Gaussian. However, as [detailed in \[6\]](#) it has come to light that the errors in the global geomagnetic models are in fact, non-Gaussian and are best modelled with a Laplacian distribution which has greater likelihood in the tails of the distribution. This presents some problems in the implementation, especially when varying the number of standard deviations at which to report the output results.

The current recommendation is to define in advance the number of standard deviations required for output and then determine the uncertainty in the magnetic model at that confidence level. Divide this value by the number of standard deviation required to get an 'equivalent Gaussian standard deviation' (valid only at the confidence level in question) and then use that value as normal in the subsequent calculations.

**Although revision 4 has been approved by the ISCWSA, there is still on-going discussion on this point. The appearance of new global magnetic models may lead to further changes in this part of the model.**

## 19.4 Gyro Error Model

### 19.4.1 Gyro Tool Types and Running Modes

Whereas we considered that all MWD tools were essentially the same and comprised three orthogonal accelerometers and three orthogonal gyroscopes, there are many different types of gyro survey tool and many different ways of running them in a well.

The running modes can broadly be divided into tools which take measurements whilst stationary at regular survey stations and those which run into hole, whilst constantly moving and recording data. Furthermore, a gyro tool may include three orthogonal accelerometers and three orthogonal gyros or might only use a subset of sensors. Tools with additional redundant sensors can be reflected in the error magnitudes assigned rather than in the model mathematics.

So the gyro model covers tools which have:

1. x-y-z accelerometers - run in stationary or continuous mode
2. x-y only accelerometers – run in stationary or continuous mode
3. x-y-z gyros - run in stationary mode
4. x-y gyros only – run in stationary mode
5. x-y-z gyros - run in continuous mode
6. x-y gyros only – run in continuous mode
7. z gyro only – run in continuous mode

In addition, the model considers these other running conditions:

8. initialisation to an external sighting reference
9. indexing in hole to remove gyro drifts
10. rotation in hole
11. the cant angle of the sensors in x-y accelerometers systems.

Furthermore, the survey mode may vary within a survey run, as a function of inclination.

### 19.4.2 Gyro Error Sources

Due to the number of tool variations and running modes, the gyro error model is more complicated than the MWD model. However, it is based on exactly the same framework for propagation, summation and transformation as the MWD model.

The gyro model contains 48 error sources. 39 of these are new and 9 are common to the latest revision of the MWD model. As before sensor errors are very prevalent.

Accelerometer biases and scalefactors and sensor misalignments are present, and these only effect inclination terms, but different error sources have been identified for tool configurations which have a full orthogonal tri-axial set of accelerometers and for tools with only x and y accelerometers, which may be canted relative to each other and not perpendicular.

For the gyros, bias, random noise, gravity dependant errors, scalefactor errors and sensor misalignment with the tool have all been identified. With suitable selection of error magnitudes, it is considered that the model is sufficient to model the various types of mechanical spinning wheel gyros in use, both single and dual axes systems, ring-laser gyros and possible future gyro systems.

The gyro sensor errors affect the azimuth measurements, but now different functions apply depending on whether the gyro operates in a stationary, gyro compassing mode at each survey station or is initialised and runs continuously in the hole. In addition, the model accommodates xyz; xy and z-only gyro systems.

For the continuous gyro systems, a new complication arises in that some of the errors will be dependent on elapsed time in the run (gyro drift errors) or the square root of elapsed time (random walk errors). These have been modelled by including a running speed in the tool model and including a term in the weighting functions which will accumulate over time. Terms for errors introduced with an external azimuth reference are also included.

From the outset, the gyro model excludes the need for toolface in any of the terms used. To do this the x and y effects are lumped together. For surveys where the tool is rotated between surveys these terms will propagate randomly, however when the tool slides between stations with fixed toolface, these same terms will propagate systematically.

The gyro error model introduced a new method of calculating the effect of tool misalignment to the borehole. This was later incorporated in to the MWD model and is described in section 19.3.2.

### 19.4.3 Gyro Weighting Functions

The gyro model weighting functions are detailed in [Appendix C](#). They are separated out more rigidly than the MWD model and aside from the misalignment terms, any given error source only effects one of the survey measurements. Hence two of the error function vector terms are zero for all except the misalignments.

### 19.4.4 Gyro Error Magnitudes

The gyro paper defines error magnitudes for six example error models. However, these are intended to be used only for testing and are not to be considered as representative of any given tool used in the industry.

### 19.4.5 Differences Between the Gyro and MWD Models

The gyro error model is essentially a superset of the MWD model. It uses the same framework for prorogation error sources, but naturally since the physics behind the tools are different, the error sources and weighting functions for the gyro error model are quite different to the MWD model.

The gyro error model uses the method of handling borehole misalignment, introduced into the MWD model as revision 1 and described in the MWD model section above.

But there are three main changes which introduced with the gyro model. Firstly, the tool running mode and hence the error sources in use, may change along the wellbore as a function of inclination. So the tool model must include inclination bounds, either for the possible running modes into which the error sources are grouped in [2] or simply for each individual error source and the software must accommodate these.

Secondly, in the MWD model the weighting functions remain fixed from survey station to station. However, for the continuous gyro operating modes there are time dependent terms in the weighting functions, which are modelled as depth dependant and which will increment as the tool moves along the wellbore. So the software must initialise these and then implement the changes as it propagates the model. All six continuous gyro azimuth error sources have this property (gyro drift and random walk terms for the three continuous gyro sensor combinations, xyz, xy and z: GXYZ-GD, GXYZ-GRW, GXY-GD, GXY-GRW, GZ-GD, GZ-GRW).

Finally, for MWD the tool model need only define which error sources are used to model a tool, the magnitudes of these error sources and their propagation modes. In the gyro model, some additional parameter values may be needed to define details of the running conditions;

- a) a cant angle for x-y accelerometer systems
- b) a logical operator indicating whether or not accelerometer switching is implemented.

- c) a logical operator indicating whether or not the tool is indexed (z-rotated) at a survey station
- d) a logical operator defining whether or not a stationary tool is rotated between stations, which will change the propagation mode for some bias terms

The latter two terms can also be accommodated either by correctly defining the error magnitude for the appropriate term to zero or by excluding these terms from the tool model, unless the values change with inclination.

## 19.5 Error Model Implementation

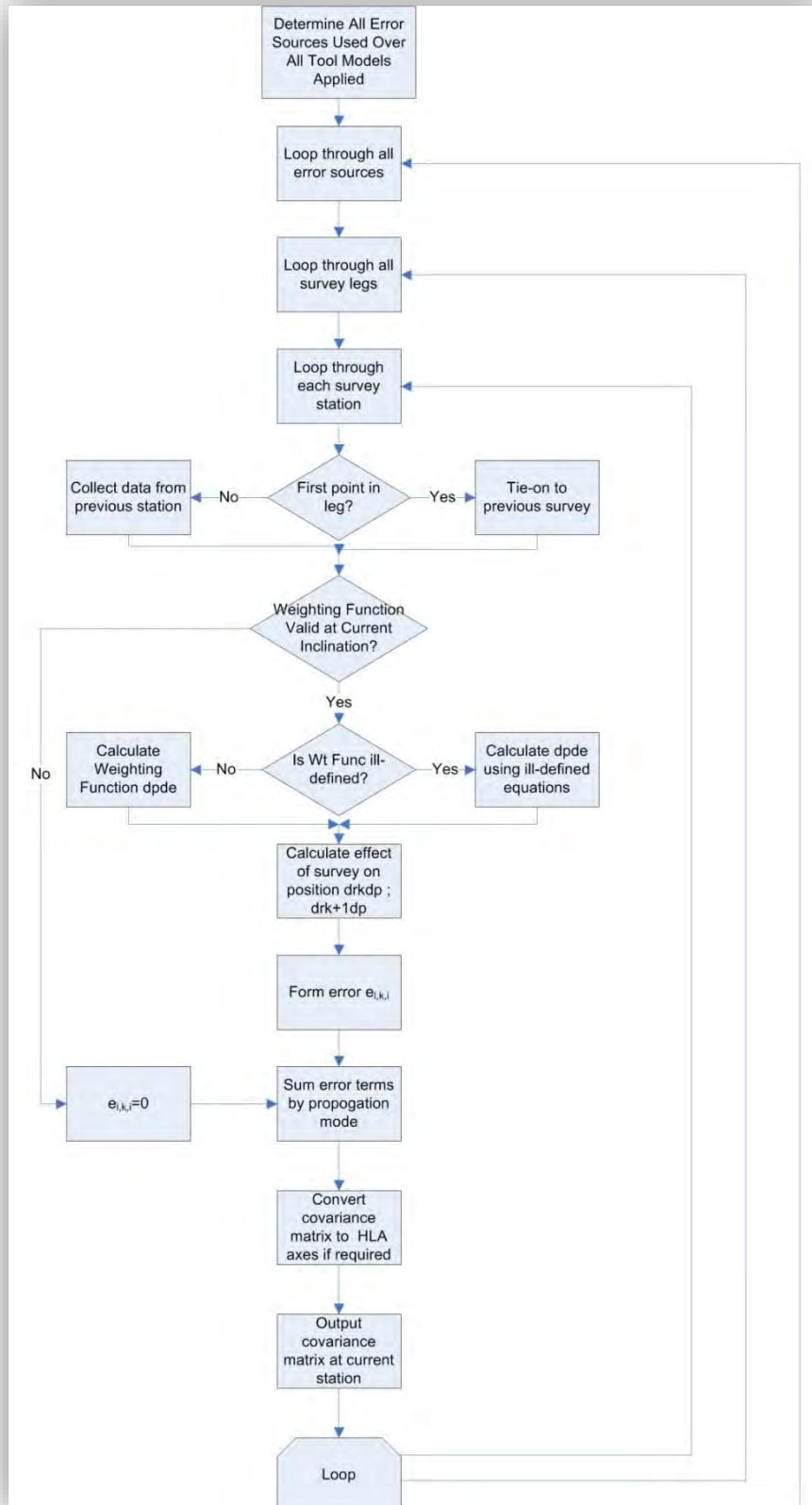
### 19.5.1 Algorithm Flow

The basic flow of the models is;

- Initialise
- Loop through error sources
- Loop through survey legs
- Handle tie -on
- Loop through survey stations
- Use inclination to define mode (for gyro)
- Determine inc, az, depth error for each error source i.e. evaluate the weighting functions
- Determine the NEV errors for each error source
- Sum these according to propagation mode
- Transform to HLA axis frame if required.

### 19.5.2 High Level Flow Chart

The chart below shows a high level overview of the dataflow for the model in general. Two other flow charts are provided in the gyro model paper [2] which give more specifics of detailed decision processes.



### 19.5.3 Inputs Required

Required input parameters for the weighting functions calculations:

#### Well site data:

Total gravity value  
 Total magnetic field value (MWD)  
 Magnetic Dip (MWD)  
 Horizontal magnetic field (function of total field and dip) (MWD)  
 Latitude (Gyro)

#### Survey data at each station:

Measured depth, Inclination, Azimuth, Toolface (early revisions)

#### Tool Model Terms:

Error sources included  
 Error magnitude for each source  
 Error propagation mode  
 Inclination bounds for change for mode or for each source (start, end)  
 Misalignment calculation method (ALT=1,2,3)  
 External reference method (gyro)  
 Running Speed (gyro)  
 Rotation of accelerometers between stations (R value, gyro)  
 Cant angle (gyro)  
 Running mode (sliding or rotating must be defined, either via IPM or as a parameter to control propagation modes.)  
 Noise reduction factor at initialisations  
 Minimum distance between initialisations

### 19.5.4 Poorly Defined Functions

The MWD model includes a set of equations for the cases where the weighting functions are mathematically ill-defined in vertical hole. The situation at 90 inclinations, 90 (or 270) azimuth is physically ill defined and a software implementation must handle these.

The following weighting functions are ill-defined in vertical hole:

ABX, ABIX, ABY, ABIY, MX, MY, XYM3, XYM4, ABXY-TI2 and ABIXY-TI2

References [1] and [5] include alternative calculation options that can be used to evaluate these functions.

### 19.5.5 Test Cases

The MWD paper [1] defines three standard test well profiles. These are for:

- a. an example North Sea extended reach well,
- b. a Gulf of Mexico fish-hook well,
- c. a Bass Strait designer well.

For each test case the well profile, location, magnitude and direction of the Earth's magnetic field and the units (m or ft) are defined.

The MWD paper then defines seven test cases and error model results for each test case at Revision 0. The gyro paper defines six gyro models and applies each model to the same three test well profiles. The gyro paper also defines acceptance criteria as having numerical agreement to within  $\pm 1\%$  of the results in the paper.



### 19.5.6 Consistent Naming of Error Sources

An attempt has been made to agree and utilise consistent naming conventions for error sources. Further details can be found in the Error Model Standardisation page of the ISCWSA website, [www.iscwsa.org](http://www.iscwsa.org).

This naming convention has been used in this document, however it should be noted that same weighting functions should be preceded with the suffix, S, G, W or R depending on the associated propagation mode.

When designing a software implementation, the decision as to be made whether or not the propagation mode is tied directly to the error codes, or whether the propagation mode is defined in with the specific tool model. The latter case allows more flexibility to the aware user when creating tool models.

### 19.5.7 Backward Compatibility

At each successive revision, the ISCWSA has generally advocated that the most current revision of the MWD model is promoted and should be used. In practise, software implementations have lagged behind updates of the model and also certain companies have made a conscious decision not to move to the latest versions. Therefore, a range of versions of the ISCWSA model can be found in the industry.

If starting from scratch, there is no reason why an implementer could not go directly to the most current version of the model and ignore the history that goes before. However, in practise of the basic framework of the model is incorporated then the overhead in adding the additional depreciated weighting functions is not too great. There may be an advantage in the flexibility to allow older versions of the model to be evaluated or accommodate.

## 19.6 Standardisation

### 19.6.1 Why Do My Standard ISCWSA Results Not Agree with Yours?

A common concern voiced by users of the ISCWSA error model is that the results that when they compare error ellipse values from different directional drilling software packages, they get different answers. In general, the immediate reaction is that one package must be wrong. However, the ISCWSA models leave a number of decisions up to either the user or software implementer and these should be taken into account when comparing results. See [reference \[7\]](#) for a fuller discussion on this topic.

*What confidence limits are being reported?*

The models make no comment on what confidence limit (number of standard deviations, sigma level) results should be given too. This is typically a user defined option in the software and values of 1, 2, 2.79 and 3 are all commonly used in the industry.

*What co-ordinate system are ellipse dimensions reported in?*

An error report may simply specify semi-major axes or semi-minor axis without detailing which co-ordinate system is being considered. Typically, the results can be in North-East-Vertical or Highside-Lateral-Alonghole axis. Some packages can output in only one or the other axis systems, other packages allow the user to select which ones are used.

*What value is being reported?*

Typically, a package will output semi-major axis and semi-minor axis. In some cases, (particularly TVD spread) it is 2 x semi-minor axis that is output (semi-diameter?).

*What revision of the error model is implemented?*

As detailed in the MWD section there have been a number of successive revisions of the MWD model and not all software packages will be at the same revision level.

*What error magnitudes are being used in the tool model?*

In general, the ISCWSA does not standardise or define the tool models to be used. It is only the mathematics that is standardised and it is left up to the survey contractor to supply appropriate tool models. The only exception is the ISCWSA has standardised on tool models for standard MWD and MWD with Axial Interference corrections. In other cases, the tool model comes supplied with directional package or can be edited by the user. Sadly, it is not uncommon to come across survey databases in use with tool models containing a very reduced set of error sources (or equivalently all the magnitudes set to zero.)

### **19.6.2 Non Standard Error Sources**

All the error sources and weighting functions defined in the three ISCWSA error model papers and associated updates on the ISCWSA website have been listed in this document.

In addition, a number of other error sources are sometimes used within the framework of the ISCWSA model, such as Wolff and deWardt [8] terms and terms for other historic survey tools. Doing this is not exactly the same as implementing the Wolff and deWardt model as detailed in their paper, but is rather a halfway house between the two error models which may agree for some situations and may give very different answers in other circumstances.

***No attempt has been made in this document to list any non-ISCWSA standard error sources. It has been recognised that a great deal of time can be lost when checking and migrating survey databases from one system to another and trying to map across historic survey tools. It is hoped in future that it may be possible to agree on some generic toolset to minimise these problems.***



**CONTENTS**

## 20. Anti-collision Techniques

*This section deals with the survey aspects of Anti-collision monitoring and does not venture into the various mitigation methods such as the use of jetting or non-aggressive bits to minimise the impact of collision. There are techniques available to monitor the proximity of adjacent wells by measuring the external magnetic interference from nearby casing but these are beyond the scope of this document.*

### 20.1 Minimum Separation Methods and Limits

The point in an adjacent well at which minimum separation occurs is where the separation vector hits the well at right angles. This is determined by conducting a 3D closest approach scan from the planned well. Relics of early well planning software are scans that can be done either at right angles or in horizontal planes from the planned well. Both of these alternatives should be avoided as they do not represent the true geometrical separation between the wells. Figure 84 illustrates this fact. In particular, scanning at right angles to the well bore can completely miss a vertical appraisal well when drilling horizontally. Best policy is that only 3D closest approach will be used for the definitive anti-collision report. Clients may also require horizontal or perpendicular scans to use in matching against their checking software.

### 20.2 Definition of Separation Factor

There are three main methods of defining the separation factor and depending on how it is defined, the results change. Also, since the separation factor is always calculated in the plane determined by the scanning method, the scanning method also obviously can change the results. The older methods of scanning will calculate the separation factor along a plane either perpendicular or horizontal to the primary well path. Again, best policy is to use 3D closest approach scanning so that the shortest distance is seen.

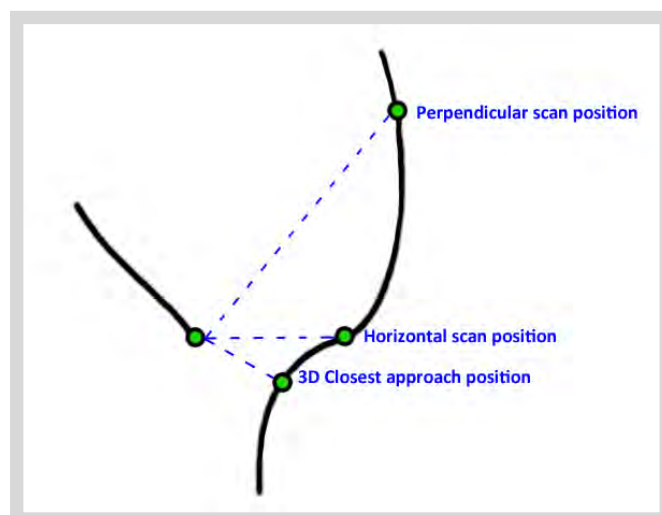


Figure 96: Separation Factor

## 20.3 Separation Vector Method

The separation vector method of calculating separation factor is shown in figure 97. (Note that in all these figures you are looking at the plane of the scan with the well bore centres and zones of uncertainty shown as they plot in that plane).

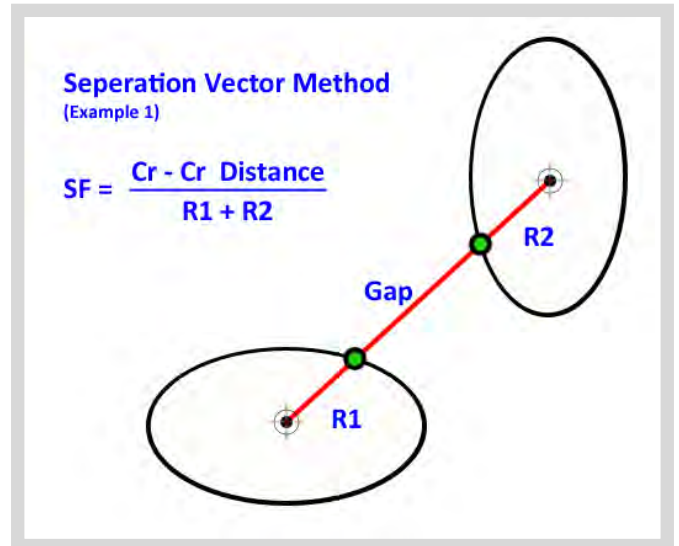
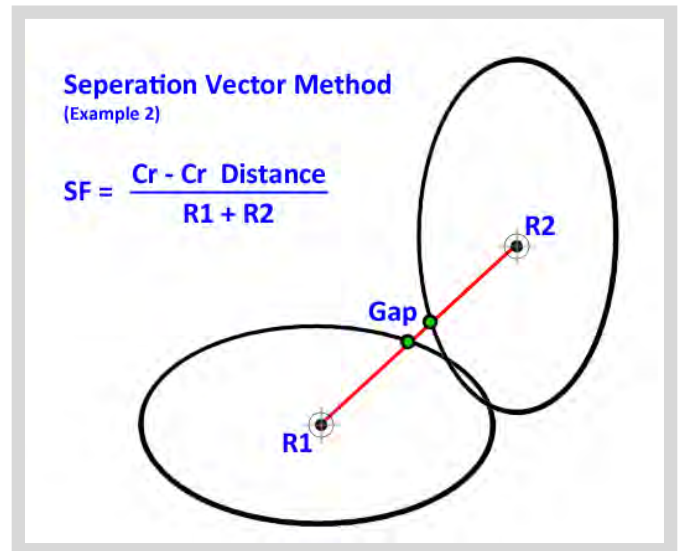


Figure 97: Separation vector method

This has the disadvantage that it can be optimistic. In a worst case scenario, it can even miss a potential collision situation as in figure 98. This represents the same target and planned well as in the above example but the conditions have varied such that the lateral uncertainty is now much larger.



### 20.4 Pedal Curve Method

The second method for calculating separation factor is the pedal curve method. This overcomes the previous problem by projecting the extremities of the ellipses onto the separation vector.

Figure 98: Separation vector method

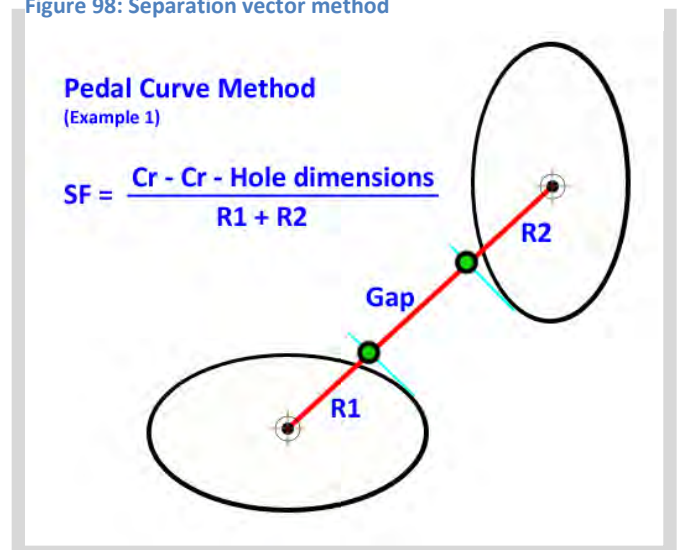


Figure 99: Separation factor – pedal curve method

However, whereas the separation vector method can be too optimistic, this one has the opposite problem of sometimes being too pessimistic. In figure 100 the two wells are crossing safely in 3D space but using this method calculates a collision risk when in fact there is not one.

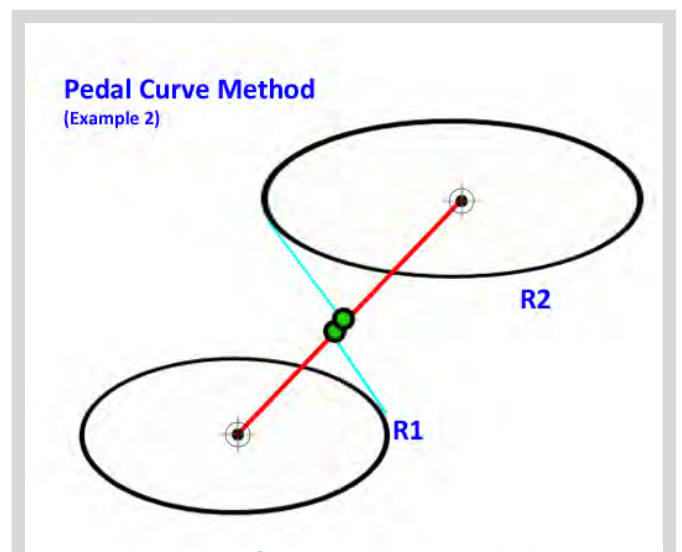


Figure 100: Separation factor – pedal curve method

## 20.5 Scalar (Expansion) Method

A third method is the scalar or expansion method. This method calculates the amount the uncertainty ellipses must be expanded or contracted (in cases where the ellipses overlap) in order to just meet. The separation factor is simply the factor by which the ellipses are expanded or contracted. The calculations required to generate the separation factor using the scalar method are best left to the computer.

In the example the green ellipses are 40% bigger than the originals so the separation factor would be 1.4. When the geometries line up correctly this method produces the same number as the alternative methods. The same safety rules developed for use with the older methods can still be used. But the scalar method has the advantage of never calculating optimistic or pessimistic separation factors no matter what the 3D geometry.

This method produces numbers which are very similar to the other two methods and can be used with the same safety rules but it is never optimistic or pessimistic in any geometry.

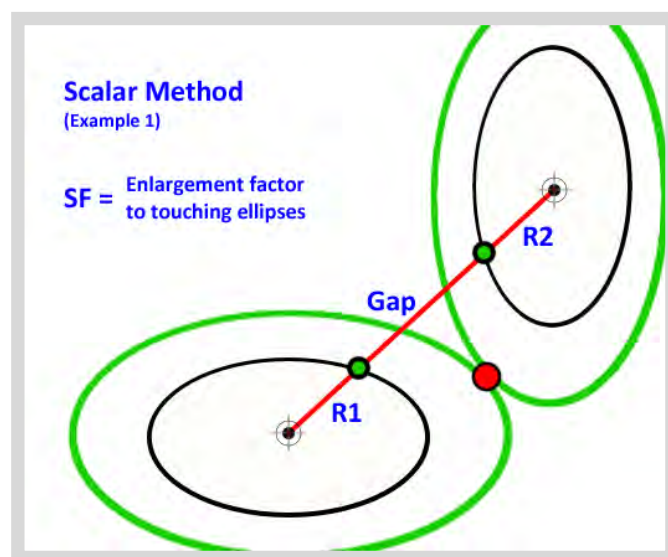


Figure 101: Scalar (expansion) method

## 20.6 Probability of Collision

There is a movement in the industry towards more probability based anti-collision reporting. As of April, 2012 there is no final recommendation from the SPE technical section (ISWASA) on this. At present this section will present information on collision probabilities and their calculation.

### 20.6.1 Difference between Separation Factor and Probability Based Rules

A separation factor based rule is purely geometric whereas a probability based rule relates to actual risk. For example, take two different uncertainty situations which both calculate a separation factor of 1.0. In the first case two 12-1/4" wellbores have uncertainty envelopes which are hundreds of feet across. In the second case the uncertainty envelopes only have a radius of one foot from each well centre. Clearly the second case has a much higher probability of being an actual collision than the former.

Rules merely using reported separation factor numbers will not distinguish between these two cases.

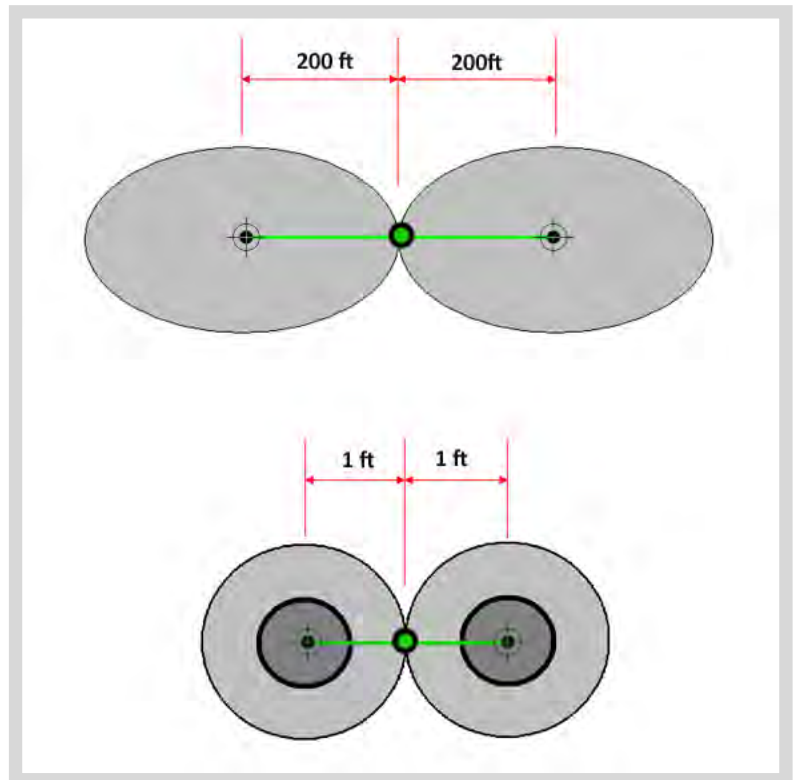


Figure 102: The uncertainty envelopes for two calculation methods



## 20.7 Acceptable Risk of Collision

A key barrier to adopting probability based rules is defining what number represents an acceptable risk. Until industry standards are developed (currently under consideration in the ISCWSA) clients are unlikely to require reporting based on probability based rules.

## 20.8 A Simplified Calculation of Probability of Collision

A second key barrier to adopting probability based rules is that calculating the actual probability of collision is a difficult problem that requires a huge 'Monte Carlo' analysis that would tax the capabilities of standard computing systems.

This is a further advantage of the scalar factor method for calculating separation factor. It can translate easily into a close approximation of the probability of intersection (actual collision) using the following process:

1. Calculate the Radius Factor for the two wells
  - a.  $Rf1 = \text{semi-major axis 1} \times \text{semi-minor axis 1} / \text{hole 1 radius squared}$
  - b.  $Rf2 = \text{semi-major axis 2} \times \text{semi-minor axis 2} / \text{hole 2 radius squared}$
  - c.  $RF = \text{square root of } (RF1 \times RF2)$
2. Calculate the number of standard deviations at which the ellipses touch
  - a. If the SF by expansion was based on 1 sigma then  $T = SF$
  - b. If the SF by Expansion was based on n sigma then  $T = n \times SF$
3. Calculate the following simple components
  - a.  $S = T \times 30$       S is an angle in degrees that can be used in the following fit model
  - b.  $\text{Index} = 7 \times (1 + \text{Cos}(S))$
  - c.  $CR = e^{\text{Index}}$       E is the base for natural logarithms (2.718282)
  - d. Collision Risk per million is  $CR / RF$

### Warning:

This formula only gives a good estimate of collision risk in the range from SF = 0 to SF = 3 at 2 sigma. Collisions are very rare indeed beyond this (6 standard deviations apart). Do not use this formula outside this range or collision risk will be over-estimated.

It should be noted that this calculation is the probability of the centre points of the ellipses colliding. It does not represent the complex probabilities of two curved well paths colliding in 3D space but serves as a useful guide. The table on the following page gives an idea of what you could expect to see:

## Separation Factor

Radius Factor	RF \ SF	0.25	0.5	0.75	1	1.25	1.5	1.75	2
10	94740	47079	15478	3632	671	110	18	3	
20	47370	23540	7739	1816	336	55	9	2	
30	31580	15693	5159	1211	224	37	6	1	
40	23685	11770	3869	908	168	27	4	1	
50	18948	9416	3096	726	134	22	4	1	
60	15790	7847	2580	605	112	18	3	1	
70	13534	6726	2211	519	96	16	3	0	
80	11843	5885	1935	454	84	14	2	0	
90	10527	5231	1720	404	75	12	2	0	
100	9474	4708	1548	363	67	11	2	0	
110	8613	4280	1407	330	61	10	2	0	
120	7895	3923	1290	303	56	9	1	0	
130	7288	3621	1191	279	52	8	1	0	
140	6767	3363	1106	259	48	8	1	0	
150	6316	3139	1032	242	45	7	1	0	
160	5921	2942	967	227	42	7	1	0	
170	5573	2769	910	214	39	6	1	0	
180	5263	2616	860	202	37	6	1	0	
190	4986	2478	815	191	35	6	1	0	
200	4737	2354	774	182	34	5	1	0	

Figure 103: Collision probability table

## 20.9 Anti-collision Scanning and Reporting

Recommended practice is to observe the following rules when scanning wells for collision risk against a subject well;

1. On first pass, scan all wells in the field.
2. Be sure to pick up all the potential hazard wells.
3. Be sure to include plugged and abandoned wells, appraisal wells, wells drilled by other operators and wells drilled by other directional drilling companies.
4. Scan all wells to all depths at a close interval (30 ft or 10 m).
5. Document that you have checked with the client and they have verified that your database contains the same number of wells located in the same locations as their database.
6. Check that the hazard wells highlighted present no surprises to the client.
7. Thereafter scan reports may be done filtering on separation factor  $\leq 4.0$ .

## 20.10 The Ellipse of Uncertainty Report

The ellipse of uncertainty report required can vary from customer to customer. Terms can vary in their usage from customer to customer and from software to software. There are certain terms that must be understood. Any ambiguity arising due to customer usage or from other software programs must be understood and dealt with so as to prevent poor well planning and accidents in execution.

Below is an example of a deep, close approach report. The table following the example presents definitions of terms commonly used in ellipse of uncertainty reporting.

Easting (m)	Northing (m)	TVD (m)	Inc	Az	MD (m)	Semi Major (m)	Semi Minor (m)	PHI	TVD Spread (m)	N'rest Well	Cr-Cr (m)	Sep Factor	Inter B'dary (m)	Hi-Side to Cr-Cr	Survey Tool
224258.31	9237705.59	1519.63	82.78	273.49	1920.00	6.46	2.57	5.16	4.86	Alpha 1 (s)	127.53	28.68	123.08	47.51	MWD
224228.61	9237707.40	1523.39	82.78	273.49	1950.00	6.82	2.68	7.59	5.06	Alpha 1 (s)	98.11	21.71	93.59	34.95	MWD
224198.90	9237709.21	1527.16	82.78	273.49	1980.00	7.19	2.78	9.75	5.25	Alpha 1 (s)	68.99	14.77	64.32	64.06	MWD
224169.19	9237711.02	1530.93	82.78	273.49	2010.00	7.56	2.88	11.67	5.44	Alpha 1 (s)	40.83	7.88	35.65	74.85	MWD
224139.48	9237712.84	1534.70	82.78	273.49	2040.00	7.93	2.99	13.38	5.64	Alpha 1 (s)	18.61	1.79	8.24	86.90	MWD
224109.78	9237714.65	1538.47	82.78	273.49	2070.00	8.30	3.09	14.89	5.84	Alpha 1 (s)	28.24	6.84	24.11	99.26	MWD
224080.07	9237716.46	1542.23	82.78	273.49	2100.00	8.67	3.19	16.23	6.05	Alpha 1 (s)	54.96	13.36	50.84	110.85	MWD

Figure 104: Example of a deep, close approach report

Header Label-Expanded Header (Term)-Definition

Easting (m)	interpolated E-W map coordinate (in specified units) of the primary well
Northing (m)	interpolated N-S map coordinate (in specified units) of the primary well
TVD True Vertical Depth (m)	the true vertical depth (in specified units) of the centre of the primary well
Inc Inclinaton	the inclination vector direction of the centre of the primary well
Az Azimuth	the azimuth vector direction of the centre of the primary well
MD (m) Measured Depth (m)	the measured depth (in specified units) of the centre of the primary well
Semi Major (m)	the length (in specified units) of the longest uncertainty axis as seen looking along the centre of the primary well. (be aware that in other software it can mean the longest axis in 3D space or the longest axis in the horizontal plane. The differences are usually small.
Semi Minor (m)	the length (in specified units) of the axis at right angles to the semi major axis in whatever plane of projection is used.
PHI Phi Angle (Orientation)	the orientation of the semi minor axis from high side
TVD Spread (m)	the TVD (in specified units) occupied by the uncertainty envelope
N'rest Well Nearest Well	the name of the closest well at this point
Cr-Cr (m) Centre-Centre Distance	the distance (in specified units) from the centre of the primary well path to the centre of the nearest well's path
Sep Factor	Separation Factor - the separation factor calculated by the specified method
Inter b'dary (m) Inter Boundary Dist	the distance (in specified units) from the boundary of the uncertainty surface of the primary well to the boundary of the uncertainty surface of the nearest well measured along the direction of 3D closest approach
Hi-Side to Cr-Cr	the orientation of the nearest well to the primary well expressed as an angle from high side of the primary well
Survey Tool	the current survey tool being used in the primary well

## 20.11 Safe Scanning Intervals

It is normally not productive to scan and report an entire well plan on a very fine grained interval. A normal practice is to scan the entire well at a rather coarse level and then examine the report for areas that will require finer scanning intervals. For example, the report above was generated using 30 m intervals. Examining this report, you should see the separation factor approaching an important value at 2040 m. When an approach is seen like this it is important to make sure that you also scan at finer resolution to make sure you catch the real closest point.

In the graphic example below a fine scanning interval has been selected and the 'tie lines' from a proposed horizontal well (blue) passing a vertical appraisal well (red) can be seen in the picture. Had a perpendicular plane scanning method been used on either well, the collision point may not have been picked up.

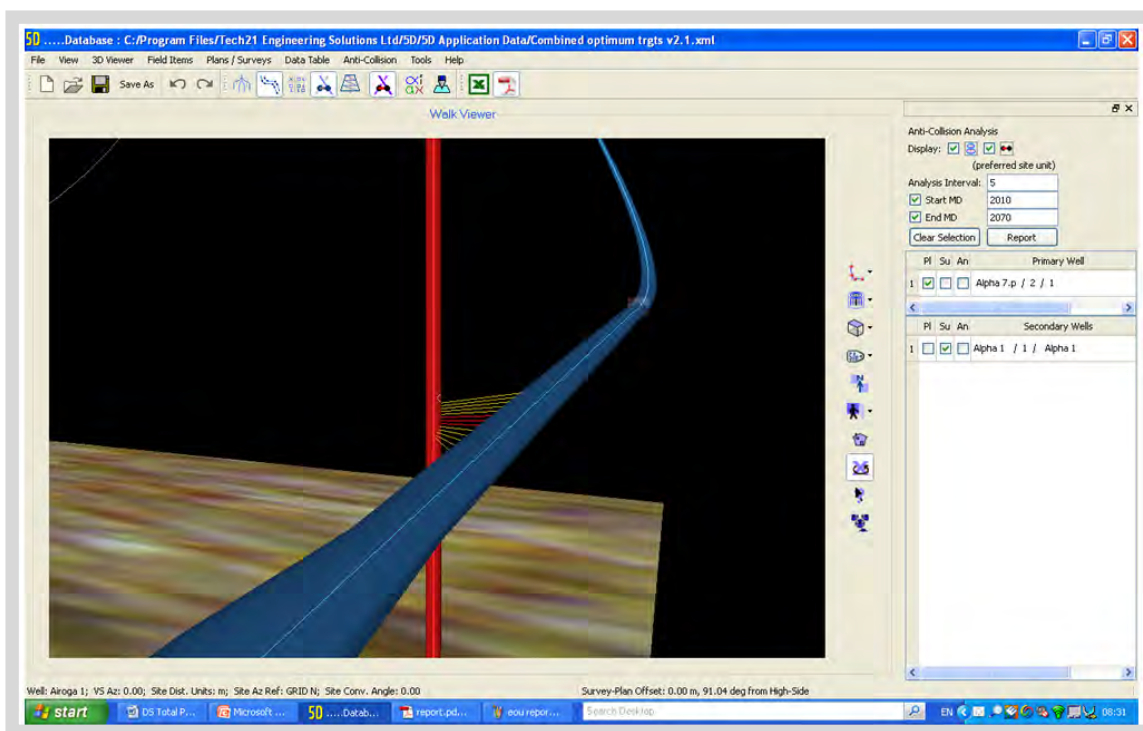


Figure 105: Fine scanning interval graphic

This produces the report below (figure 106) and it can be seen that in this case the close approach point occurred between 2035 and 2045 meters.

Primary Well : alpha 7.p (p)															
Easting (m)	Northing (m)	TVD (m)	Inc	Az	MD (m)	Semi Major (m)	Semi Minor (m)	PHI	TVD Spread (m)	N rest Well	Cr-Cr (m)	Sep Factor	Inter B'dary (m)	HE-Side to Cr-Cr	Survey Tool
224169.19	9237711.02	1530.93	82.78	273.49	2010.00	7.56	2.88	11.67	5.44	Alpha 1 (s)	40.83	7.88	35.65	74.85	MWD
224164.24	9237711.33	1531.56	82.78	273.49	2015.00	7.62	2.90	11.97	5.48	Alpha 1 (s)	36.38	6.74	30.99	76.79	MWD
224159.29	9237711.63	1532.19	82.78	273.49	2020.00	7.68	2.92	12.26	5.51	Alpha 1 (s)	32.09	5.61	26.37	78.77	MWD
224154.34	9237711.93	1532.81	82.78	273.49	2025.00	7.74	2.94	12.54	5.54	Alpha 1 (s)	28.02	4.47	21.76	80.77	MWD
224149.39	9237712.23	1533.44	82.78	273.49	2030.00	7.80	2.95	12.82	5.57	Alpha 1 (s)	24.28	3.35	17.03	82.79	MWD
224144.44	9237712.53	1534.07	82.78	273.49	2035.00	7.87	2.97	13.10	5.60	Alpha 1 (s)	21.05	2.31	11.93	84.84	MWD
224139.48	9237712.84	1534.70	82.78	273.49	2040.00	7.93	2.99	13.38	5.64	Alpha 1 (s)	18.61	1.79	8.24	86.90	MWD
224134.53	9237713.14	1535.33	82.78	273.49	2045.00	7.99	3.00	13.64	5.67	Alpha 1 (s)	17.27	2.30	9.77	88.97	MWD
224129.58	9237713.44	1535.95	82.78	273.49	2050.00	8.05	3.02	13.89	5.70	Alpha 1 (s)	17.31	3.13	11.78	91.04	MWD
224124.63	9237713.74	1536.58	82.78	273.49	2055.00	8.11	3.04	14.15	5.74	Alpha 1 (s)	18.72	3.98	14.01	93.11	MWD
224119.68	9237714.04	1537.21	82.78	273.49	2060.00	8.17	3.06	14.40	5.77	Alpha 1 (s)	21.21	4.67	16.86	95.17	MWD
224114.73	9237714.35	1537.84	82.78	273.49	2065.00	8.24	3.07	14.65	5.81	Alpha 1 (s)	24.48	5.83	20.28	97.22	MWD
224109.78	9237714.65	1538.47	82.78	273.49	2070.00	8.30	3.09	14.89	5.84	Alpha 1 (s)	28.24	6.84	24.11	99.26	MWD

Figure 106: Fine scanning interval report

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One good approach is to scan the entire deep well sections at a 30 m or 90 ft interval and then report close approaches at a finer 5 m or 15 ft interval. Top-hole sections with great well density may require other treatments.



## 20.12 Travelling Cylinder Plot

The travelling cylinder plot was invented by John Thorogood in the 1980s and is an excellent 2D representation of the proximity of other wells to planned trajectory.

### 20.12.1 Reading the Traveling Cylinder Plot

These plots were used regularly in the days before computers and 3D visualization software. They are still used on many rig sites where 3D visualization is unavailable. Following the examples and text below should enable you to read and understand traveling cylinder plots. Consider these screens like a radar scan when travelling down the planned trajectory.

This scan shows the basic radar screen out to a range of 250 ft. Our well passes to the left of the red well, beneath and to the right of the green well and over the top of the blue well.

At their closest points the red well comes within 120 ft., the green well comes within 70 ft. and the blue well within 30 ft.

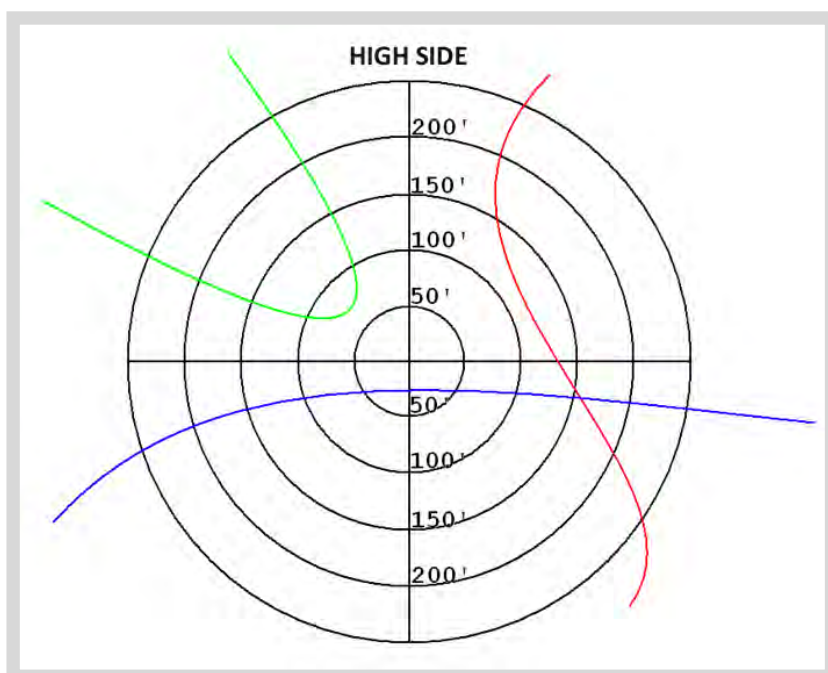


Figure 107: Traveling Cylinder Plot - basic

It is useful then to include marker points on the object wells for each MD in our well at some reasonable interval. This shows us where that well will be relative to us when we reach that depth.

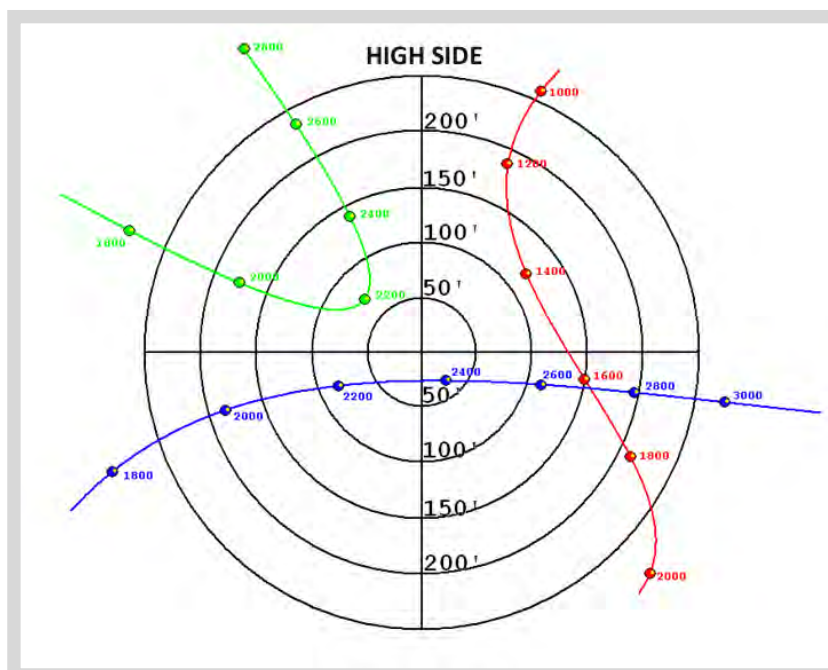


Figure 108: Traveling Cylinder Plot - with marker points

Then it is also useful to include the uncertainty around the wells. This is best done by combining our uncertainty with the object well uncertainty and showing that as a simple offset towards us to create a 'no go' boundary for the other well.

Now we can see that the green and blue wells might be dangerously closer than we think. To avoid the blue well we would want to be above our current plan around 2300 ft. and to avoid the green we should perhaps be a little more to the right.

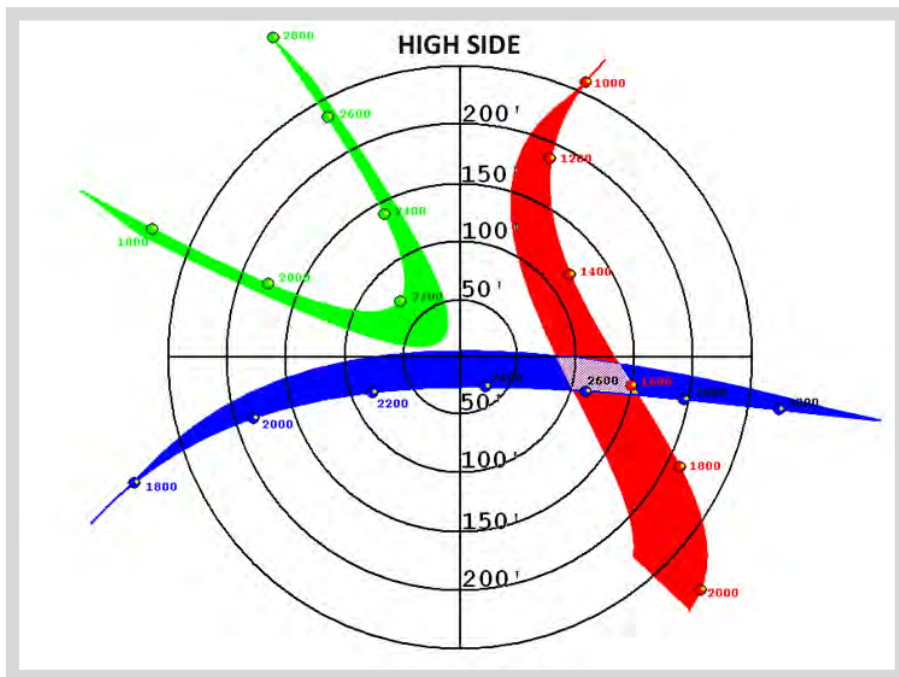


Figure 109: Traveling Cylinder Plot – marker points and uncertainty area

### 20.13 Travelling Cylinder Options

There are two options for creating traveling cylinder plots, “High Side” referenced or “North” referenced.

The first example shown in this section is a “High Side” referenced traveling cylinder plot. This option has the advantage of being easier to understand but it suffers from a peculiarity in top hole as follows.

Consider how a vertical well would appear against a well drilled roughly towards and then away from it.

The red well is our well and from points A to C it would be plotted on our high side. However, from points D to F it would be plotted on our low side since we have changed direction. This is the example “High Side” traveling cylinder plot shown on the right above. It appears that we will drill or have drilled straight through the blue well.

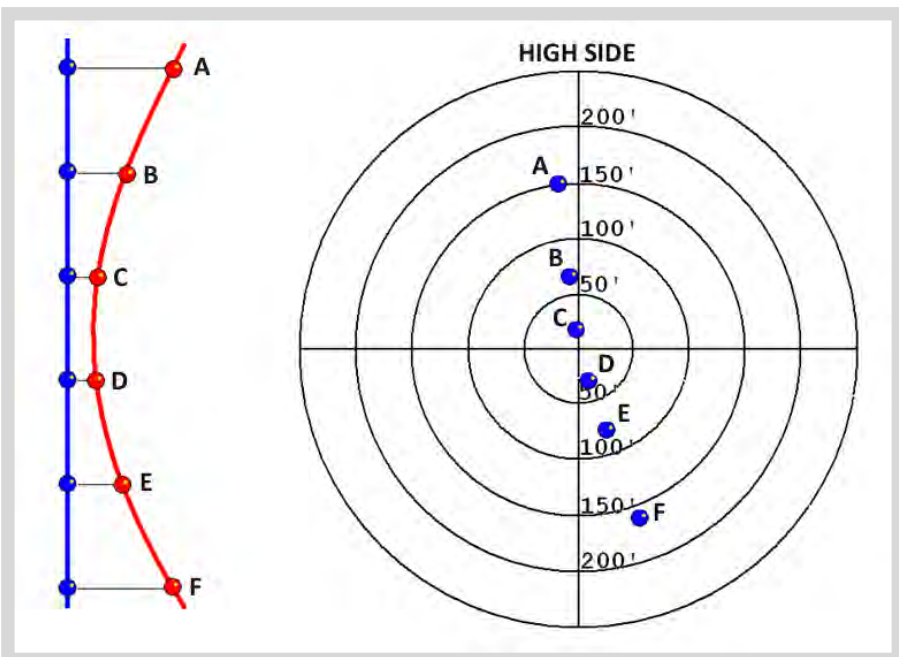


Figure 110: Traveling Cylinder Plot – marker points and uncertainty area



One solution is always to plot your high side values along a line representing your current azimuth. This makes the traveling cylinder plot look a little different. Now North is at the top of the plot and for the first three points high side is plotted along my current azimuth e.g.  $45^\circ$ .

When the well is turned around before passing through points D, E, and F, the high side is now plotted along the new azimuth e.g.  $225^\circ$ . The points are correctly plotted to low side and appear to go out the same way they came in rather than causing unnecessary alarm with an apparent collision.

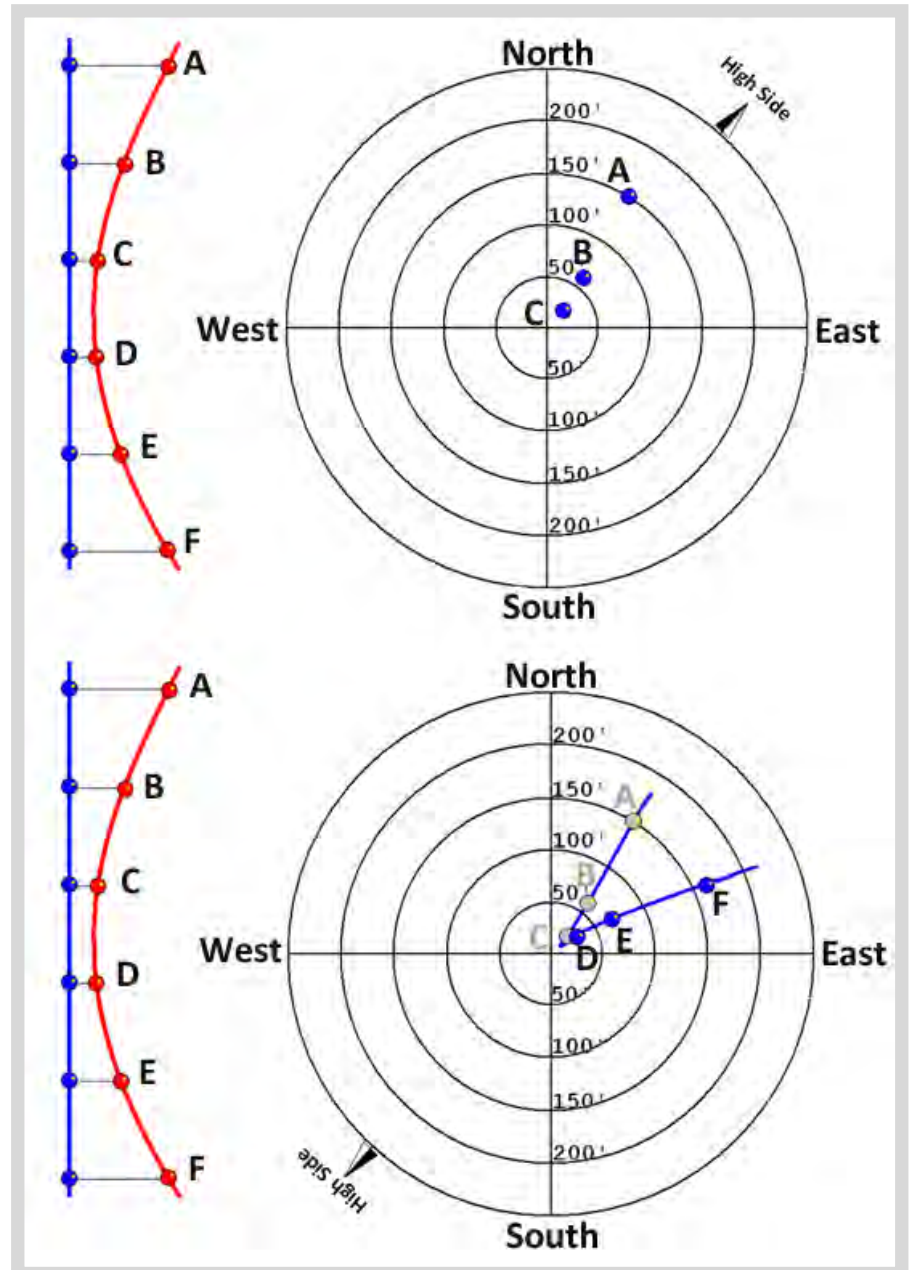


Figure 111: Azimuth referenced Traveling Cylinder Plot

## 20.14 Using TVD “Crop” Diagrams

TVD “Crop” Diagrams are useful in determining the relative positions of wells when the inclinations of ALL the wells being viewed all have inclinations which are LESS THAN 60°. This diagram slices the wells along a TVD plane and presents a view of them from above. They are particularly useful in top-hole drilling to examine the trends and help visualize the clearances at each level. They are also a great aid when having collaborative discussions with either the office or client if all parties have a copy of the diagram to view.

This diagram represents a ‘slice’ through the wells at a given TVD which can be advanced and the relative positions of the wells are updated in real time. As you continue drilling down the actual well, the start of the slicing should be incremented to match the latest TVD achieved. The examples represent the well as the 0m, 50m and 100m TVDs are reached.

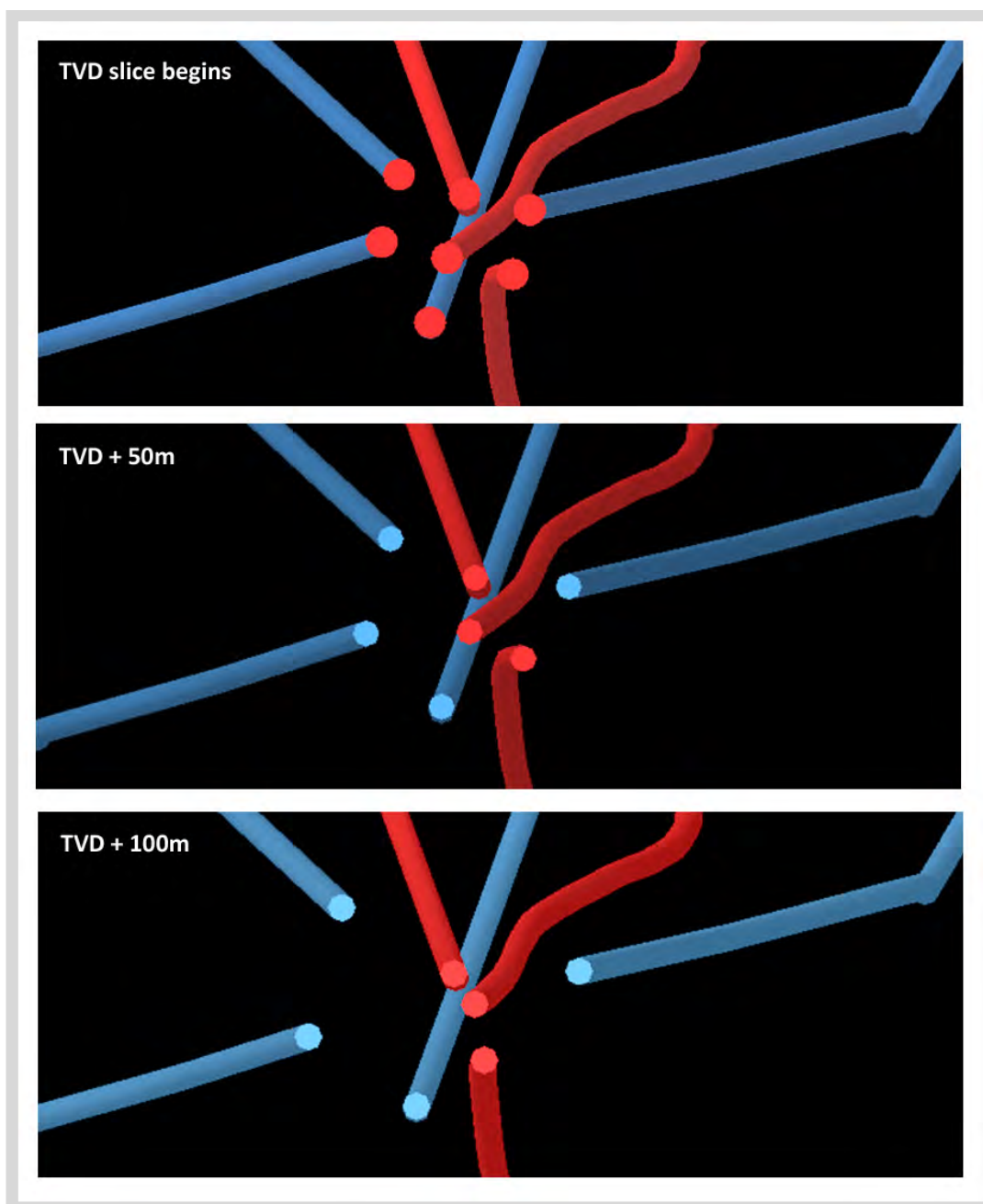


Figure 112: Slicing through the well models at a given TVD

## 20.15 Using Ladder Plots

The ladder plot is simply a graph of the separation to target wells against the measured depth of the planned well. They are very useful for determining which well to watch for at which depth.

The y-axis can either be the true centre to centre distance or more usefully, the inter-boundary distance of the zones of uncertainty to the object wells.

*Be sure to understand the value on the y axis. The most common will be a simple centre to centre separation but ladder plots are more useful if they include uncertainty.*

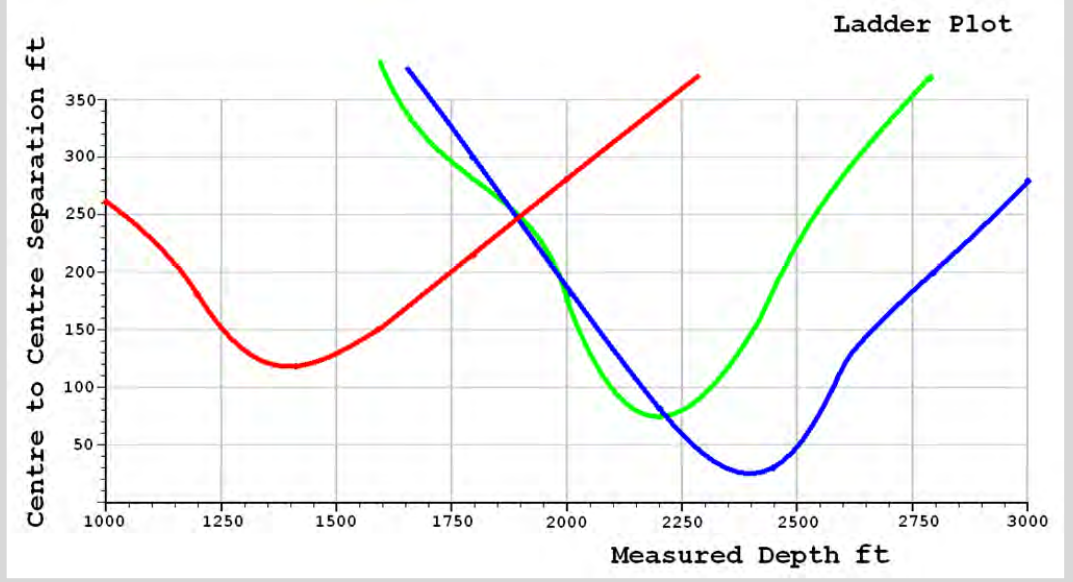


Figure 113: Basic ladder plot

*In this example the uncertainty is shown as a shaded area around the wellbores.*

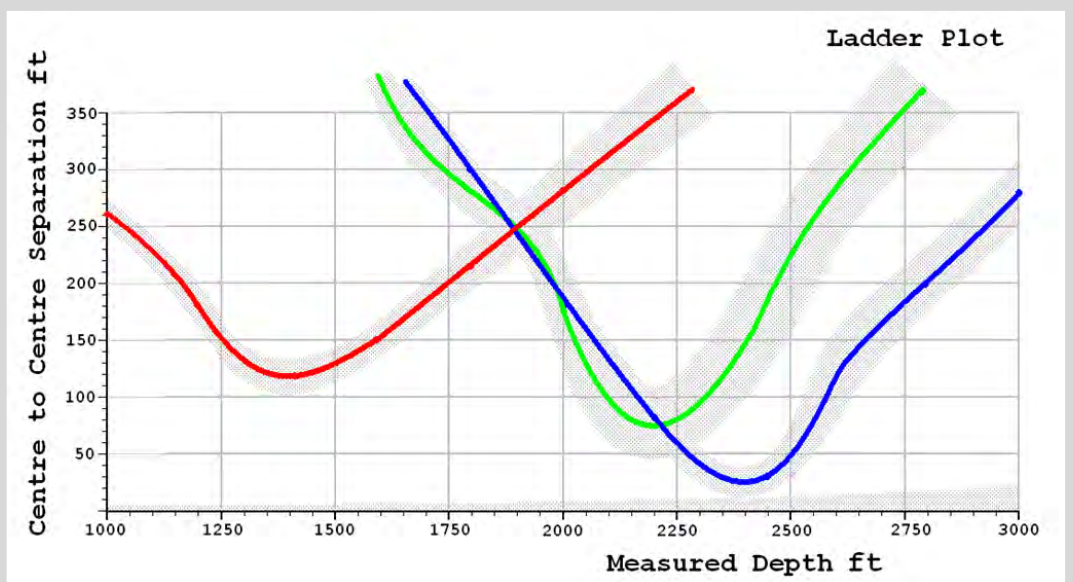


Figure 114: Ladder plot with uncertainty added

Another example is to show the inter-boundary separation only on the y axis. In this example you can see that the blue well uncertainty combined with the planned well uncertainty uses up all the separation.

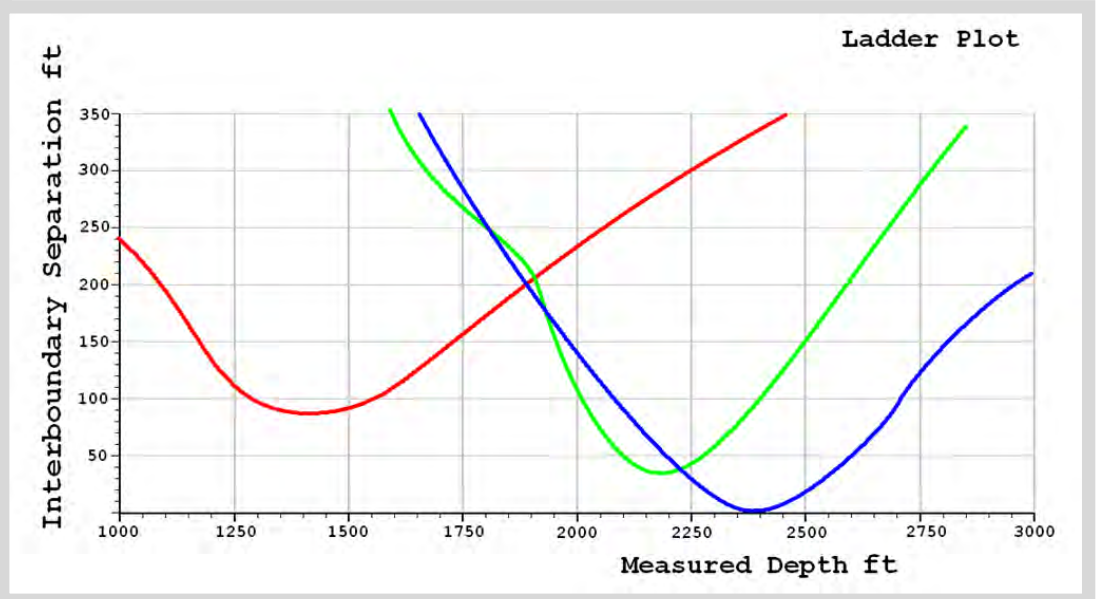


Figure 115: Ladder plot using inter-boundary separation only

In these examples you can see that the most dangerous hazard is the blue well at the planned well's interval between 2350 ft. to 2450 ft.



CONTENTS

## 21. Planning for Minimum Risk

### 21.1 Designing the Wellpath

The well planner has to consider all of the following criteria when designing the original wellpath;

- a) Is the design drillable in the formations it encounters?
- b) Are the doglegs practical from a Torque and Drag standpoint, drillpipe fatigue, casing wear, formation damage, the potential for positioning ESPs or other dogleg dependent completion equipment?
- c) Does the design hit the target with confidence?
- d) Does the design avoid other wells safely and avoid geo hazards?

Once the well plan has been created the first time, it will only be a geometrical solution which may need reviewed in the light of experience.

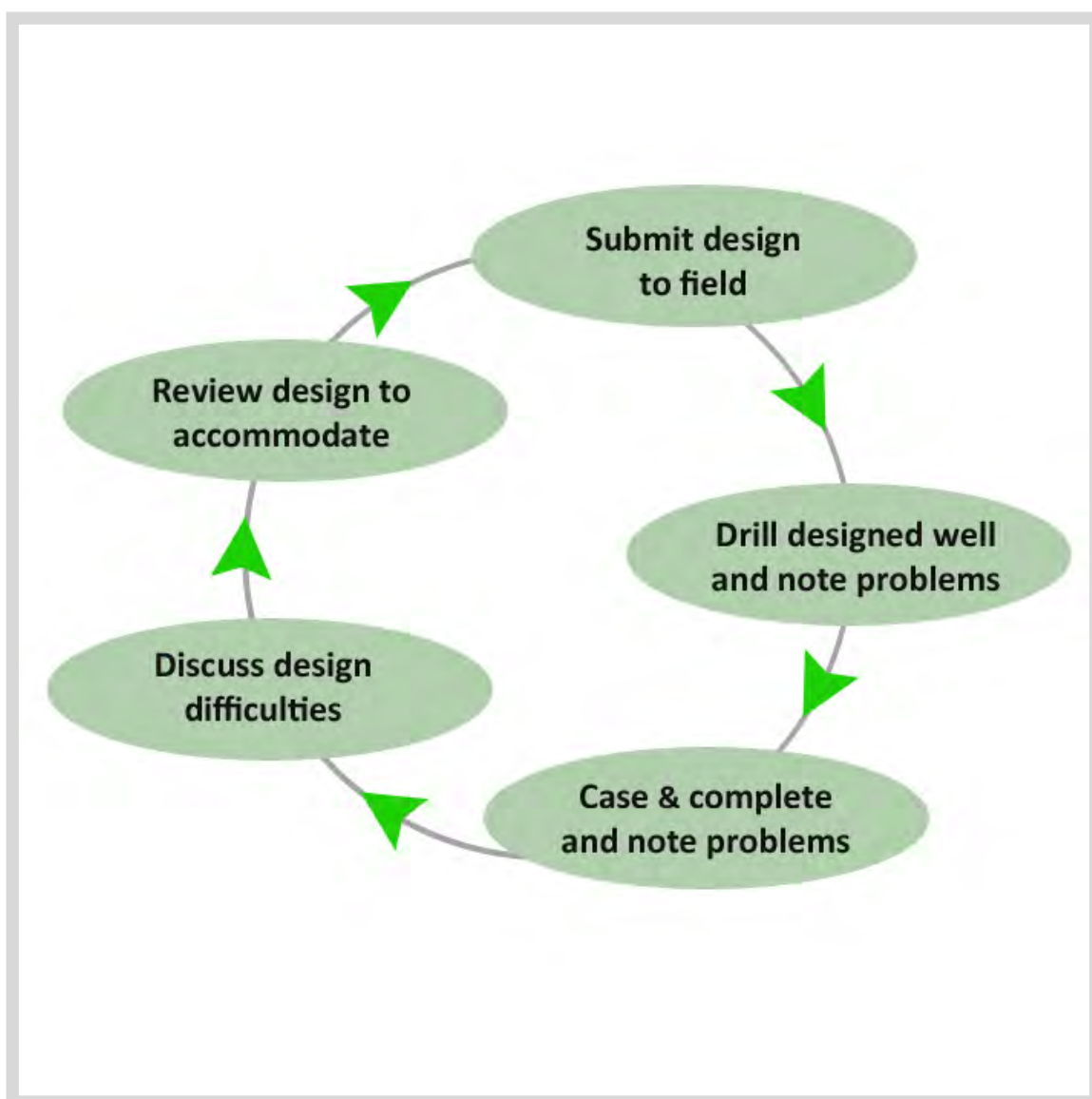


Figure 116: Minimum risk planning wheel

The following shows some of the feedback from the field and some possible remedies that will ensure that the well plan is improved for the next iteration:

**Problems**

1. Shallow formation can't take the build rate.
2. Rotating the tangent drops 0.5 per 100.
3. Formation at 6700 to 6800 TVD is too soft.
4. Can't get RSS to go above 5.2 degs/100.
5. Formation tops are always early.

**Remedies**

1. Build at 1 then 1.5 then 2 in shorter sections.
2. Design the tangent as a 0.5 per 100 drop.
3. Either pass through at low inc or design a drop.
4. Use the RSS actual DLS value in the design.
5. Compensate to observed depths.



**CONTENTS**

## 22. Basic Data QC

### 22.1 Checking Raw Data

Raw data observed in the field can be checked for basic quality control. Any set of MWD raw sensor data can be used to calculate a field strength and dip angle using the following formulae.

The Dip Angle can be calculated from the following simple formula:

$$\text{DipAngle} = \sin^{-1} \left[ \frac{(B_x G_x + B_y G_y + B_z G_z)}{(B_t G_t)} \right]$$

Where  $B_t$  = square root of  $(B_x^2 + B_y^2 + B_z^2)$  i.e. the total Magnetic Field

And  $G_t$  = square root of  $(G_x^2 + G_y^2 + G_z^2)$  i.e. the total Gravity Field

In general, if the Field Strength calculated is within 300nT of the expected field and the dip angle to be within 0.25 of the expected dip, we would consider the MWD to be within acceptable tolerances.





## 23. Advanced Data QC

### 23.1 Varying Curvature Method

Although Minimum Curvature is now considered the indisputable industry standard for survey calculation, another method was developed in the early 1990s known as Varying Curvature. It turns out that the VC method produces very similar results to Minimum Curvature but has the advantage that it can be used to perform QC on whole surveys to check for poor consistency in the data.

Consider again the effect of a small increase in MD along a particular inclination and direction.

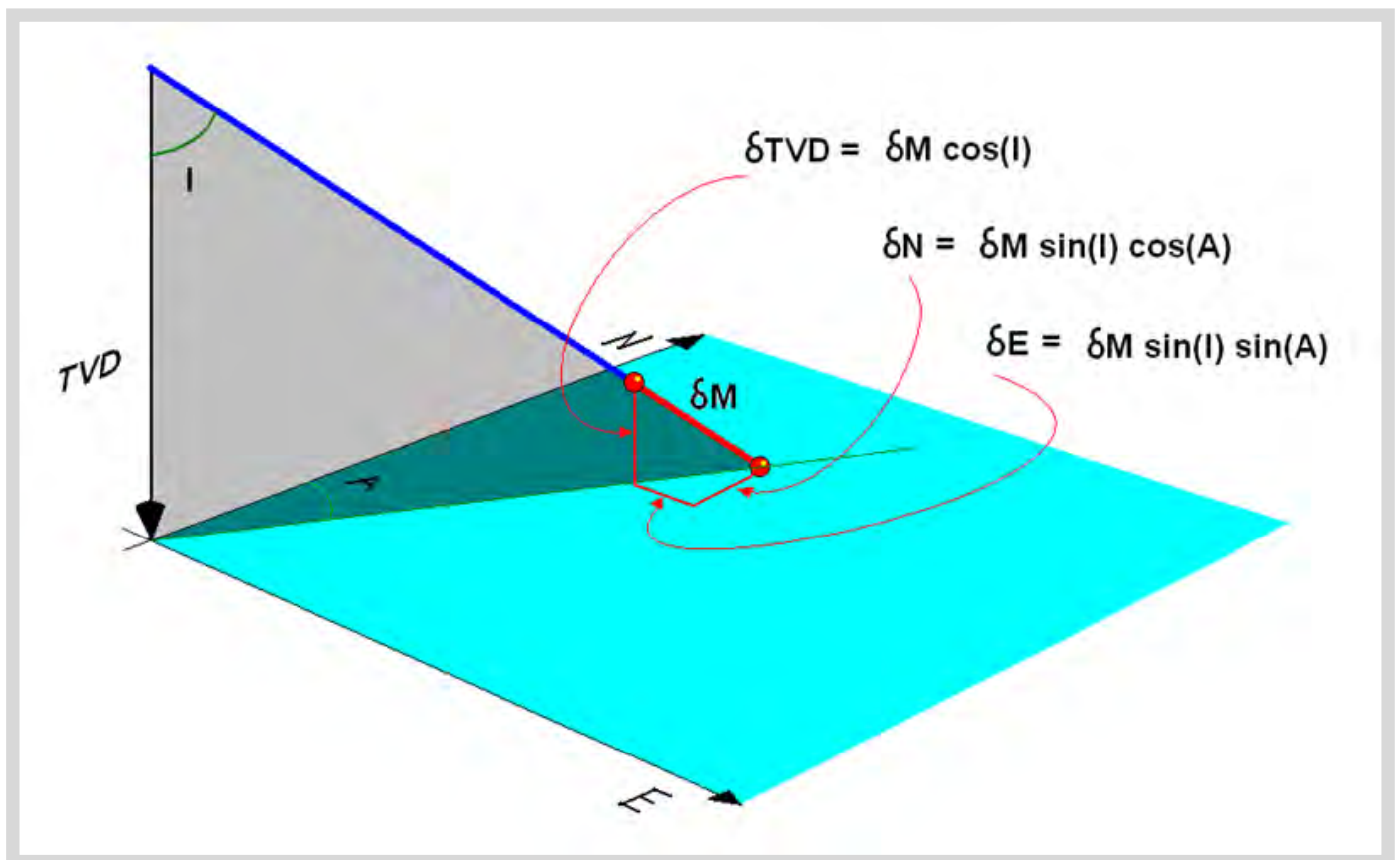


Figure 117: Measured depth error and the effect on North, East and TVD

If we were to produce a set of graphs where the x axis is measured depth and the y axes were respectively  $\cos(I)$ ,  $\sin(I)\cos(A)$  and  $\sin(I)\sin(A)$  then we can use the fact that the integrals of each would be the accumulated sums of TVD, Northing and Easting.

$$\begin{aligned}
 \delta \text{TVD} &= \delta M \cos(I) & \int \delta \text{TVD} &= \int \cos(I) \delta M &= \text{TVD} \\
 \delta N &= \delta M \sin(I) \cos(A) & \Rightarrow \int \delta N &= \int \sin(I) \cos(A) \delta M &= N \\
 \delta E &= \delta M \sin(I) \sin(A) & \int \delta E &= \int \sin(I) \sin(A) \delta M &= E
 \end{aligned}$$

In the graphs below, the y axis is used to plot the terms shown for each observation and if a smooth curve is drawn through the observed points, the TVD, Northing and Easting (from the start of the well to any MD) are simply the areas under the graphs.

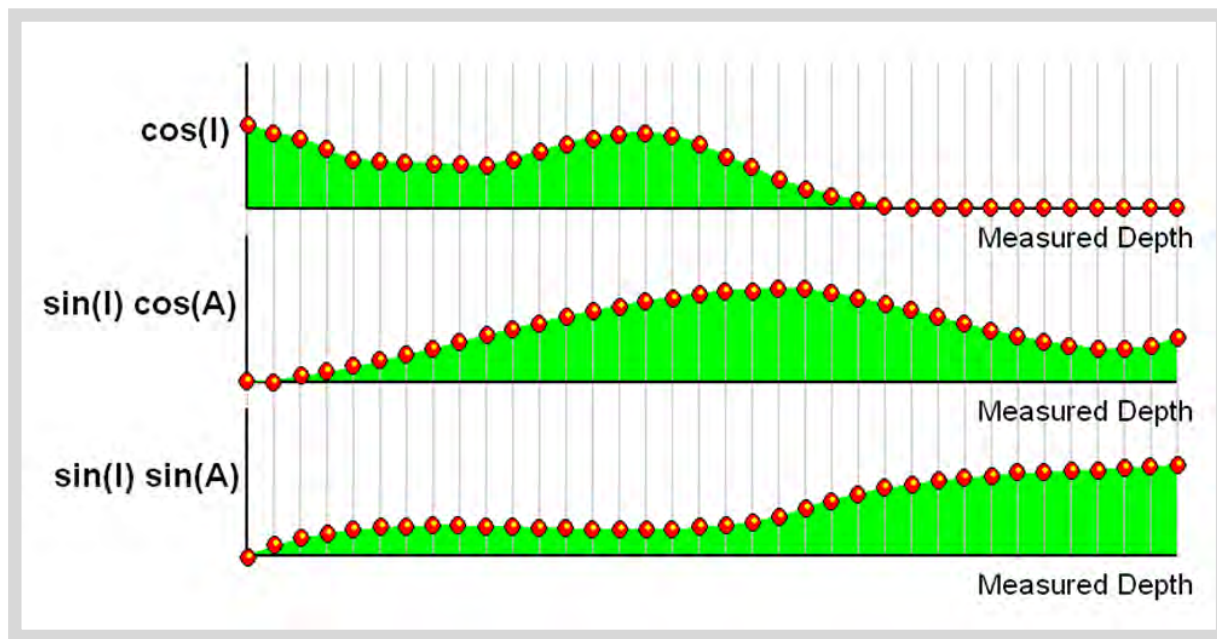


Figure 118: Using a smooth curve drawn through the observed points to show North, East and TVD

The

area of the  $\cos(I)$  graph is the TVD, the area of the  $\sin(I)\cos(A)$  graph is the Northing and the area of the  $\sin(I)\sin(A)$  graph is the Easting. By fitting smooth curves through the points, the curvature of the wellpath effectively varies smoothly through the survey rather than being fixed to a given radius between observations. Now consider the effect of a poor survey on the above graphs.

The inconsistent survey will ‘pull’ the area towards itself and the difference it makes can be determined by the difference in the area (The blue region in figure 107). In other words, varying curvature can compare the area under any of the three graphs, with and without a given survey observation and determine the effect each observation has on the wellpath position. Surveys consistent with those on either side will have very little effect if they are removed. This produces a 3D vector ‘shift’ in TVD, Northing and Easting created by the rogue observation. This vector can be split into a high/low side component and a left/right component and plotted against measured depth for a very useful consistency ‘signature’ known as a varying curvature analysis. This provides the surveyor with a digital spellchecker on his data since any typing errors will show up as highly inconsistent with the surrounding surveys.

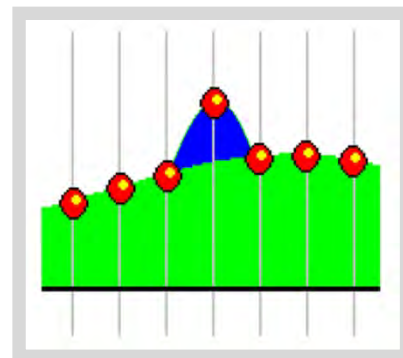


Figure 119: Spotting inconsistencies in the survey



## 24. Tortuosity

### 24.1 Illustrating Tortuosity

This has been variously defined as the variability in dogleg severity or the unnecessary undulations in the wellpath. Essentially tortuosity describes a lack of smoothness in the well trajectory and the greater the tortuosity the greater the likelihood of problems when running casing or excessive drillpipe stress when rotating in hole. One simple presentation of tortuosity is to plot the dogleg severity against measured depth.

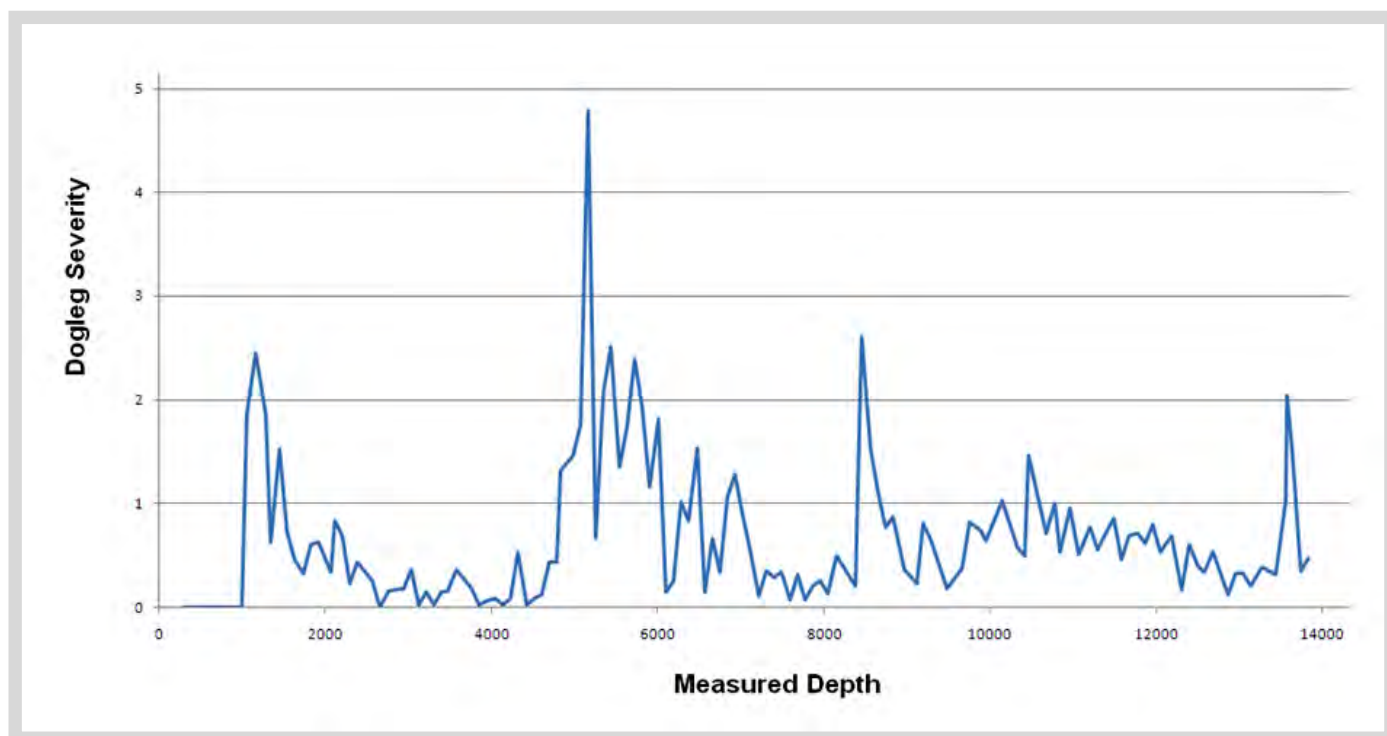


Figure 120: Plotting the dogleg severity against measured depth

However, on its own, this is hard to interpret in a measurable way. Clearly, the well is tortuous but how can we define acceptable tortuosity? If the wellplan had prescribed a 4 deg/100 build rate, it would be inappropriate to penalise a dogleg severity of 4 deg/100. The real problem is when the dogleg severity varies too much and a 4 deg/100 build is constructed with dogleg severities of 0 to 12 varying wildly during the build section. A well which smoothly followed the wellplan would have very little variation in dogleg severity. Figure 121 includes the well plan for the well above.

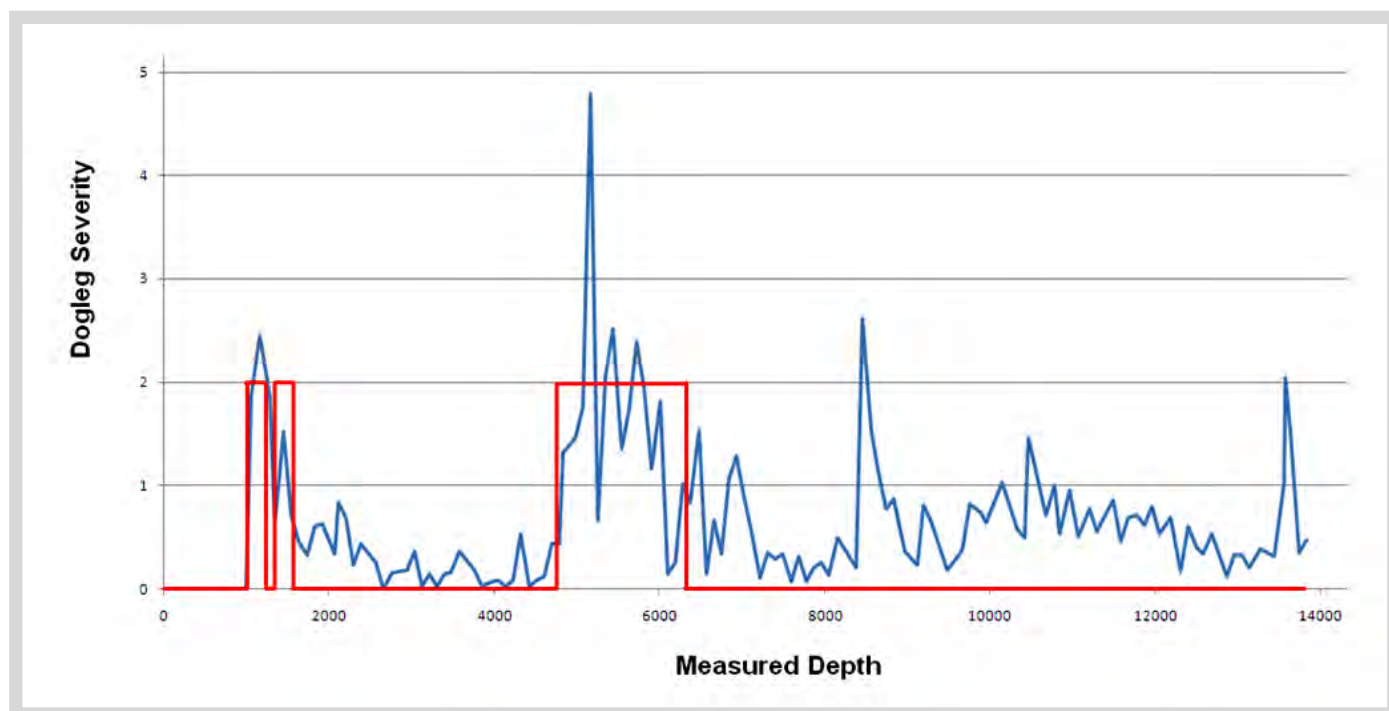


Figure 121: Example well plan graph

The planned dogleg severity should have consisted of a short 2 deg/100 nudge and drop then a simple 2deg/100 build to 27 degrees inclination then a hold to TD. The actual inclination against md graph is plotted in figure 110:

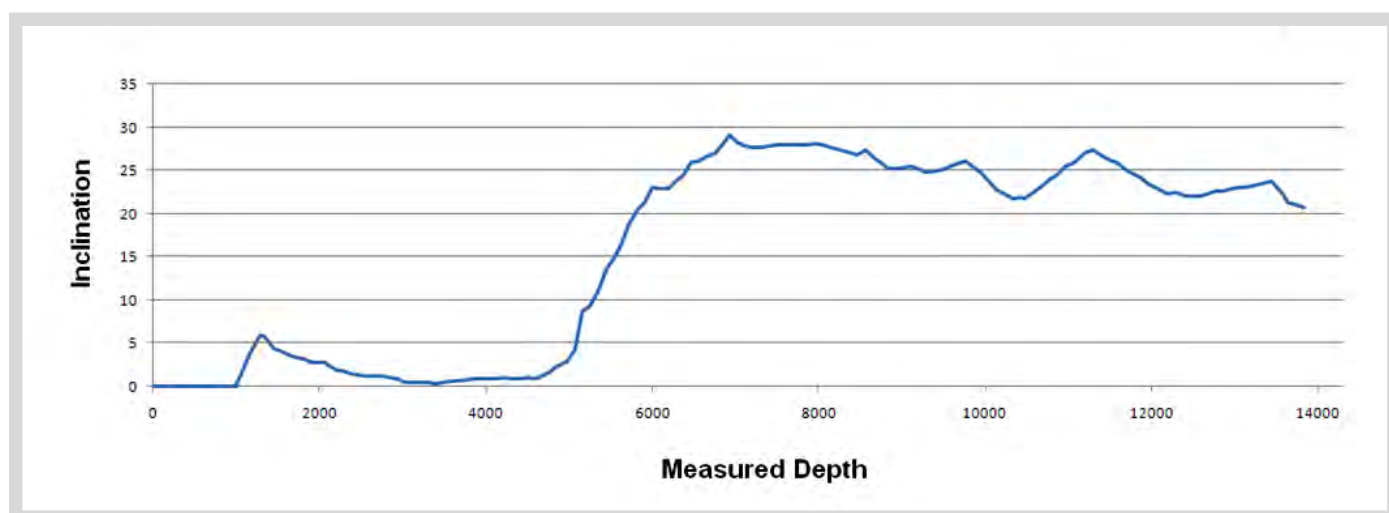


Figure 122: inclination against measured depth graph

Clearly things did not go according to plan. However, the directional driller used a standard technique for the drop section of the nudge by replacing a motor (smooth build) with a pendulum rotary assembly (slow natural drop) which is an acceptable and economic method of returning to vertical. On closer examination, the build section is rapid at first then slower later. This is likely to be an assembly with a bent sub above the motor which is less aggressive at higher inclinations but assembly was capable of over 5 degrees of dls when only 2 was needed, suggesting a slide ratio of less than 40%. This explains the rapid changes in dls in the build section but even that is not unusual. The main problems here lie in the hold section where the directional driller has great trouble holding inclination and tends to steer a great deal in an attempt to place the surveys 'on the line'. He is over correcting and creating unnecessary doglegs when a simple 'aim at the target from where you are' approach would have created a smoother well path.

## 24.2 Calculating Tortuosity

If we create an additional column in a spreadsheet to hold the changes in dls from one survey to the next, we can use that to calculate unwanted curvature induced in the wellbore. We do not need to know the well plan since any well plan will require constant curvature in each section and we are measuring the deviations from constant. By multiplying the change in dls (converted to degs/ft or degs/m) by the measured depth difference, we can simply add up the unwanted curvature in the wellpath. If the dls is unchanged, this process accumulates zero unwanted curvature.

Unwanted curvature is the sum of (dls change x md change). In the example above the unwanted curvature accumulation looks like this:

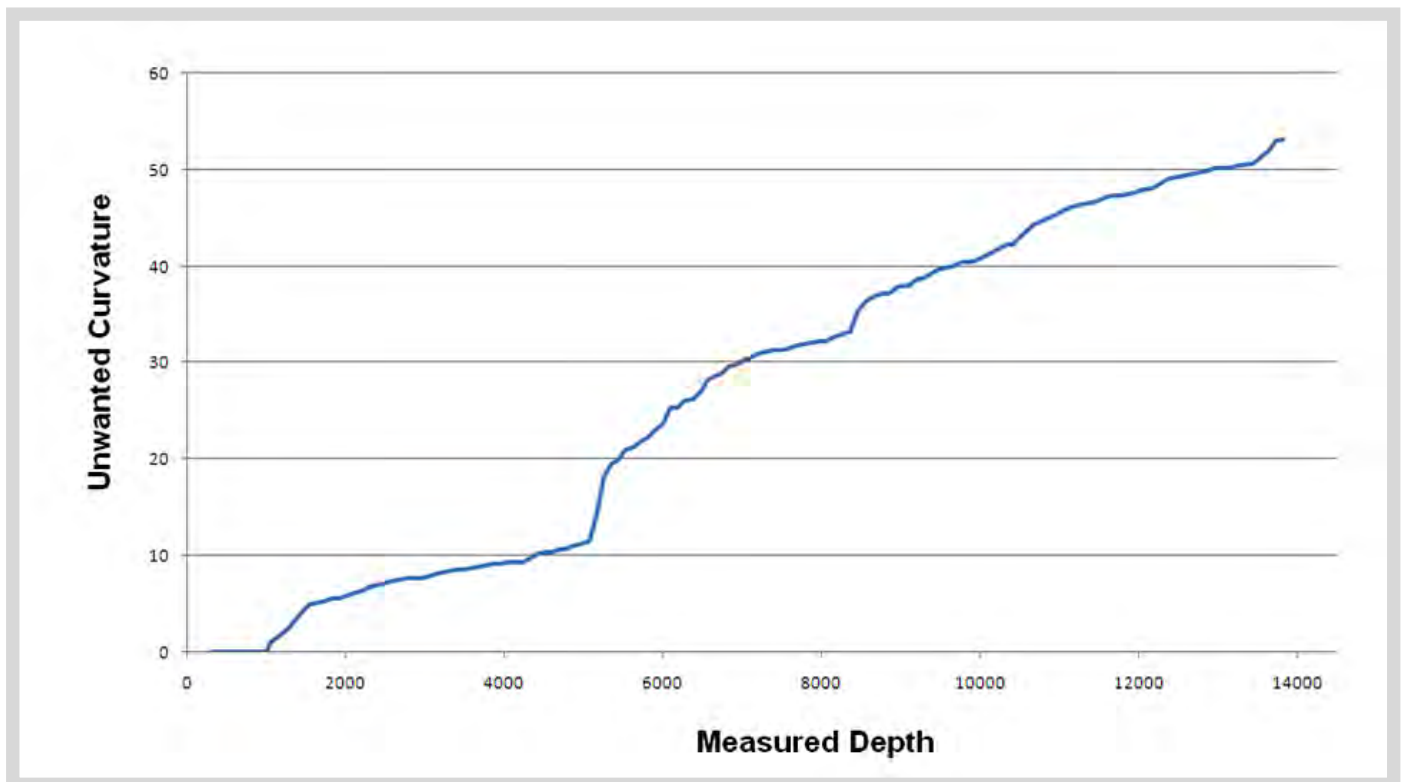


Figure 123: Unwanted curvature accumulation graph

The design total curvature was only 27 degrees and the unwanted curvature is an additional 54 degrees or 200%. Anything over 100% would be considered tortuous and likely to cause casing and pipe problems.



## 25. Combined Surveys

For many years, we have taken MWD surveys then perhaps run a gyro afterwards and thrown away the MWD and replaced it with the gyro. There is no need to waste data like that. One of the simple rules of statistics is that the standard deviation of a combined measurement is the square root of the sum of the squares of the individual measurements divided by the number of measurements.

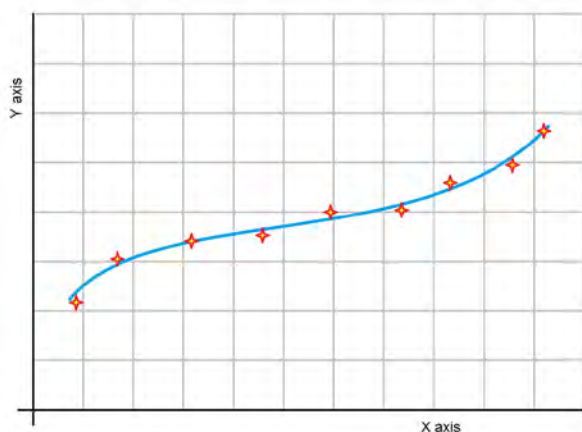
$$\sigma_c = \sqrt{\frac{\sigma_1^2 + \sigma_2^2 + \sigma_3^2 + \sigma_4^2 + \dots + \sigma_n^2}{N}}$$

In other words, if we had two similarly accurate instruments which we could demonstrate were uncorrelated in their error sources and we took an average of their observations, the uncertainty would reduce by 1/1.414 or approximately 30% reduction.

On certain high accuracy jobs, we can combine multiple gyro runs along with the MWD, (in-runs and out-runs) and fit a best fit curve through the data to produce a synthetic trajectory which is more accurate than any of the original surveys on their own.

Right now we don't have a formal error model for combined surveys but it would not be difficult to derive as it would simply be a combination of the covariance matrices of the individual surveys. Nevertheless, it is often very worthwhile to combine the available surveys just to improve confidence in the well path position even if we do not see the benefit in the calculated ellipse of uncertainty.

First of all, we need to understand how to curve fit smoothly through multiple observations.



Choose what rank of polynomial you wish to fit to the data.

A straight line will be of the form  $y = ax + b$

A quadratic curve will be of the form  $y = ax^2 + bx + c$

A cubic curve (allows for inflection as in the diagram)  $y = ax^3 + bx^2 + cx + d$

We will use a cubic (rank 3) polynomial. At each observation within the range we would ideally like the curve to pass through the coordinate  $x, y$ .

we have 4 unknowns, the coefficients  $a, b, c$  and  $d$  so if we only had to fit 4 coordinates we could write 4 equations

$$\begin{aligned} a x_1^3 + b x_1^2 + c x_1 + d &= y_1 \\ a x_2^3 + b x_2^2 + c x_2 + d &= y_2 \\ a x_3^3 + b x_3^2 + c x_3 + d &= y_3 \\ a x_4^3 + b x_4^2 + c x_4 + d &= y_4 \end{aligned} \quad \text{or in matrix form} \quad \begin{bmatrix} x_1^3 & x_1^2 & x_1 & 1 \\ x_2^3 & x_2^2 & x_2 & 1 \\ x_3^3 & x_3^2 & x_3 & 1 \\ x_4^3 & x_4^2 & x_4 & 1 \end{bmatrix} \begin{bmatrix} a \\ b \\ c \\ d \end{bmatrix} = \begin{bmatrix} y_1 \\ y_2 \\ y_3 \\ y_4 \end{bmatrix}$$

Matrix X    A    Y

However we have 9 observations and therefore 9 equations to solve only 4 unknowns. To get the best fit cubic curve we can pre-multiply these matrices by  $M$  Transposed to achieve a definable, unique solution from

$$M^T M A = M^T Y$$

Figure 124: Polynomial fit through the data

This multiplication produces the following matrix equation from which the coefficients  $a, b, c$  and  $d$  can be easily calculated.



$$\begin{bmatrix} \Sigma X^6 & \Sigma X^5 & \Sigma X^4 & \Sigma X^3 \\ \Sigma X^5 & \Sigma X^4 & \Sigma X^3 & \Sigma X^2 \\ \Sigma X^4 & \Sigma X^3 & \Sigma X^2 & \Sigma X \\ \Sigma X^3 & \Sigma X^2 & \Sigma X & \Sigma 1 \end{bmatrix} \begin{bmatrix} a \\ b \\ c \\ d \end{bmatrix} = \begin{bmatrix} \Sigma X^3 y \\ \Sigma X^2 y \\ \Sigma X y \\ \Sigma y \end{bmatrix}$$

This is a really useful tool for fitting curves through any data and if you need a higher ranking polynomial you just continue the pattern for extra parameters.

In order to combine surveys of different instruments and differing accuracies, we can create a rolling curve fit using say the nearest 6 observations of inclination and azimuth using the following procedure.

1. Choose a final survey interval of say 20 ft
2. From the first to the last measured depth value in the surveys in steps of 20ft:
  - a. Find the nearest 6 surveys
  - b. Let  $x = 0$  at the Md of interest
  - c. For each survey set  $x = \text{Md survey} - \text{Md of interest}$ .
  - d. Let  $y = \text{inclination of each survey}$
  - e. Fit the curve as above through all 6
  - f. The inclination required at Md of interest is just the value  $d$  (at  $x = 0$ )
  - g. Let  $y = \text{azimuth of each survey}$  (if passing through North add 360)
  - h. Fit the curve as above through all 6
  - i. The azimuth required at Md of Interest is just the value  $d$  (at  $x = 0$ )
3. When weighting the curve, the relative accuracy can guide the use of weights so all the additions should be done with the appropriate weighting values. For example, if it is considered that a gyro survey is twice as accurate as a raw MWD survey, you would add the gyro survey contributions to the matrix with a weighting of 2 and the MWD with a weighting of 1.

In this example plot the various contributions to a relief well survey are superimposed in different colours with inclination in the top graph and azimuth in the bottom graph. The grid on the left shows the disagreement survey by survey in inclination and azimuth (all less than 0.5 degrees) and the length of the line is the relative weighting.

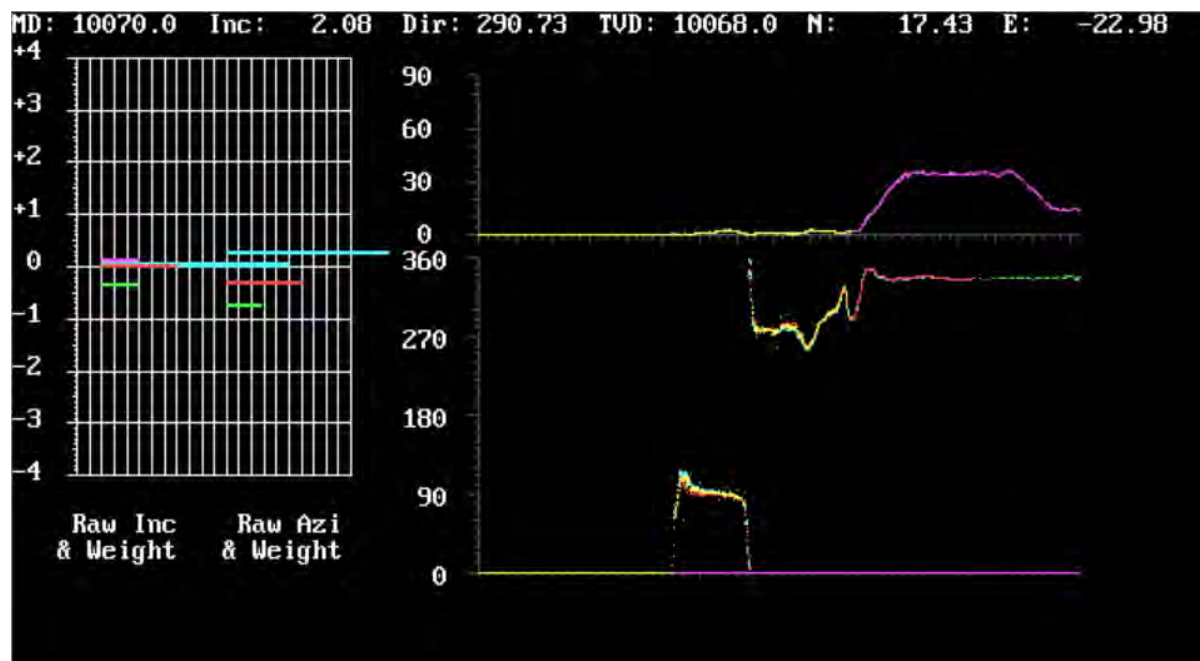


Figure 125: An example of combined survey data

The final result is a complete synthetic survey that best fits all the input data.



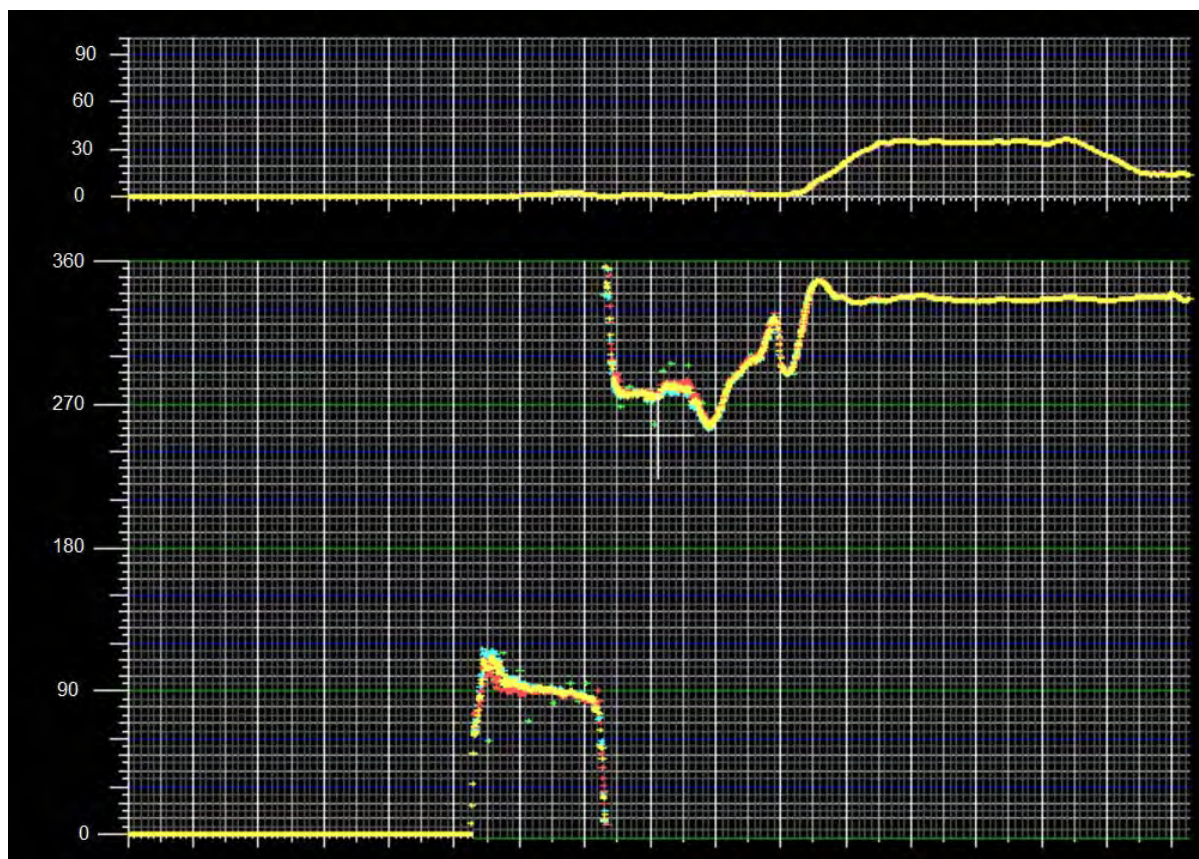


Figure 126: The definitive best fit survey

In this case the uncertainty of the final well path was around 1 to 2 feet per thousand.

## 26. Some Guidelines for Best Practice

### 26.1 Required Data

Experience has shown that the most common cause of an unexpected collision is lack of awareness of the very existence of the hazard well! It is essential that the following questions are asked before well planning commences;

1. What are the sources of the client survey data?
2. How can we be sure that the data set is complete?
3. How does the database compare with the data held by the geoscientists, in-house surveyors and the regulatory authorities?
4. Are we sure that all surveys are complete to TD?
5. Are all possible offset wells within reach of the current well included? (Be sure to include wells from other sites if necessary and exploration wells).
6. Does the reference data agree with those held in other in-house databases and is it what the site surveyors used when establishing site coordinates and directions?

The following information should be gathered and considered in detail prior to beginning the actual well planning design process.

## 26.2 Position and Referencing Data

Clearly it is essential that all data required to fully define the location of a well and its adjacent hazard wells must be available to the well planner. These must include;

<b>Required Data:</b>	<b>Example:</b>
The field or project name	Orkney West
The name of the well site	Alpha Platform
The units of measure used at this site	Ft
The geographic location of the Site Centre in Latitude and Longitude	56° 26' 18.32" N 11° 32' 56.78" W
The Geographic Datum on which Latitude and Longitude are defined	WGS 84
The map coordinates of the Site Centre	6257790.50 North 342842.46 East
The map units used	m
The coordinate system in which the Map Coordinates are defined	UTM Zone 29 North
The accuracy of this point (surface uncertainty)	+/- 5 m
The clients preferred North Reference True or Grid	Grid
The Grid Convergence	-2.12°
The height of the drill floor above Field Datum	120 ft
The Definition of Field Datum	Mean Sea Level
The Depth BDF to the Ref Point from which uncertainty accumulates	270ft
The Definition of the Reference Point	Mud Line

*For each well including the new planned well:*

The local slot coordinates relative to the site centre	15.56 ft N
(Note these must be in the clients preferred North Reference)	1.41 ft E
Any deviation of TVD origin above (or below) site drill floor	0 ft
Current Magnetic Vector at site (for inclusion in drawings only)	50017 nT @ 70.19° Dip Angle -7.76° Declination
Magnetic Field Date	27th July 2009
Magnetic Field Model	BGGM 2009

\*If IFR data is to be used then the Magnetic Vector relevant to each hole section must be identified.

## 26.3 The Existing Well Data Including Survey Tools and Depth Ranges

Any missing data within the drilling range of the new well constitutes a serious safety hazard. Whilst the legal responsibility for the completeness and quality of a survey database rests with the asset owner, in practice, many operators do not have a formal survey focal point with responsibility for this. It is imperative that all steps be taken to ensure the quality and completeness of the data before the well is planned and this should be formally agreed in writing with the operator and included in any new proposals.

**Table 11: Example of tool runs in a survey**

The required data includes the surveys and the detail of the individual tool runs in each survey leg, for example:

Survey Summary Form											
Well Name	Surface Position				Survey Runs	Survey Tool	Date (dd/mm/yy)	Start Depth	End Depth	Corrections	Comments
	North	East	Defined	Accuracy							
Alpha 5	0	0	local		2	Gyrodata RGS	18/05/08	0	1567	None	13 3/8 Casing
						MWD	12/06/08	1620	7943	Sag + IFR	
Alpha 9	-15.56	-1.41	local		3	SDI Keeper	02/11/08	0	1638	None	13 3/8 Casing
						SDI Keeper	16/11/08	1640	2189	None	Drillpipe in 12 1/4 hole
						MWD	23/11/08	2240	8345	Sag + IFR + Mag Int	
22/17 a	6270163	341763.8	map	20m	1	TOTCO	09/04/83				

\*all depths in consistent units

Then for each survey:  
Alpha 5 Gyrodata RGS from 0-1567

Md	Inc	Dir	TVD	North	East
0	0	0	0	0	0
etc					
etc					

#### Notes on the treatment of vertical wells:

1. If any "inclination only" surveys are part of the database, they are best entered with the inclinations set to 0.00 for the entire "inclination only" survey. A common error is to enter the actual inclination whilst leaving the azimuth set to 0.00. This erroneously enters a well that has been drilled due north and creates a false impression that a safe clearance exists passing to the south side of the "vertical" well.
2. If the vertical well has been surveyed by "inclination only" then well planners should assume the vertical well can deviate 50 feet per thousand in any direction as the safety envelope for planning around this "vertical" well.
3. When a 'vertical' well with "inclination only" surveys constitutes a high collision risk a recommended practice is to enter the "well" at least six times into the database. This should be done by entering the actual inclinations (in six successive wells) first with azimuths of 0°, then another with azimuths of 60°, and then additional wells at azimuths of 120°, 180°, 240° and 270° successively to create an 'Eiffel Tower' of possible locations of the vertical well. The well planners' and directional drillers' software can then conduct anti-collision scans against these dummy wellbores.

## 26.4 Existing Planned Well to be Avoided (Caging)

'Caging' can happen in the latter part of a site development program when collision risk with currently undrilled planned wells are given low priority. Eventually the planned wells cannot be drilled as the slot is 'caged' in by other wells. It is worth including the trajectories of currently undrilled but planned wells into the program so that their positions can be considered when assessing the impact of a non-conformity to plan. In such cases, the client should be apprised of the risk to future well plans and his agreement to proceed be obtained in writing. Clearly it is best if all anticipated future well plans are included at the earliest stage.

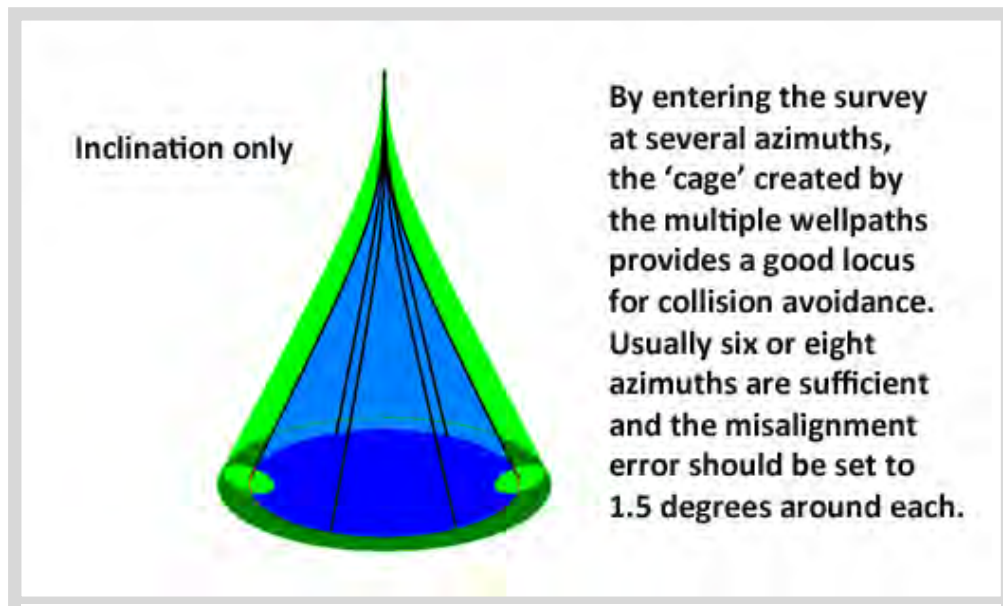


Figure 127: 'Caging' for collision avoidance planning

## 26.5 Separation Rules

Most clients will adopt a safety rule based on separation factor. Separation factor is the ratio of the "as surveyed" or "as planned" centre to centre distance of the wells divided by the uncertainty as to their actual locations.

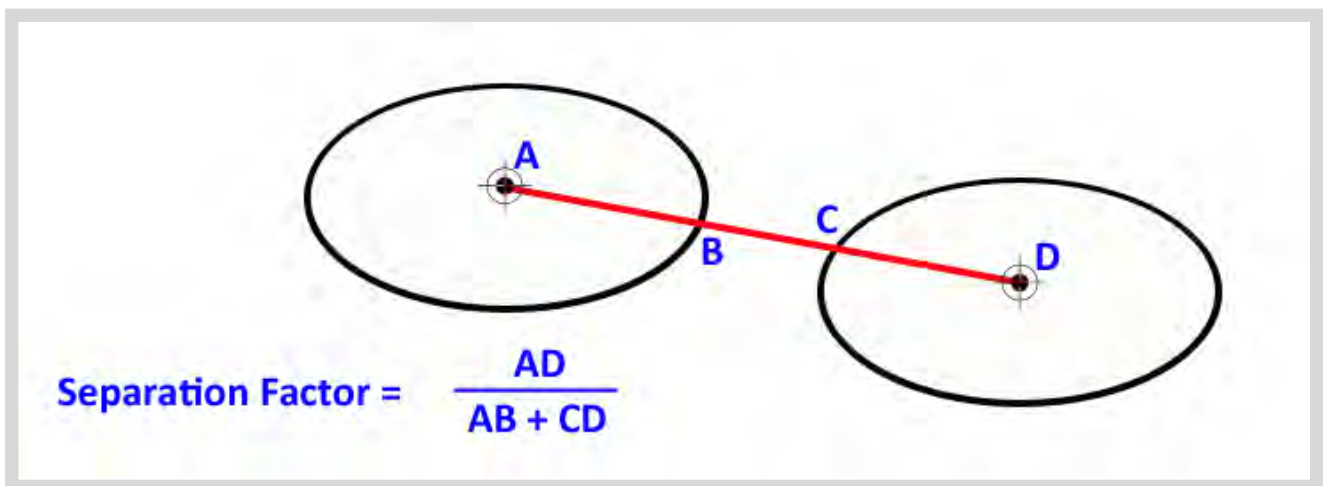


Figure 128: Graphic of separation factor calculation



For most companies the rules will be similar to the following but in the absence of client guidelines the following should be adopted:

1. When the database is newly acquired or constructed, or when starting a new project, a scan of all wells in the field must be conducted.
2. Review this scan with a local field expert to verify:
  - a. All wells are present. (Be careful to verify plugged and abandoned exploration wells as well as wells drilled by other operators are included).
  - b. All wells are located properly. (The catalogue of errors that can occur when transferring a database is numerous but just two examples are: 1) incorrect platform location and 2) transposing the inclination and azimuth values between the original data and the new database).
3. With a fully quality controlled database scan all wells that have even a remote possibility of being within the path of the planned well.
4. Report all sections where the separation factor falls to less than 4.0.
5. If the separation factor falls below 1.5 attempt to adjust the well plan. For many operators this is the approach limit that requires adjacent wells to be shut in whilst drilling the new well. This is not in itself a risk free strategy since the pressures rise bringing their own hazards.
6. If the separation factor falls below 1.25 attempt to adjust the well plan. This is leaving inadequate room for directional drilling adjustments during the execution phase.
7. In certain cases, it will not be possible to plan the well without generating separation factors that transgress the limits in the two previous instructions. Most companies have a policy that in no cases should a well be planned with a separation factor less than 1.0. There may be some dispensation policy in place that if the risk is merely fiscal and other mitigating steps are taken, permission may be given to proceed but this should always be the last resort.
8. If it is impossible to plan the well without separation factors equal to or greater than 1.0 then a special dispensation to drill with a sub 1.0 separation factor must be granted by the client. The operator may grant this dispensation in special cases. Examples cases might be; if the hazard well is one that is planned but not yet drilled, or perhaps in a case where circumstances like the following apply: (These are only examples and by no means comprehensive).
  - a. The hazard well is protected by at least two layers of casing.
  - b. The angle of attack is less than 10 degrees.
  - c. The wells are equally pressured or the pressure difference is safely manageable.
  - d. The well cross sections make up less than 1% of the 1 sigma error ellipse.



## CONTENTS

## 27. Relief Well Drilling

It is now a requirement in many parts of the world to have a contingency plan in place for a potential relief well. This section of the manual sets out the main positioning considerations for such an operation and these have a very significant effect on well planning, especially for complex and crowded pads and platforms.

### 27.1 Magnetic Ranging

All steels are magnetic to some degree but the mild steel, used in casing and lining is very magnetic. When steel pipe magnetises naturally in the earth's magnetic field it tends to magnetise with the opposite polarity to the Earth Field. This means that pipe that has been stored together tends to have a change of polarity at every thread joint and a strong detectable magnetic field along its length. A magnetometer placed close to the steel, will measure the vector sum of the earth's magnetic field and the steel magnetic field. A magnetic influence increases with the inverse square of the distance from the source. If we hold a magnetometer at half the distance, we see 4 times the field strength. As a result, the strength of the earth's magnetic field can be considered to be relatively constant due the fact that the source, however strong, is so far away, but the influence of nearby steel will vary considerably depending on our proximity to it.

There are two broad types of magnetic ranging known as Passive and Active. Passive Magnetic Ranging uses a standard MWD sensor set, to detect changes in the background magnetic field. These changes are affected by the distance from the magnetic source as described above and the polarity of the influence which changes with every casing joint. It is possible then to observe the influence from several positions and 'triangulate' the location of the centreline of the other well from the results. This requires that the pole strength be sufficient to be 'seen' by the sensors and for practical reasons this unlikely beyond about 15m or 50ft.

Active Magnetic Ranging uses a power source downhole to inject current into the surrounding rock. When the current is passing through rock, the resistance is high but when the electrons find steel, they rush through the steel with very little resistance creating a very strong cylindrical magnetic field around the steel. This active magnetic induction can be 'seen' from up to 100ft away and is a popular alternative to passive ranging in relief well situations. However, although it provides more accuracy, the ranging tool requires a separate trip in hole and for a deep relief well, this is very time consuming. More recently an Active Ranging While Drilling (ARWD) tool has been developed which will provide an active ranging facility within an otherwise normal drilling assembly which is very useful for the closer range operations and avoids the need for tripping.

The magnetic field is detected using a set of three magnetometers but these are not arranged in the usual orthogonal geometry. They are arranged in a ring and set at 120 degrees to each other. The three readings will not exactly agree. The magnetometer closest to the source will show a stronger reading than the other two and the degradation in signal over the very short baseline provides an estimate of the distance.

In this example, the magnetometers at A, B and C experience the magnetic field at different intensities as illustrated by the graphs.

Comparing the values at A, B and C we can determine the direction of the field gradient which will point approximately to the centre of the well. The magnitude of the gradient can be determined from the degradation from A to B to C resolved along the vector of approach. From this an estimate of the distance to the magnetic source can be derived. The 'direction' is actually a toolface angle in a plane at right angles to the wellbore.

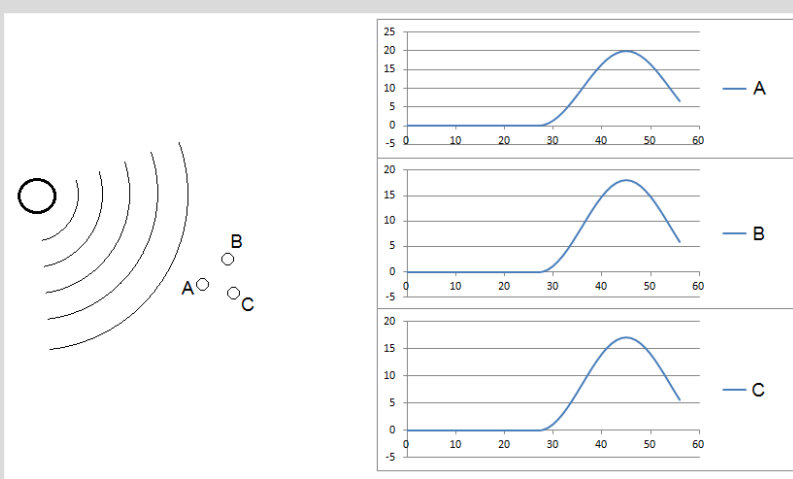


Figure 129: Estimating the range from a magnetic source

Clearly, this is very inaccurate when the field strength is weak and the degradation is very small from one signal to the other. This occurs when the target is a long way off and thus the uncertainty is very large. A first ranging shot is not worth taking unless you are within about 100ft of the target well.

The uncertainty on a ranging shot is on both distance (Range) and Bearing (Toolface Angle) and the normal distribution of likely positions of the target well looks like a wedge shaped mountain as shown. The surveyed target well trajectory (shown here in red) is then adjusted to the centre of the normal distribution after each shot and the plan to target is updated based on the latest estimate of the relative position. Clearly this becomes much more accurate as the proximity improves.

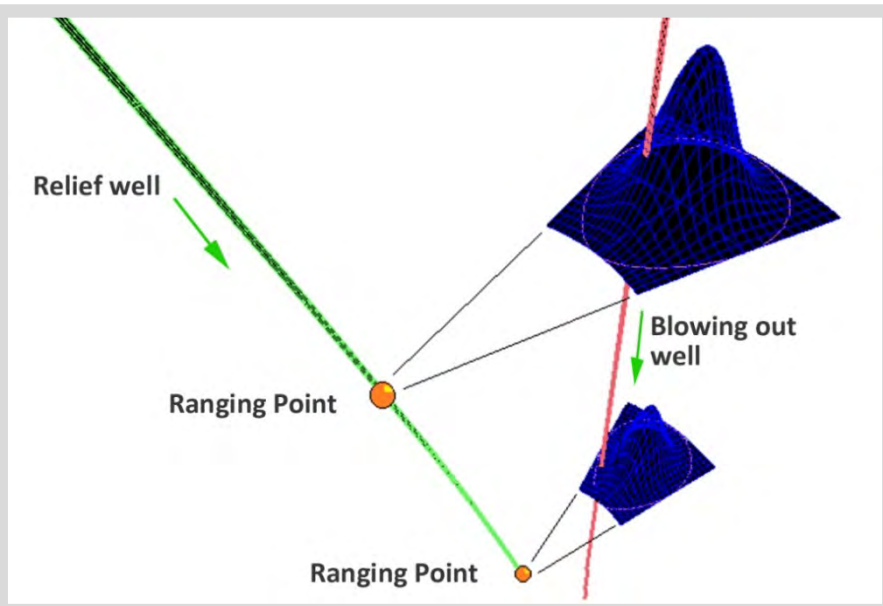


Figure 130: How the uncertainty forms on the ranging shot

### Some Practical Considerations

1. A relief well can only be drilled from a safe location. This usually means that a relief well plan will estimate the prevailing wind direction and 'smoke range' and this determines the location of the relief well rig. This will be a considerable distance from the target well so accurate surveying including surface positioning, is required in both for a successful relief well.
2. The kill point in a relief well cannot be any shallower than the point at which the hydrostatic head of kill mud exceeds the pressure in the target well. At this point the uncertainty may well be more than 100ft. When planning the relief well, it is often required to design to a 'location' or 'homing in' point well shallower of the kill point. This point has to be shallow enough that the combined uncertainty of the relief well and the target well does not exceed 100ft for active ranging and 50ft for passive ranging.



3. It is never allowed to approach the target well with a separation factor less than one before ranging. Once ranging is underway, the relative positioning uncertainty takes over but prior to the first ranging shot, there must be no danger of colliding early with the target well or you may have two blowouts for the price of one.
4. When selecting the homing in point, it is important to remember that the ranging tool will only see the effects of one magnetic field no matter how many wells have contributed to it. It is vital then that at this point there is no danger of ranging to the wrong well. This then forces discipline in the planning stage especially on crowded platforms and pads where there has to be enough space for the relief well to reach the target without significant collision risk and for the target well response to be unambiguous. As a rough guide, all other wells should be at least three times the distance away that the target well is when taking the first ranging shot.
5. After each ranging shot, the survey on the target well is shifted to pass through the observed position. As you approach closer, this shift should reduce in size. If it increases in size, there is a danger that the ranging is seeing more than one well and the procedure should build in more ranging checks to establish an unambiguous target. Another reason though may simply be a poor quality survey in the original well. This is one of the main reasons why relief wells can be severely delayed as we 'search' for the trajectory of the other well. This is often a frustrating and expensive process often with considerable public interest and the excuse that we saved money on surveying does not go down well in the press.
6. The combined uncertainty is a specialist calculation that looks at the sources of error affecting both the relief well position and the target well position. In the absence of anything else, if both wells are MWD, it is safest to assume that both error ellipses are full size and geometrically add them together. However, in many cases, when a relief well is called for, the primary cost consideration is not surveying. There is usually justification for multiple gyro runs to minimise the uncertainty on the relief well. (Gyros can be attached to the ranging tools for additional high quality in-runs and outruns with multiple overlaps). As a result, in the calculation of combined uncertainty, the target well uncertainty dominates the error budget and the contribution of the relief well gyros is almost negligible in the sum of the squares of the errors but it cannot be ignored completely.
7. When planning a relief well, if the homing in point is not the same as the kill point, it may be necessary to 'track' the target well until kill depth is achieved. This usually means that the relief well crew will want to approach the homing in point with a similar inclination and direction as the target well to minimise steering to parallel in order to keep the target well in range. For example, if the target well is vertical the bypass may be done at about 15 degrees and a drop planned after the closest approach point to run parallel with the target still in range.

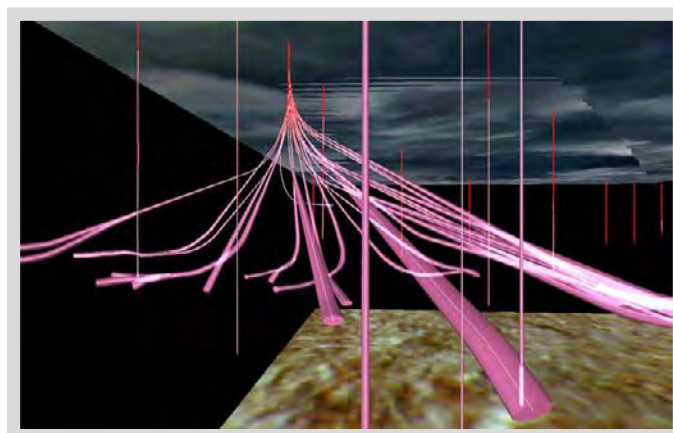


Figure 131: Ranging on crowded platforms

8. In some cases, the kill mud connection will be made by perforation and the accuracy of the intersection need only be a few feet but in many cases, the target well has to be milled. It is likely that the well control engineers will prefer a long milled notch in the target well casing. This means the well plan for the relief well will have to approach the well at an angle of 5 – 10 degrees and may need a casing included before the kill mud is deployed to avoid lost circulation under the kill mud pressure. Again the space for this approach to the kill point has to be adequate to accommodate the final section known as the 'gun barrel' section and this must not be close to any other wells. It is also important that this point is in stable rock just above the reservoir to ensure that the action of pumping kill mud does not fracture the formation so badly that another escape route is opened up for the reservoir fluids.

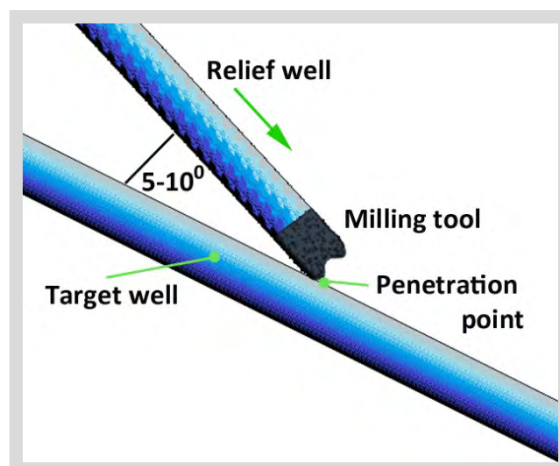


Figure 132: Relief well penetration point

9. As is clear from the diagram above, the final approach section will be steered and yet it is critical that this steering is of the highest accuracy. It is actually better when aiming a milling tool to aim slightly anticlockwise of the casing centre to ensure that the clockwise milling action does not 'roll off' the casing on contact. In order to steer accurately when this close to casing, it may be necessary to use GWD on approach to the final casing shoe especially if the inclination is not close to vertical as the azimuth uncertainty could jeopardise the kill run. After the final casing shoe is in place, there is very little steering ability and the success of the kill is dependent on accurate placement of the casing.
10. It is worth noting that a relief well contingency plan will be pointless if the original well is not surveyed with sufficient accuracy AND frequency. When the ranging shots are taken, the entire trajectory is shifted to fit the relative position discovered by ranging. A new relief well plan is generated every time a ranging shot is taken and a new kill point is interpolated in the target well survey. If the original survey is only available every 500ft, it is impossible to predict where the well will be between surveys and the kill could fail due to unmeasured doglegs creating unforeseen deviations in the well path.



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## 28. Subsea Positioning

For Offshore wells, the accuracy of the well coordinate is based on the accuracy of the surface and underwater positioning systems. These days, the surface positioning is invariably done using DGPS and this contributes very little (<1m) to the overall accuracy. However, this accuracy only describes the accuracy of the DGPS antenna position. This will not therefore be the accuracy of the final wellhead position.

**This section describes the process and the likely accuracies of the process depending on water depth.**

### 28.1 GPS Positioning

GPS positioning uses orbiting satellites as a reference. On board each satellite is a very accurate clock and a transmitting radio. These are powered by batteries with solar panels which charge up the batteries while the orbit is in sunlight. Once a second, each satellite emits a signal with its ID and time. (The clocks are deliberately set fast to compensate for the curvature of space time to keep up with time on the earth. If they were not, GPS would drift by about 4km per day).

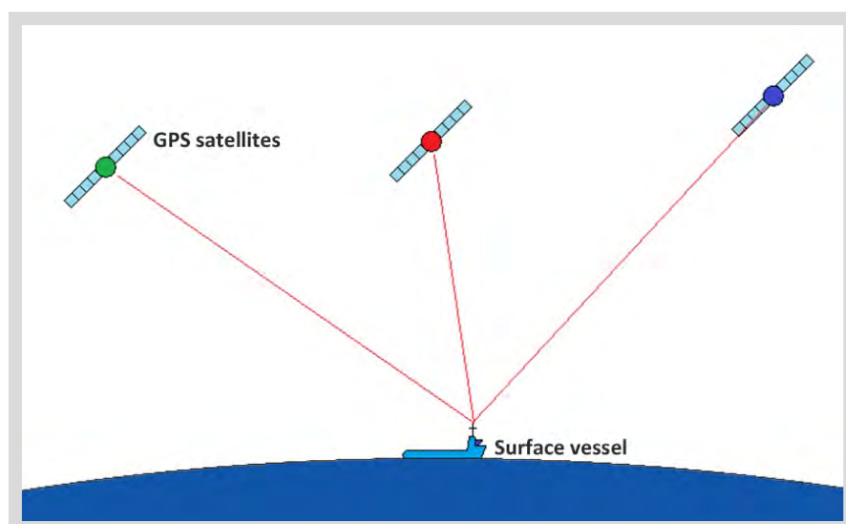


Figure 133: Satellite positioning

In each receiver, software knows the equations of the orbits of each satellite and calculates exactly where the satellite was when the signal was transmitted. It is also time synchronised with the satellites and therefore can measure the time difference from transmission to reception which is converted to a distance in 3D space. This distance from the satellite location defines the radius of a sphere with its centre at a known latitude, longitude and height above the centre of the earth. Two spheres intersect with a circle and three or more define unique points on the surface of the earth. This raw position is good to about 5m. For oilfield positioning this is not sufficiently and so usually, the survey company will employ differential GPS.

### 28.2 DGPS

Differential GPS uses a local (within 500km) fixed GPS receiver as a reference station. The fixed station observes its position over a much longer period and knows its own coordinates very well. When a new signal is received, it observes the position and calculates a local correction which is then transmitted to all other DGPS receivers in the vicinity. In this way, our dynamic unit can observe its position as above but then listen for a correction signal from the fixed station. Once the latitude and longitude are corrected, the position is usually good to about 0.1m. This is usually adequate accuracy for oilfield positioning applications. If greater accuracy is required, a more expensive system known as Real Time Kinematic (RTK) can be used which also makes use of the observed frequencies of the incoming signals which are affected by Doppler shift based on the relative velocity of the satellite orbit to the receiver. This is used in the mix to improve the observation accuracy and often results in position uncertainties of the order of 0.01m.

## 28.3 Vessel Offsets

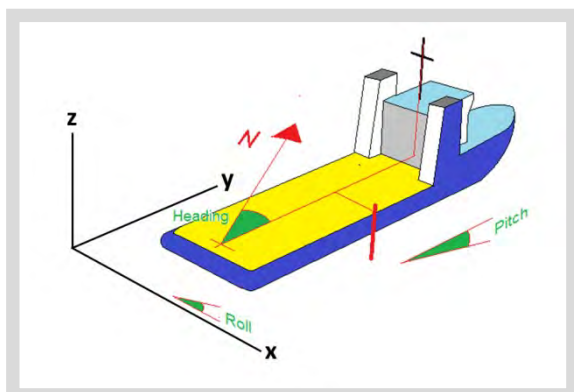


Figure 134: GPS considerations on vessels

The GPS position is the position of the antenna. However, at the instant the position is taken, the vessel will have a given heading and may also have a pitch and roll angle. These are observed with gyros and accelerometers and the offsets to any point of interest can then be converted from the ships reference where X, Y and Z are starboard, forward and above keel draft to a shift in real world coordinates in East, North and Height above sea level. For this to be done accurately, the offset distances need to be correctly tape measured or taken from accurate drawings and the vessel motion reference unit (MRU) has to be accurate in pitch roll and heading. For long offsets this can add another metre or two of uncertainty depending on the vessel size.

It is important that the marine survey report includes a section on expected accuracy of offset calculations based on the instruments and measurement methods used. This information should be submitted to the SFP and be understood by the SFP. A simple sign convention error on offsets can translate into a very significant subsea positional error.

## 28.4 Acoustic Positioning

The speed of sound in water is about 1500 m/s. Acoustic positioning systems measure the time taken for an acoustic pulse to travel from an emitter to a receiver and convert it to distance. A so called long baseline acoustic array is a set of acoustic transponders (AT) dropped to the seabed that can measure distances between themselves or distances from any mobile transponder such as on a Remote Operated Vehicle (ROV) to navigate relative to the array. Ultra Short Baseline Acoustics use multiple (at least three) high accuracy receivers to measure, not just the distance, but can also use the phase difference of the incoming signals to determine the horizontal and vertical angle to the source.

In order to establish the position of any permanent acoustic transponders on the seabed, two techniques are commonly used. These are 'Boxing In' and USBL.

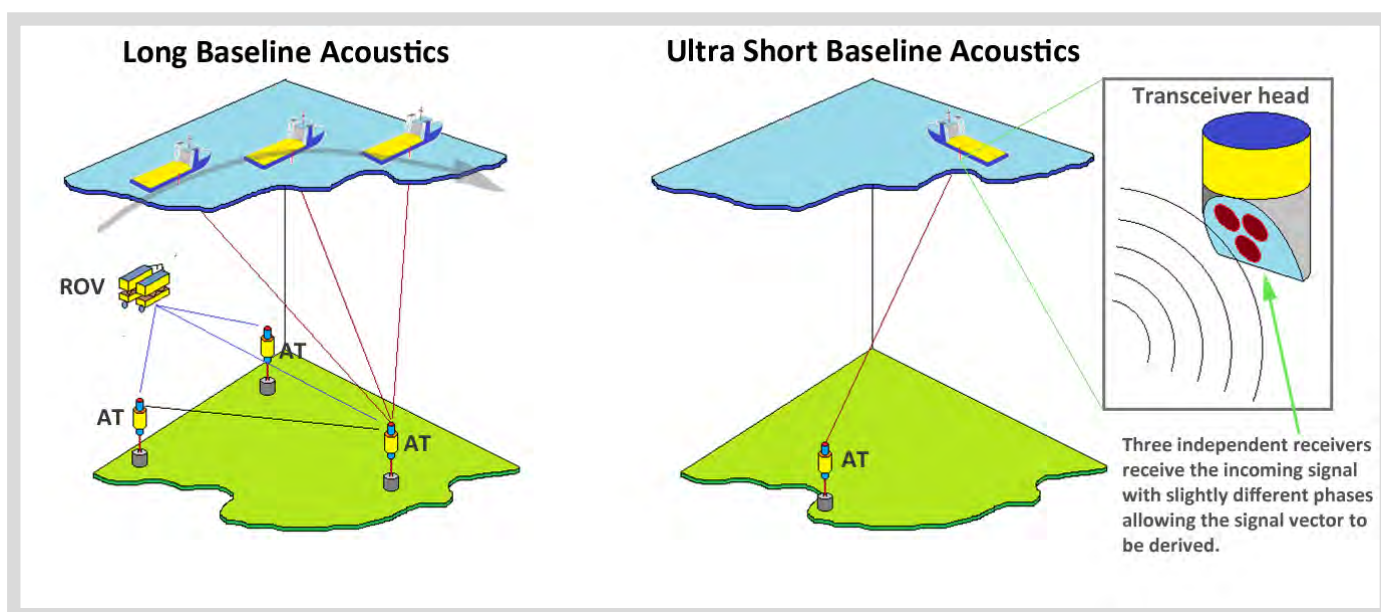


Figure 135: Baseline Acoustic Array

## 28.5 Boxing In

This is simply a series of distance measurements taken from a surface vessel to a transponder on the seabed. The vessel will use DGPS at surface along with the Gyro and Pitch and Roll to determine a location for a hull mounted transponder when each measurement is taken. This provides a series of surface locations and 3D distances to the transponder. The boxing in process finds the best fit position for the seabed transponder to fit the multiple observations. To minimise systematic errors, the vessel usually sails in a circle around the transponder so that any scale factor error or depth error tends to cancel out as observations are taken from all directions. For critical operations like Relief well drilling it useful to ask the marine survey contractor for the standard deviation of the box in results. This will usually result in a circular uncertainty envelope that follows the same rules as the 1, 2 and 3 Standard Deviation (SD) probability distributions we are familiar with.

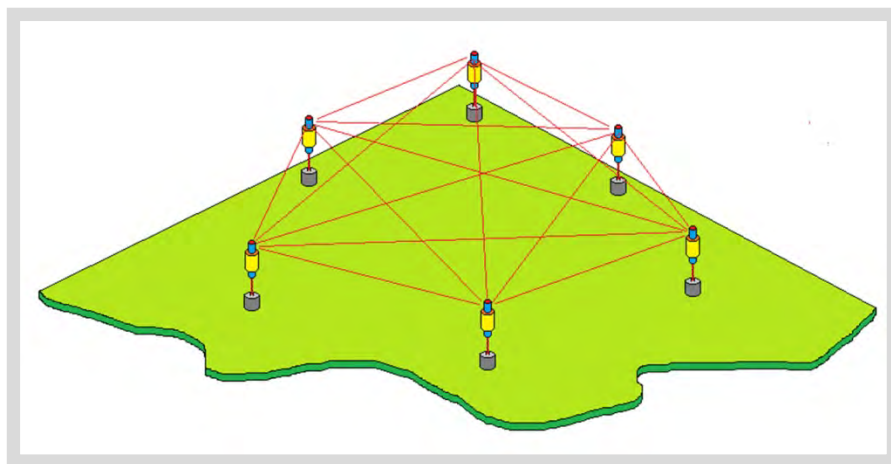


Figure 136: Networked Acoustic Array

With Long Baseline arrays, a signal can also be sent to each transponder in turn to measure the distance to all the others. This is usually accurate to a few centimetres and is adjusted for a best fit network to match the box in and the internal baseline observations. However, it should be noted that the network adjustment only provides a very accurate relative position of the array.

The absolute position and the orientation (which can be crucial for relief well positioning) are still dependent on the quality of absolute positions of the individual transponders. The final absolute position may well be established by taking a weighted average of the transponder positions and fitting the final network to the same average. Similarly, the orientations of each transponder may be calculated from the new centre and the network rotated to fit the average orientation. These processes will inevitably result in uncertainties for the array which will translate into surface position uncertainties for any ROV positions or spudding positions if a transponder is used on the drillstring.



## 28.6 USBL

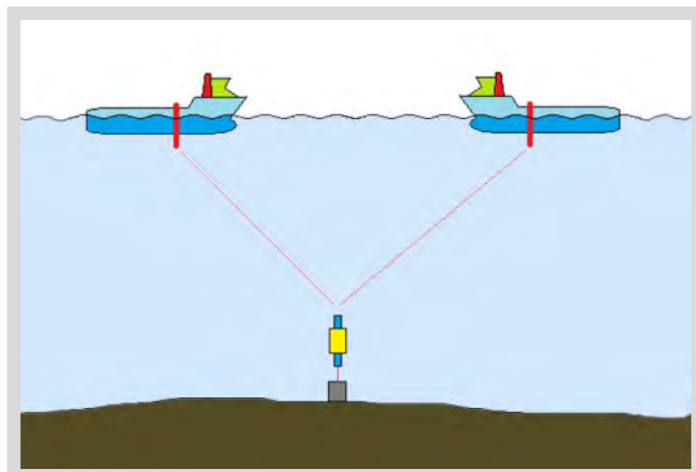


Figure 137: Reading a permanent seabed AT by vessel

Ultra Short Baseline systems measure the time taken for a signal to travel to the transponder and return but they also measure the phase difference of the incoming response between multiple receivers. This provides a 3D vector from the USBL position to the transponder on the seabed. If the transponder is a permanently positioned unit, multiple USBL positions can be taken and the vessel observing the seabed position will take readings with the vessel at two opposing headings. The effect of this is that any pitch or roll error will be the opposite if the heading changes by 180 degrees and the resulting seabed position is unaffected. The final scatter of results is averaged out and the first estimated position for the subsea transponder is established. This will be further improved by a subsequent network adjustment and so there is not much difference in the final accuracy of the seabed array.

### Procedures for establishing offshore position.

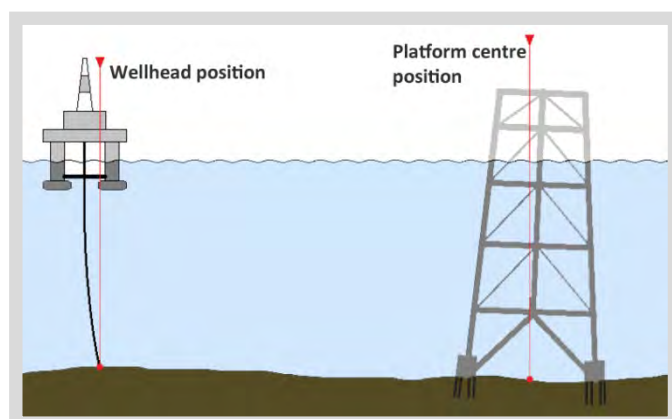


Figure 138: Wellhead and Platform coordinates

When spudding an offshore well or positioning a jackup or jacket, the final seabed coordinate will be the definitive position used for future drilling operations. This is unlikely to be exactly beneath the centre of the topside structure due to ocean currents, tilting, piling limitations or spud can penetration differences. In deep water, even a 0.5 degree tilt will create a shift of about 1% of water depth. Once the spud or the jacket upending is complete, the final coordinate is simply copied to surface and the wells are assumed vertical above the seabed. Not only do we inherit the coordinate from the subsea operation but we also inherit the uncertainty.

For Long Baseline acoustic positioning this is likely to be of the order of .5% of water depth at 1 SD and for USBL it is likely to be 1% of water depth at 1 SD. In the absence of a detailed marine survey report demonstrating otherwise, these figures should be used.

## 28.7 Section Summary

Subsea positioning accuracy is dependent on the equipment used, the water depth, and the absence of human error in the taping and recording of offsets. It is important that the SFP communicates well with the marine survey department to ensure the following

1. That both departments are using the same [coordinate reference system](#) and [datum](#)
2. That vertical references are clearly understood and agreed
3. That the method of calibration of seabed arrays is understood and adequate for the job

4. That a clear report is produced of the final positions and their uncertainties
5. That subsea well positions and not topside centres are used for well coordinates



***CONTENTS***



## 29. Wellbore survey quality control

*The information presented in this chapter is based largely on SPE papers<sup>1-3</sup> by Ekseth et al which were the result of a collaborative work on wellbore survey quality control within the SPE Wellbore Positioning Technical Section (SPE-WPTS), formerly known as the ISCWSA, to which the reader is referred for further details on this topic.*

### 29.1 Introduction

Well path position uncertainty estimates, discussed in Chapter \*, are used to determine if there is an adequate probability of hitting the geological target, of avoiding collision with offset wells, and of drilling a successful relief well in the event of a blowout. These are high value decisions and they depend heavily on the validity of the uncertainty estimates. However, error models are based on many assumptions. If the actual survey data are not acquired in conformance with these assumptions, the uncertainty estimate is invalid and it can no longer be assumed that the directional objectives for a well are being met. For this reason, it is dangerous to place any trust in an error model without an accompanying set of validating quality control (QC) measures. Therefore, a comprehensive set of QC measures, derived from the model, is required.

Various methods of QC are possible, including:

- Georeference tests whereby measurements of the Earth's gravity field and its magnetic or spin field, derived from the tool's sensors, are checked against independent measurements or estimates of these quantities.
- Multi-station analysis of reference field measurements; an extension of georeference tests which becomes an option after measurements have been collected at multiple survey stations.
- Tests based on repeated or duplicate measurements at the same survey station and in-run/out-run comparisons.
- The use of independent data in the form of an overlapping survey provides additional reliability; the error models predict how well the orientation measurements and calculated positions provided by the respective surveys should agree.

Although it cannot identify all potential errors, a second independent survey is the most powerful QC check. This chapter describes a comprehensive set of both the georeference QC tests and independent survey QC tests, including their limitations and operational recommendations. A few error sources, mainly linked to human inputs, cannot be fully tested by such data checks. They should in addition be subject to systematic manual cross checking to justify fully the use of a claimed error model. The highest level of reliability is achieved by the application of all of the QC techniques outlined here.

The proposed QC tests are intended to demonstrate that a directional survey does not contradict its error model uncertainty estimates. The limit values used in the tests must therefore be derived from the relevant model, and there is a need for an industry agreed confidence level. If applied correctly and consistently, the methods described here are capable of assuring valid attitude and positional data, and should be incorporated into standard operational practices.

## 29.2 Standardized confidence level

The QC methods described here are based on statistical tests to ensure that directional survey measurements have an accuracy that is compatible with the applicable error model. The testing is based on the assumption that the measurements have known statistical distributions. In accordance with the recommendations of the ISCWSA, measurements which deviate by more than plus or minus three standard deviations ( $3\sigma$ ) from the expected value are classified as gross errors (noisy measurements); and should be ignored. Only measurements falling within the  $\pm 3\sigma$  interval should be used to calculate wellbore orientations and positions.

All QC tests and examples presented here are based on the availability of a dedicated error model, the assumption of Normally distributed measurements, and the use of a  $3\sigma$  test limit is commonly adopted. For a Gaussian one-dimensional error distribution, a  $3\sigma$  limit corresponds to working at a 99.7% confidence level provided the basic geometrical requirements for the test are fulfilled.

## 29.3 Georeference QC tests

Downhole survey tools measure their attitude with respect to the Earth's gravity field and its magnetic or spin field (georeferences). A survey tool's error model predicts how well the measured field values should agree with the theoretical fields derived as functions of the latitude and depth at which the survey is performed. Compliance of the survey data with these criteria implies compliance with the inclination and azimuth accuracy assumptions of the model. When applied to individual stations this method is very cost effective, since it requires no significant additional data acquisition time and no additional processing effort. However, as will be described, the reliability of this type of test is very dependent on the wellbore and tool attitudes. Detailed mathematical descriptions of these tests are given in reference 1.

**Gravity error test.** The measurements provided by three axis (xyz) accelerometer packages can be used to determine the magnitude of the local gravity, in addition to the inclination and toolface of the survey tool. The local gravity ( $G$ ) is calculated using the equation:

$$G = \sqrt{G_x^2 + G_y^2 + G_z^2}$$

where  $G_x$ ,  $G_y$  and  $G_z$  are the three accelerometer measurements.

The local gravity is usually known with high precision, given knowledge of the local latitude, elevation, and vertical depth of the tool. It is therefore possible to calculate the error in the gravity estimate by subtracting the known value of local gravity from the measured value formed using the accelerometer measurements. The gravity estimation error can be used as a QC measure for the accelerometer package performance at each survey station.

The absolute gravity error value is tested against a tolerance level which is related to the error model inputs at a  $3\sigma$  confidence level. The gravity error test will then classify a survey station as a good station if the measured gravity error falls within the tolerance interval and as a bad survey station if it falls outside this limit.

The sensitivity of the gravity error to a particular accelerometer error is dependent on the tool orientation. The inclination and toolface errors created by individual sensor errors are also dependent on tool orientation. However, the orientation dependency of these errors is different from the gravity error dependency. For example, for a survey tool that is vertical, a z-accelerometer bias has a maximum effect on calculated total gravity field but a minimum effect on inclination. The converse is the case if the survey tool is horizontal. The large and small differences in the measured gravity field for the vertical and horizontal tool cases respectively are depicted in Figure 1.

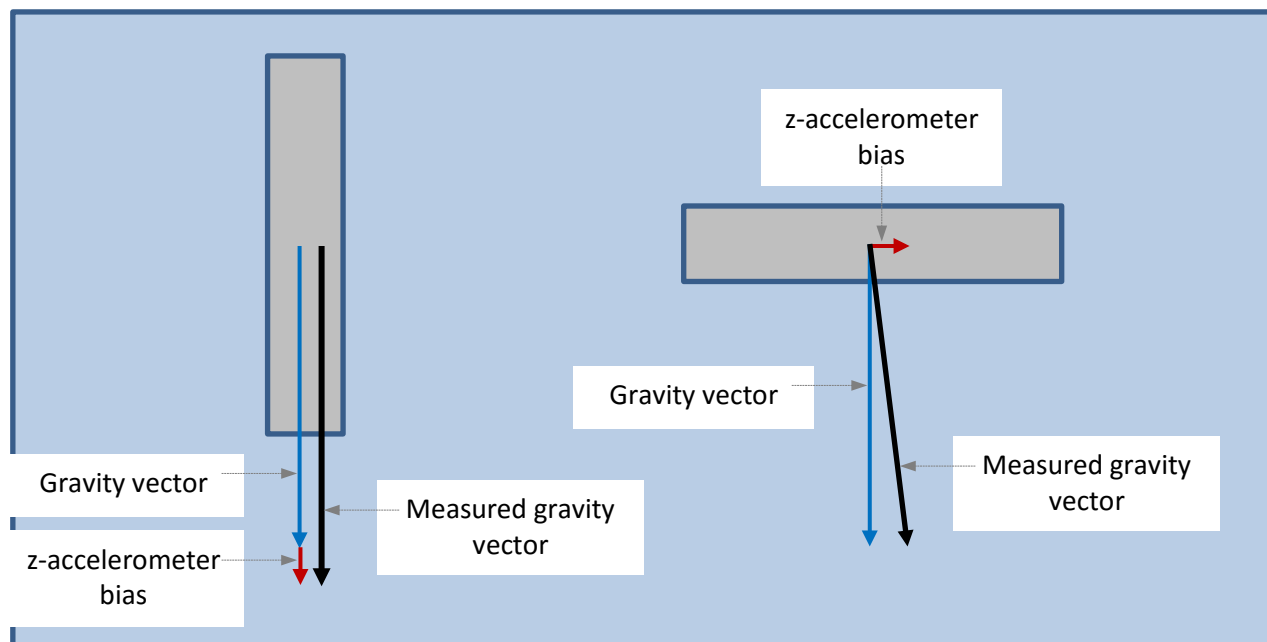


Figure 1: Detection of z-accelerometer bias – tool vertical and horizontal

Detailed analysis of the inclination, toolface and gravity error weighting functions shows that the gravity error test works optimally when the inclination is 45°, and the toolface angle is 45°, 135°, 225° or 315°. In these orientations, the statistical probability that test will indicate a good survey station when the accuracy of both the inclination and toolface estimates are consistent with the error model is greatest. In other words, the results are less likely to be offset by gross accelerometer errors, and indicate a bad survey station when the inclination and/or toolface errors fall outside the limits defined by the error model.

**Earth rate tests.** Modern north-seeking gyros determine azimuth by measuring orthogonal components of the Earth's spin vector in a process referred to as gyrocompassing; described in Chapter 9 and 10. Various gyro packages are used and, dependent on the particular sensor configuration adopted, are also capable of providing estimates of the turn rate of the Earth, or the horizontal or vertical component of Earth's rate. These quantities can therefore be used as gyro quality control measurements in the same manner as the gravity measurement may be used for the accelerometers.

For example, many gyro survey tools use an *xy* gyro only which provides measurements of the angular rate components about the *x* and *y* axes of the survey tool. In addition to the estimation of azimuth, these measurements can also be used to generate an estimate of the horizontal component of Earth's rate using the following equation:

$$\Omega_H = \sqrt{(\omega_x \cos \alpha - \omega_y \sin \alpha)^2 + \left( \frac{\omega_x \sin \alpha + \omega_y \cos \alpha - \Omega \sin \phi \sin I}{\cos I} \right)^2}$$

where  $\omega_x$  and  $\omega_y$  are the gyro measurements,  $\phi$  is the local latitude,  $I$  is the inclination of the tool and  $\alpha$  is the toolface angle. The true value of this quantity is usually known, and it is therefore possible to calculate a horizontal rate error,  $\Delta\Omega_H = \Omega_H - \Omega \cos\phi$ , and to use this as a gyro QC parameter. Analysis has shown that the reliability of the horizontal Earth rate test is very dependent on the tool orientation, not only inclination and tool face but also azimuth. The horizontal Earth rate test is optimal when the inclination is  $45^\circ$  (or  $135^\circ$ ), and the azimuth and toolface are  $45^\circ$ ,  $135^\circ$ ,  $225^\circ$  or  $315^\circ$ . It becomes singular at both poles, and where the well is vertical or horizontal, and therefore has no value at or close to these locations/orientations. The test has further weaknesses when the survey tool is located in a north/south or an east/west well. Examples are given in SPE 103734<sup>1</sup>.

For gyro survey tools which provide angular rate measurements about three orthogonal axes, it is possible to conduct additional gyro tests; a total Earth rate test and a latitude test. Unlike the other tests discussed here, the total Earth rate and latitude tests are not described in the QC reference papers<sup>1-3</sup>.

**Total Earth rate test.** For a stationary xyz gyro tool, the gyro measurements of angular rate about the three orthogonal axes (xyz) can be used to determine the total Earth rate ( $\Omega$ ) using the equation:

$$\Omega = \sqrt{\omega_x^2 + \omega_y^2 + \omega_z^2}$$

where  $\omega_x$ ,  $\omega_y$  and  $\omega_z$  are the three gyro measurements. It is therefore possible to determine the error in the Earth rate estimate and to use this quantity as a gyro package quality control parameter.

**Latitude test.** For an xyz gyro tool, a further test can be conducted. The dot product of the measured gravitational and Earth rate vectors can be used to provide an estimate of the local latitude. The equation for latitude as a function of the accelerometer and gyro measurements is as follows:

$$\phi = \arcsin \left[ \frac{G_x \omega_x + G_y \omega_y + G_z \omega_z}{G \Omega} \right]$$

The error in the latitude estimate generated using the gyro and accelerometer measurements is derived by comparing the estimated latitude with the known latitude of the well site. This quantity may then be used as a further quality control parameter for both the gyro and accelerometer packages.

For a survey tool that provides measurements about the xyz axes, the total gravity test controls the accelerometer package performance, the total Earth's rate test controls the gyro package performance, and the latitude test provides combined control of both sensor packages. Depending on the particular system mechanisation used, the combination of these tests results in a very robust quality control of survey accuracy during operation of the tool, independent of the well trajectory.

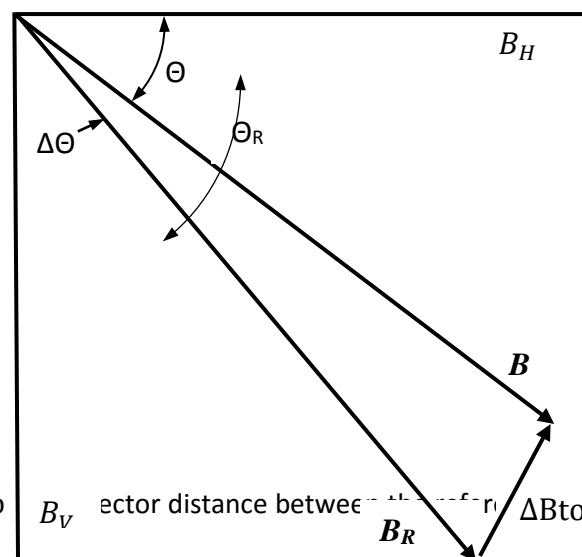
**Magnetic total field and dip tests.** State-of-the-art magnetic instruments make use of xyz magnetometer and xyz accelerometer packages to determine magnetic azimuth; true azimuth is determined subsequently given knowledge of magnetic declination at the well location. Control of the accelerometer package has already been described. It is also necessary to verify the performance of the magnetometer package in order to gain some control of the azimuth estimation process. Magnetometer packages are capable of measuring the Earth's magnetic field strength ( $B$ ) and its dip angle ( $\theta$ ) in addition to the azimuth, where:

$$B = \sqrt{B_x^2 + B_y^2 + B_z^2}$$

$$\Theta = \arcsin \left[ \frac{G_x B_x + G_y B_y + G_z B_z}{G B} \right]$$

and  $B_x$ ,  $B_y$  and  $B_z$  are the three magnetometer measurements. These quantities can therefore be used as magnetometer quality control measurements in the same manner as the gyro and accelerometer measurements can be used for the gyros and accelerometers. However, in this case, the same quantities are also used to check the quality of the magnetic reference, as discussed below.

An alternative test is sometimes conducted in which a quality control parameter  $\Delta B_{total-Dip}$  based on a combination of the measurement errors in total field and dip ( $\Delta B$  and  $\Delta \Theta$ ) is defined.



In the diagram,  $\Delta B_{total-Dip}$  is the vector distance between  $B_R$  and the measured field vector ( $B$ ), viz.

$$\begin{aligned} \Delta B_{total-Dip} &= \sqrt{(B_R \cos \Theta_R - B \cos \Theta)^2 + (B_R \sin \Theta_R - B \sin \Theta)^2} \\ &= \sqrt{(\Delta B_H^2 + \Delta B_V^2)} \end{aligned}$$

where  $\Delta B_H^2$  and  $\Delta B_V^2$  are the errors in the horizontal and vertical components of the Earth's magnetic field. The combined  $B_{total-Dip}$  test is useful for axially corrected surveys which have one less degree of freedom. Independent  $B_{total}$  and Dip tests provide more information with standard surveys.

The magnetometer tests are also subject to some geometrical limitations as occur when using other georeference tests since the various error contributions propagate in a different manner into the azimuth, the total field and the dip measurements. For example, these tests are unable to detect errors on a sensor axis which is aligned with the horizontal east/west direction.

It is noted that using the two Earth's magnetic field measurements as quality measures is not as straightforward as using the gravity and the Earth's rate measurements. The Earth's magnetic field is much more unstable and therefore less predictable than the other two measures. The magnetic tests are therefore required to control the reference itself, in addition to the magnetometer performance. Such tests make use of geo-magnetic models and are strengthened considerably by the application of in-field referencing techniques. However, the total field and dip measurements are unaffected by declination, an error parameter which has a major effect on the calculation of true azimuth. The total field and dip tests can therefore classify a bad survey station as good, even if a gross

declination error is present. The azimuth determined using magnetic surveys can never be controlled fully using this type of test.

## 29.4 Multi-station QC tests

The limitations of the georeference tests can be overcome, to some degree, with multi-station analysis of reference field measurements as outlined below. Clearly, such tests can only be conducted when measurements are available from a number of survey stations from the same survey. Detailed mathematical descriptions of these tests are given in reference 1.

**Multi-station accelerometer test.** The basic gravity error test can be expanded to a multi-station accelerometer test when xyz accelerometer measurements are available from a number of survey stations from the same tool. The major difference between the two methods is that the multi-station tests the magnitudes of the individual accelerometer errors, and/or the average resultant sensor error for each accelerometer, while the single-station gravity test tests only the lumped effect of all accelerometer errors. The multi-station test is therefore the more powerful of the two, but has the disadvantage that it can only be used after an extended period of drilling.

Analysis has shown that the quality of the multi-station test in terms of the number of individual error terms that can be estimated increases with a larger number of survey stations, and with increased variation in inclination and toolface. The test is of little or no value for surveys with only small angular variations, such as tangent section and/or constant toolface surveys. In these cases, the test mathematics will be singular, and strange results can be obtained. In such situations, it is better to use a reduced multi-station test with fewer error parameters<sup>1</sup>.

**The Multi-station Gyro Test.** This test can be used to estimate the biases and gravity dependent errors for dry-tuned dual-axis gyro systems, errors which tend to be less stable over time and can therefore vary following factory calibration of the survey tool. The test is also applicable, in principle, for survey tools that use other gyro types. The multi-station gyro test, like the multi-station accelerometer test, is subject to some geometrical limitations. The test is less effective for tangent section and constant tool face surveys, and for surveys of wells that lie predominantly in an east/west direction<sup>1</sup>.

A general test quality number, the standard deviation of the individual Earth's rate measurements, is generated as part of this test procedure. This figure becomes excessively large and causes the test to fail in the presence of gross errors in any gyro parameter including errors which are expected to be stable over time; errors which are not estimated individually by the multi-station procedure.

**The Multi-station Magnetometer Test.** This test can be used to estimate magnetometer biases and scale factor errors, axial and cross axial magnetization errors, and local magnetic field strength and dip errors. The total number of parameters is large, and some terms are closely coupled to each other. A reduction in the number of estimated parameters is frequently implemented to avoid mathematical correlation problems and to obtain results that can be trusted. For this reason, this test is less reliable than the equivalent accelerometer and gyro tests.

The multi-station magnetometer test can be slightly strengthened if merged with the multi-station accelerometer test into a full multi-station analysis<sup>4-8</sup>. The application of in-field referencing (IFR) further strengthens both this process and the single-station magnetometer test described above.

## 29.5 Repeated measurement QC tests

The shortcomings described in the previous sections demonstrate that a QC system based purely on georeference comparison and/or multi-station QC tests is not adequate to prove that a given survey is performing within the assumed error model. Significant error sources, including errors in depth, magnetic declination, continuous gyro drifts, drill string sag, and often survey tool misalignment, are uncontrolled with these tests. Additional QC tests based on repeated or duplicate measurements at the same survey station, in-run/out-run comparisons and comparisons with independent overlapping surveys are therefore vital to QC these additional terms. Repeated measurement tests are discussed here and the application of independent overlapping surveys is described in the section which follows this.

**The rotation-shot misalignment test.** It is necessary to control the misalignment and the gravity driven sag errors, in addition to controlling the accelerometer sensor errors, in order to document the quality of an inclination measurement. Since accelerometer tests are not sensitive to misalignment and sag, further tests are required. The rotation-shot-misalignment test has been developed to control toolface dependent misalignments; it does not QC the survey against sag errors.

The test is built around repeated inclination measurements taken at different tool faces at the same depth. Different tool faces are usually achieved by rotating the drill-pipe between the measurements. Therefore, the test is only suited for MWD and for gyros run at a locked orientation inside drill-pipes. It is noted that the accelerometer package should always be tested, using the methods described earlier in relation to accelerometer testing, and accepted prior to running this test.

**Rotational Check-Shot Test.** A series of measurements taken at different tool faces at a common depth forms a basis for additional tests that investigate the stability and tool face dependence of measured magnetic field strength, dip angle, and azimuth. Tests of this type have been employed for many years to detect and in some cases to correct for transverse magnetometer errors that might arise from drill collar hot spots.

**Dual Depth Difference Test.** The depth measurement is regarded as the most difficult directional surveying parameter to QC fully against gross errors. There exists no reference measurement in this case. The only possible downhole QC measurement is, therefore, an independent depth measurement, and this is usually not available for single surveys, for example for MWD, gyro while drilling and drop gyros. The only exception is for wireline gyro surveys run with a casing collar locator (CCL) inside casing or drill pipe. Two depth measurements, a wireline and a pipe depth measurement, are then available at every pipe connection. The depth difference at pipe connections between the pipe depth measurement and the associated wireline depth measurement can be used for QC.

**The In-Run/Out-Run Misalignment Test.** This test can be used to detect and secure against severe misalignment errors in continuous surveys, where the internal rotation-shot misalignment QC test is usually inapplicable<sup>2</sup>. Because tool face rotation is necessary to estimate the misalignment components, this test is suited only for surveys with gradually changing tool face, such as wireline surveys run on roller centralizers. Other misalignment tests have to be used for surveys with constant or near to constant tool face.

The in-run/out-run misalignment test can only be used if both in-run and out-run survey data exist for the entire survey section. Both the in-run and the out-run data should be proven free from gross accelerometer errors by applying internal QC testing, such as the gravity error test or the multi-station accelerometer test before running this test.



The in-run/out-run misalignment test makes use of the in-run/out-run inclination differences taken at the same depths as the fundamental QC measurements. It is, therefore, essential that the in-run and out-run depths at which the measurements are taken correspond to the same location in the well.

**The Continuous Azimuth Drift Test.** Continuous gyro and inertial navigation system (INS) surveys have an accumulative azimuth error behavior<sup>9-10</sup>, and it is not practical to QC each individual azimuth output. It is more convenient to examine the propagation of the azimuth error over the entire survey, and the continuous azimuth drift test has been developed precisely for this purpose<sup>2</sup>. It makes use of in-run/out-run azimuth differences to estimate the two recommended error model parameters, the linear gyro drift and the gyro random walk. To achieve this, the out-run azimuths ideally should be depth correlated relative to the in-run before running the test.

## 29.6 Independent surveys QC tests

**The Inclination Difference Test.** As indicated in the georeference QC section, the inclination cannot be controlled against gross sag errors, and often also not against gross tool misalignments, by the survey itself. External data, usually in the form of an independent overlapping survey, will be needed to fulfill this goal. The inclination difference test, which is based on two independent overlapping surveys, has been developed to obtain control over the sag and misalignments. It does not test the sag and misalignment errors directly but looks at the resultant effect of all error sources affecting the inclination accuracy. The test is only capable of indicating that something is wrong with the inclination estimate in at least one of the two surveys being compared. It cannot be used to detect the specific error source that may be affecting the outcome of the test.

The inclination difference test is a Chi-squared test<sup>2</sup> designed to detect systematic inclination differences present throughout the survey. It is stressed that the test relies totally on independence between the two inclination measurements used to form each inclination difference, which means that the two overlapping surveys must be performed with different surveying instruments and running gear/bottomhole assemblies (BHAs).

Figure 2 shows the inclination profile and the inclination differences between a magnetic MWD survey and a drop gyro survey. The jumps in the inclination differences may either be caused by depth differences or BHA dependent inclination errors like the sag. The depth difference option was ruled out in this case, and it became important to determine whether or not the inclination errors giving rise to these inclination differences were in accordance with the error models. A 15 station inclination difference test was run to address this question. The resulting Chi-square test value of 102 is far greater than the associated tolerance level of 34, and it is concluded that gross inclination errors are present in at least one of the two surveys.

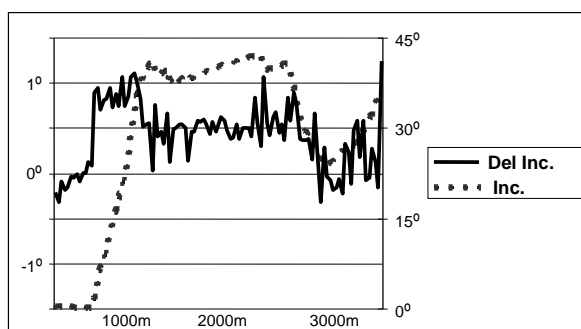


Figure 2: Inclination differences between a drop gyro survey and consecutive MWD sections

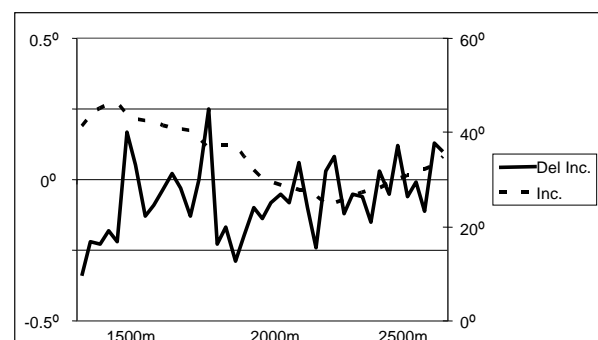
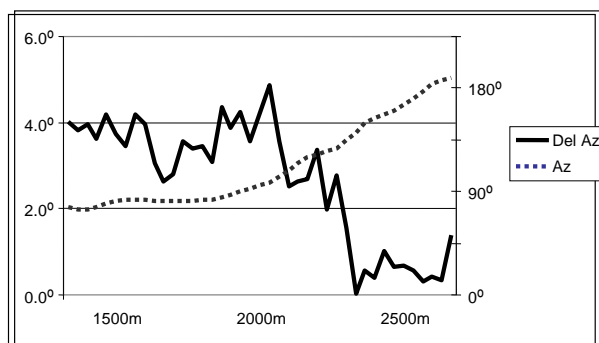


Figure 3: Inclination differences between a continuous gyro survey and a MWD survey

Another example of inclination differences is shown in Figure 3. A 15 station inclination difference test was conducted resulting in a Chi-square test value of 16, approximately half of the tolerance level of 34. Because the error model estimates for the performance of both systems are similar in size in this case, it can be concluded that both surveys are in accordance with their respective error models.

**The Azimuth Difference Test.** The azimuth difference test is based on the same mathematical principles as the inclination difference test. A three station azimuth difference test run immediately after a bit run is an excellent check against severe BHA magnetization errors and is generally recommended in connection with any bit run that involves a significant BHA change.

An error in the magnetic declination is an example of a potentially significant azimuth error that only can be verified through an independent overlapping non-magnetic survey. The azimuth difference test has been developed for this task. It does not estimate the declination error directly, but it is capable of indicating that something is wrong with the azimuth in at least one of the two surveys involved. Other QC tests are needed to identify the real cause of a failed test.



# Figure 4: Azimuth differences between a continuous gyro survey and a MWD survey

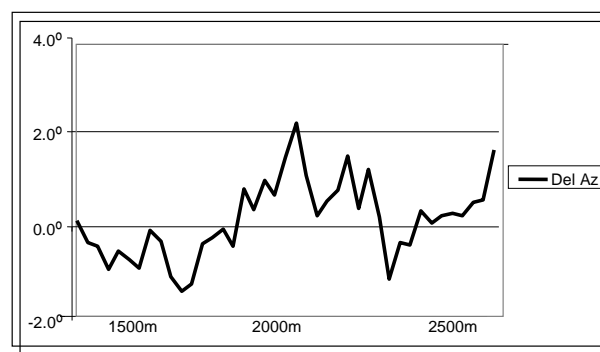


Figure 5: Azimuth differences after MWD multi-station correction for same surveys as in Fig. 4

Figure 4 shows the azimuth profile and the azimuth differences between the same two surveys used in the second inclination difference test example. The jumps in azimuth differences are not consistent with the behavior that would arise through depth differences, and they must, therefore, have their origin in real azimuth errors in one or both of the surveys. The question is whether these errors are too large to satisfy the error model.

A 15 station azimuth difference test was run resulting in a Chi-square test value of 112, substantially greater than the tolerance value of 34. The test fails, indicating that gross errors affecting azimuth estimation must be present in either one or both of the surveys. This result also serves as a reminder that a pass of the inclination difference test cannot be taken as evidence that the azimuth estimates also lie within acceptable bounds. To isolate the cause of this failed test, the MWD survey was run through a magnetic multi-station estimation process that removed most of the azimuth differences, as can be seen from a comparison of Figures 4 and 5.

A repeat of the 15 station azimuth difference test with the multi-station corrected MWD data resulted in a Chi-square test value of 9.7, well within the tolerance level. The test is now passed, and it can be concluded that the multi-station corrected MWD data did perform within the tolerances defined by the expected MWD error model. The errors predicted by the gyro error model are much smaller than those predicted by the MWD error model. In view of this fact, it is not possible to conclude for certain that the continuous gyro survey is performing within its error model.

**The Coordinate Difference Test.** This is another useful test based on the same type of Chi-square statistics used in the inclination and azimuth difference tests, but it deals with lateral, along-hole, and vertical positional differences instead of inclination and azimuth differences. For optimal performance, the independent survey QC process should include inclination, azimuth, and coordinate difference tests, and constitutes the most powerful survey QC tool available.

## 29.7 Recommended Use of QC Methods

This section provides an overview of the error terms that can be controlled using the various QC test described here and makes recommendations for an optimal sequence of tests to be performed at different stages of the drilling process<sup>3</sup>.

Table 1 indicates those error terms that can be quality controlled during or after each survey station/section using georeference comparison and multi-station tests, and those terms that can be controlled using repeated measurements and independent surveys tests. The table shows that a few highly significant error terms (continuous gyro drift, sag, and declination) can rarely or never be controlled or are very difficult to control, with georeference comparisons and multi-station tests. However, these error terms can be controlled using repeated measurements based on in-run/out-run survey comparisons and independent verification surveys. It is concluded that it is usually necessary to use one or more of the independent surveys tests to QC a survey fully with respect to its entire error model.

Error Source	Test Method			
	Georeference Comparison (1)	Repeated Measurement (2)	Multi-station Analysis (3)	Independent Surveys (4)
Accelerometers	Some control	Moderate control	Good control	Some control
Magnetometers	Some control	Moderate control	Moderate control	Some control
Stationary gyros	Some control	Moderate control	Good control	Some control
Continuous gyros and INS <sup>(5)</sup>	No control	Moderate control	No control	Some control
Misalignment	No control	Moderate control	No control	Some control
Sag	No control	No control	No control	Some control
Magnetic interference	Some control	No control	Moderate control	Some control
Magnetic reference: total field/dip	Some control	No control	Moderate control	Some control
Magnetic reference: declination	No control	No control	No control	Some control
Depth	No control	No control	No control	Some control

(1) Georeference Comparison includes comparison of the nominal values of Earth's gravity and magnetic field or rotation rate with the estimates of these quantities derived from the accelerometer, magnetometer, and gyroscope measurements; each test performed on a single-station basis.

(2) Repeated Measurements is analysis of the spread between several measurements made with the same tool, at the same depth, and within the same bit-run/wireline operation. Includes rotational shots and check shots made with the same tool, also comparison of the results from in-run and out-run continuous gyro surveys.

(3) Multi-station Analysis means that all measurements performed with the same tool in the same run are analysed simultaneously, thus achieving similar effects to methods (1) and (2) combined.

(4) Independent Surveys involves comparison of two or more surveys using different tools and different depth measurement systems. At least one of the tools must be a gyroscopic tool.

(5) Inertial navigation System

## 29.8 Concluding remarks

1. A combination of dedicated QC processes involving georeference checks relative to the local Earth's gravity, magnetic and rotation fields, multi-station tests, repeated measurements, and independent verification surveys are needed to ensure a survey reliability level consistent with the demands embedded in instrument performance/error models.
2. These QC procedures, together with a standardized 99.7% confidence level, should be incorporated into common practice for the design and verification of most wellbore survey operations.
3. Georeference checks, multi-station tests, and repeated measurements may protect against a wide range of potential gross errors and should be used to maximize the survey reliability whenever possible during a drilling process.
4. Georeference checks, multi-station tests, and repeated measurements with a single tool/BHA cannot detect gross errors in a few critical sources, like BHA sag and magnetic declination errors.
5. Multi-station tests can only be fully used after a long wellbore section has been drilled and several stations have been surveyed in significantly different attitudes.
6. Single-shot/rotation-shot georeference checks are usually weaker than multi-station checks, but are sometimes the only available QC options, for example, during kick-off operations and therefore, they should be used.
7. A data check, consisting of combined comparisons of inclinations, azimuths, and coordinates relative to an independent verification survey, is the most powerful QC test method available. Georeference checks usually have to be supplemented with data checks based on a comparison of inclinations, azimuths, and/or coordinates relative to independent verification surveys to ensure optimal survey reliability.
8. The value of checks relative to independent verification surveys depends on the degree of independence between the surveys. A verification survey is independent only as long as it is performed with a different survey method, a different survey tool, different running gear/BHA, and a different depth measurement system.

## 29.9 References

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## 30. Error model validation

### 30.1 Introduction

This chapter draws attention to the vital need for representative and justifiable error model inputs in the quest for safe and reliable surveying when using wellbore survey tools. The error model for a particular survey tool is intended to be representative of the average performance of a large number of surveys and for the well placement accuracy that can be expected using that tool for a planned survey. However, it is difficult to know whether or not these objectives are fulfilled unless the survey tool error model has been fully verified.

The use of non-verified error models may be adequate for assigning position uncertainties to surveys that can be tested relative to the chosen error model, with the help of the tests described in the chapter on survey quality control for example. Whether the error model used is valid for a large number of surveys is less important than whether it is valid for the given survey.

The use of non-verified error models is far more questionable if the error models are used to design optimal wellbore survey programs to ensure that the drilling target is intercepted in a safe and economical manner. The result might be the use of survey programs that are too comprehensive and overly expensive when the error models are too pessimistic, and give rise to an excessive number of failed surveys and/or bad wellbore placements when the error models are too optimistic. Methods are therefore needed to validate error models through the use of downhole data collected under real operational conditions. Such methods can be based either on direct measurements of the error terms involved, or on the comparison of multiple surveys in the same well.

The error model for a particular survey service is influenced not only by the choice of sensors and their configuration, but also by factors including the tool running configuration, choice of centralisation adopted, the platform from which the system is operated and the detailed operating/QC procedures applied when running the tool. It is therefore the responsibility of individual service companies to provide error model data based on the statistical analysis of real downhole data for each type of tool and service on offer. Simulation and theoretical analysis should be used wherever possible to support this process and so add credence to the statistical derivation.

### 30.2 Discussion relating to survey type

MWD makes use of the Earth's magnetic field as a reference in its azimuth calculations. The sensor errors present in modern MWD instruments are small in comparison to typical variations in the Earth's magnetic field, which constitutes a rather unstable reference. The MWD positional uncertainty is therefore, to a large extent, a result of environmental errors originating from natural fluctuations in the magnetic field and distortions caused by adjacent magnetic material, and not variable sensor quality. Knowledge and techniques on how to minimize the effects of the unstable magnetic reference have been known for many years, and the practical implementation does not vary significantly between the major MWD suppliers, who have focused on factors other than survey accuracy in their marketing. It was therefore possible to create an MWD error model<sup>1</sup> which has been accepted as an industry standard.

For gyro surveying, in which direction is determined with respect to the Earth's rotation vector, the situation is quite the opposite. State of the art gyro instruments are far less accurate than the stability of the Earth's rotation rate. Tool design and operational procedures vary significantly between the different suppliers, and survey accuracy is regarded as a competitive advantage. For these reasons, the SPE WPTS decided to provide the drilling industry with a framework for mathematical error modeling of gyroscopic survey tools<sup>2</sup>, and not to supply numerical error parameter inputs. It

was left to the gyro service providers themselves to supply the rest of the industry with the necessary gyro model inputs, mainly without any external industry accepted guidelines or review/audit processes in place.

In this situation, operators and directional drillers might believe they are operating within acceptable safety margins while, in reality, they may operate with critically low safety margins. In the following, validation methods based either on direct measurements of the error terms involved, or on the comparison of multiple surveys in the same well based on the statistical analyses of real downhole data are outlined. Specific examples are given of how realistic uncertainty estimates for some existing gyroscopic tools are obtained.

### 30.3 Validation through determination of individual error parameters

Many of the tests described in the QC chapter are based on the determination of one or more error model terms. It is possible to derive and to test existing error model inputs through statistical analyses of such QC results obtained from a large number of surveys originating from different sources and locations. However, it is important to remember that the accuracy of most of these methods is dependent on wellbore geometry and/or operational conditions. Only results from surveys matching the different test recommendations should therefore be used in such statistical analyses. An overview of the QC tests that can be used to derive the different error terms is given in Table 1<sup>3</sup>.

**Table 1: QC tests suites for individual error model error term measurement**

Error model terms	QC tests
Accelerometer biases Accelerometer scale factor errors (z component is difficult)	Multistation accelerometer test
Magnetometer biases Magnetometer scale factor errors Axial magnetisation Cross-axial magnetisation Total field strength error Dip error (The separate identification of all sensor and field errors is difficult)	Multistation magnetometer test
Gyro biases Gyro g-dependent errors Gyro random errors	Multistation gyro test
Survey tool misalignment	In-run/out-run misalignment test
Azimuth drift Azimuth random walk	Continuous azimuth drift test

Illustrations of the procedures adopted by one gyro service provider to generate error model validation data for a range of survey tool types is described in SPE paper 140192<sup>4</sup>. The following example describes how multistation test data are used to quantify the major errors that are expected to arise in a gyro tool that provides stationary surveys.

**Example 1.** The procedure described here relates to the validation of the gyro error model for a gyrocompassing tool equipped with a single dual-axis (xy) gyro.

In addition to the gyro random noise, the following important error sources for gyrocompassing with xy gyro systems are specified in the gyro error model; gyro bias, mass unbalance, gyro scale factor errors and gyro misalignments. These highly significant gyro error sources are measured and corrected for at least once at master calibration facilities for all gyro survey instruments operated by the company. The company also corrects for the following less severe, but still significant, sources of error: input axis g-sensitive error (quadrature effect), spin sensitivity and anisoelastic effects.

While most of these terms remain constant, the mass unbalance and the x and y gyro biases are known to change with respect to the master calibration and may produce large survey errors if left uncorrected. The company operating the tools and services analyzed here has developed a number of methods to control the time dependent errors, by embedding the following processes into the standard operational software and practices:

- z axis indexing
- multistation correction
- pre and post job field roll tests
- pre and post job base roll tests

These correction methods can be looked upon as simplified recalibrations of the survey tool. The z axis indexing is designed to remove x and y biases on individual survey station basis. However, many years of experience has shown that part of the biases, or bias-like lumped residual errors, may not be removed through the indexing process, and form apparent bias errors which tend to be systematic within a given survey and random between surveys. The company has implemented a horizontal Earth rate based multistation correction algorithm to measure and correct for the two apparent biases and the direct mass unbalance.

The drawback with this correction method is, as indicated in the quality control paper SPE103734, that it is not applicable for all wellbore geometries and running configurations. The multistation correction quality depends on latitude, the amount of inclination and toolface variation over the well section surveyed, and on the dominant horizontal direction of the well. The dependency is quite complicated, and it is often difficult to decide whether a multistation result can be trusted or not without some kind of numerical geometrical evaluation. An automatic test based on the actual latitude, the calculated correlation coefficients and the percentage of stations within an east/west sector, has therefore been integrated within the software. As a result of this procedure, the multistation correction will not usually work in connection with spring-bow surveys (no tool rotation), tangent section surveys and surveys of wellbores that lie predominantly in an east or west direction. Geometrical tests are conducted to identify these cases, and such surveys are recalibrated with an alternative method utilizing the pre and post job roll tests as described next.

Roll test data will be needed in addition to the downhole data to produce a result with the multistation correction software when the geometrical tests fail. Roll tests obtained at the drill site a short time prior to and immediately after a survey (field roll tests), are generally more consistent than roll tests conducted over a larger time span, tests performed at the warehouse prior to shipment and after return (base roll tests) for



example. Field roll tests are therefore preferred, but experience shows that acceptable field roll tests may be difficult to achieve on floating drill-rigs like semi-submersibles, and that it often is necessary to recalibrate with base roll tests when operating from these types of rig.

Regardless of which recalibration method is used, it is concluded from the discussion above that error models for all tools used in this study require only the following four sensor dependent gyro errors from the list of options given in the gyro error model paper<sup>4</sup>: the apparent gyro bias errors ( $GBX$  and  $GBY$ ), the direct mass unbalance error ( $M$ ) and the random gyro noise ( $RG$ ). Nevertheless, it is necessary to populate these terms with numbers derived independently for each of the recalibration methods. Both the multistation correction and the different roll tests provide estimates of  $GBX$ ,  $GBY$  and  $M$ , their standard deviations ( $\sigma GBX$ ,  $\sigma GBY$  and  $\sigma M$ ), and the random noise ( $RG$ ). The necessary numerical error model inputs can therefore be derived through statistical analysis of multistation correction results from the different surveys and tools.

The multistation corrected/uncorrected error models are most simple to derive since a one to one relationship exists between the test output and the input values required for these model inputs. A multistation uncorrected model must not be misinterpreted as an error model that can be used regardless of quality control level. As described above, multistation corrections will not usually be applied to surveys of east-west wells and tangent sections, or where the toolface does not vary significantly without the use of roll test data in the test. The uncorrected systematic parameters ( $GB_{uc}$ ,  $M_{uc}$ ) are given as the zero mean standard deviation of the actual corrections given in the following equations.

$$GB_{uc} = \sqrt{\frac{\sum_{i=1}^n GBX_i^2 + \sum_{i=1}^n GBY_i^2}{2n}}$$

$$M_{uc} = \sqrt{\frac{\sum_{i=1}^n M_i^2}{n}}$$

The corrected systematic parameters ( $GB_{co}$ ,  $M_{co}$ ) are given as the root-sum-square of the estimated standard deviation of the actual corrections given by the equations below.

$$GB_{co} = \sqrt{\frac{\sum_{i=1}^n \sigma GBX_i^2 + \sum_{i=1}^n \sigma GBY_i^2}{2n}}$$

$$M_{co} = \sqrt{\frac{\sum_{i=1}^n \sigma M_i^2}{n}}$$

In both cases, the random noise parameter ( $RG$ ) is given as the root-sum-square of the actual random output as defined in equation 7. It must be noted that only results passing the internal correlation coefficient and east/west tests should be used in these equations.

$$RG = \sqrt{\frac{\sum_{i=1}^n \sigma RG_i^2}{n}}$$

$GBX_i$	= systematic X bias correction applied to survey number i
$GBY_i$	= systematic Y bias correction applied to survey number i
$M_i$	= systematic mass unbalance correction applied to survey number i
$\sigma GBX_i$	= standard deviation of systematic X bias correction applied to survey number i
$\sigma GBY_i$	= standard deviation of systematic Y bias correction applied to survey number i
$\sigma M_i$	= standard deviation of systematic mass unbalance correction applied to survey number i
$\sigma RG_i$	= standard deviation of one gyro measurement - survey number i
$n$	= total number of surveys

The numerical values selected for these error parameters vary not only with the sensors used and their configuration, but also with the choice of running gear and the platform from which the system is operated.

The corrected model should always be employed provided that all QC requirements are satisfied; standard operating procedures dictate that the gyro measurements are always corrected using the multistation estimates of gyro bias and mass unbalance under such conditions. The uncorrected values serve purely to define the corrections applied ( $1\sigma$  values) following the successful implementation of the multistation correction QC procedure. It is noted that gyro biases propagate randomly for operation in a rotating survey tool, while bias propagation is systematic if the tool is not rotating. Mass unbalance always propagates as a systematic error, regardless of the running conditions.

Similar statistical analyses of other QC test results can be used to quantify other sources of error in survey tools. The following example outlines the use of data obtained using the in-run/out-run misalignment test described in the QC chapter.

*Example 2.* Consider  $n$  independent continuous gyro surveys from different sources/locations that have been run on roller centralisers, and that have all been subjected to the in-run/out-run misalignment test and satisfied the requirement of that test. Misalignment estimates  $MX_i$  and  $MY_i$  will then be available for each of these surveys ( $1 \leq i \leq n$ ). The individual misalignments all have zero expectation, and the standard deviations of the misalignment errors, the error model misalignment input, can be calculated using the following equation.

$$\sigma MX = \sigma MY = \sqrt{\frac{\sum_{i=1}^n (MX_i^2 + MY_i^2)}{2n}}$$

Surveys with known gross errors should not be used in this standard deviation calculation as they can distort the results substantially.

## 30.4 Indirect validation through the comparison of independent surveys

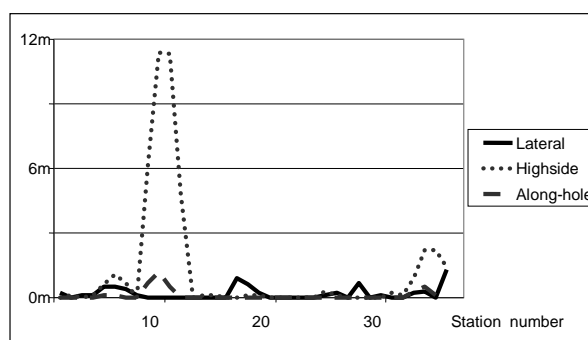
It is sometimes difficult, or even impossible, to verify a given error model through independent estimation of all individual error parameters from downhole data. The magnetic declination, the sag and the depth error terms are, as indicated in Table 1, examples of parameters that cannot be estimated directly. It is therefore necessary that a method for final error model validation be used in addition to individual error term validations. The framework for

the co-ordinate difference test can be used for this purpose. However, some equations and the test limits are slightly different, as described below. Both survey types used will of course have to have error models assigned to them.

The main difference between the basic co-ordinate difference test and error model validation is that the former is based on single sided Chi-square tests of a single pair of overlapping surveys, while error model validation is based on two sided tests of multiple sets of overlapping surveys of the same type originating from different wells.

To ensure that the random between survey behaviour takes precedence over the systematic between survey station behaviour, the number of overlapping survey stations used from each survey pair should be significantly smaller than the number of survey pairs used, but not so small that the random between station behaviour takes precedence. Four overlapping stations from each survey pair spread over the survey stations available for each run, and at least 10 survey pairs seems to be a good compromise. An example that illustrates how this method can be used as a partial validation of a non-downhole derived error model is given below.

**Example 3.** Overlapping survey data (same type) from 3 different wells are used here to illustrate how the coordinate difference test can be used to verify a given error model, which in this case is identical to the error model recommended by the service provider. Both co-ordinate differences from the same survey (in-run/out-run differences), and from two different surveys in the same well (in-run/in-run and in-run/out-run differences), are used. Four sets of co-ordinate differences (taken at 25%, 50% and 75% of TD, and at TD) were used in each case. They are shown in the following plot.



This provides a total of 36 test sets to combine. This is not enough for a final verification of the error model. Data from many more wells, including a substantial number of overlapping surveys made with different tools and different wireline units, would have been necessary to achieve a full verification. However, the data set should be sufficient to visualise the process of using the coordinate difference test for final error model validation.

In accordance with the Chi-square test procedure<sup>3</sup>, the coordinate differences scaled by the error model variances of the survey systems used are summed over the number of survey stations and the number of wells to give the following Chi-square test parameters. Along-hole, lateral and highside sums are denoted by the symbols  $X_L$ ,  $X_W$  and  $X_H$  respectively.

$$X_L = 6.6, X_W = 3.6, X_H = 44.2$$

Upper and lower tolerance limits for all three cases are selected corresponding to the Chi-square test value for  $n$  degrees of freedom with 95% significance ( $Z_{0.95,n}$ ), and the Chi-square test value for  $n$  degrees of freedom with 5% significance ( $Z_{0.05,n}$ ), where:

$$Z_{0.95,n} = 51 \text{ and } Z_{0.05,n} = 23$$

The along-hole and lateral sums are both smaller than the lower tolerance limit, while the highside sum is inside the tolerance limits. The results suggest that the recommended error model may be slightly pessimistic. However, such a conclusion may not be valid since these results are based on too few surveys, and on data that may be correlated between surveys, and therefore overly optimistic.

## 30.5 References

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# APPENDICES

## Appendix A: Details of the Mathematical Derivations

### A1 - Details of the Propagation Mathematics

Recall from section [19.2.5](#) that the core equation for the propagation of the errors from the error source through to the survey position error is:

$$e_i = \sigma_i \frac{dr}{dp} \frac{\partial p}{\partial \varepsilon_i} \quad (\text{A.1})$$

Where:

$e_i$  is the size of the error in NEV axis due to error source  $i$  at the current survey station

(a 3x1 vector)

$\sigma_i$  is the magnitude of the  $i$ th error source (a scalar)

$\frac{\partial p}{\partial \varepsilon_i}$  are the weightings functions, the effect of the  $i$ th error source on the survey measurements; md, inc and azimuth. (a 3x1 vector)

$\frac{dr}{dp}$  is the effect of the survey errors in md, inc and az on the wellbore position in the NEV axis, (i.e. a 3x3)

$$\text{matrix} \begin{pmatrix} \frac{dN}{dMd} & \frac{dN}{dInc} & \frac{dN}{dAz} \\ \frac{dE}{dMd} & \frac{dE}{dInc} & \frac{dE}{dAz} \\ \frac{dV}{dMd} & \frac{dV}{dInc} & \frac{dV}{dAz} \end{pmatrix}$$

So we need to be able to calculate the  $\frac{dr}{dp}$  matrix. Given that the survey measurements define the depth, inclination and azimuth at either end of an interval the position over an interval will depend on the survey measurements at two stations. If we write  $\Delta r_k$  for the displacement between survey station  $k-1$  and  $k$  and hence  $\Delta r_{k+1}$  for the displacement between stations  $k$  and  $k+1$ , then we can split  $\frac{dr}{dp}$  in to the variation over the preceding and following survey intervals and write:

$$e_{i,l,k} = \sigma_{i,l} \left( \frac{d\Delta r_k}{dp_k} + \frac{d\Delta r_{k+1}}{dp_k} \right) \frac{\partial p_k}{\partial \varepsilon_i}$$

Where:

$e_{i,l,k}$  is the error due to the  $i$ th error source at the  $k$ th survey station in the  $l$ th survey leg

$\frac{d\Delta r_k}{dp_k}$  is the effect of the errors in the survey measurements at station  $k$ , on the position vector from survey station  $k-1$  to survey station  $k$  and similarly

$\frac{d\Delta r_{k+1}}{dp_k}$  is the effect of the errors in the survey measurements at station  $k$ , on the position vector from survey station  $k$  to survey station  $k+1$

Although minimum curvature is the preferred method for calculating the wellbore positions, it is simpler to use the balanced tangential method to determine  $\frac{d\Delta r_k}{dp_k}$  and there is no significant loss of accuracy.

The balanced tangential model gives us the following equation for the displacement between any two survey stations  $j-1$  and  $j$  in *nev*-axes:

$$\Delta r_j = \begin{bmatrix} \Delta N \\ \Delta E \\ \Delta V \end{bmatrix} = \frac{D_j - D_{j-1}}{2} \begin{bmatrix} \sin I_{j-1} \cos A_{j-1} + \sin I_j \cos A_j \\ \sin I_{j-1} \sin A_{j-1} + \sin I_j \sin A_j \\ \cos I_{j-1} + \cos I_j \end{bmatrix} \quad (\text{A.3})$$

So for the interval between stations  $k-1$  and  $k$  we can write:

$$\frac{d\Delta r_k}{dp_k} = \left[ \frac{d\Delta r_k}{dD_k} \quad \frac{d\Delta r_k}{dI_k} \quad \frac{d\Delta r_k}{dA_k} \right]$$

Substituting  $j=k$  and differentiating equation (A.3) we get:

$$\frac{d\Delta r_k}{dD_k} = \frac{1}{2} \left[ \begin{array}{c} \sin I_{k-1} \cos A_{k-1} + \sin I_k \cos A_k \\ \sin I_{k-1} \sin A_{k-1} + \sin I_k \sin A_k \\ \cos I_{k-1} + \cos I_k \end{array} \right]$$

$$\frac{d\Delta r_k}{dI_k} = \frac{1}{2} \left[ \begin{array}{c} (D_k - D_{k-1}) \cos I_k \cos A_k \\ (D_k - D_{k-1}) \cos I_k \sin A_k \\ -(D_k - D_{k-1}) \sin I_k \end{array} \right]$$

$$\frac{d\Delta r_k}{dA_k} = \frac{1}{2} \left[ \begin{array}{c} -(D_k - D_{k-1}) \sin I_k \sin A_k \\ (D_k - D_{k-1}) \sin I_k \cos A_k \\ 0 \end{array} \right]$$

Putting it together:

$$\frac{d\Delta r_k}{dp_k} = \frac{1}{2} \left[ \begin{array}{ccc} \sin I_{k-1} \cos A_{k-1} + \sin I_k \cos A_k & (D_k - D_{k-1}) \cos I_k \cos A_k & -(D_k - D_{k-1}) \sin I_k \sin A_k \\ \sin I_{k-1} \sin A_{k-1} + \sin I_k \sin A_k & (D_k - D_{k-1}) \cos I_k \sin A_k & (D_k - D_{k-1}) \sin I_k \cos A_k \\ \cos I_{k-1} + \cos I_k & -(D_k - D_{k-1}) \sin I_k & 0 \end{array} \right]$$

Similarly, for the interval between stations  $k$  and  $k+1$  we can write:

$$\frac{d\Delta r_{k+1}}{dp_k} = \left[ \frac{d\Delta r_{k+1}}{dD_k} \quad \frac{d\Delta r_{k+1}}{dI_k} \quad \frac{d\Delta r_{k+1}}{dA_k} \right]$$

Substituting  $j=k+1$  and again differentiating equation (A.3) we get:

$$\frac{d\Delta r_{k+1}}{dD_k} = \frac{1}{2} \left[ \begin{array}{c} -\sin I_k \cos A_k - \sin I_{k+1} \cos A_{k+1} \\ -\sin I_k \sin A_k - \sin I_{k+1} \sin A_{k+1} \\ -\cos I_k - \cos I_{k+1} \end{array} \right]$$

$$\frac{d\Delta r_{k+1}}{dI_k} = \frac{1}{2} \left[ \begin{array}{c} (D_{k+1} - D_k) \cos I_{k+1} \cos A_{k+1} \\ (D_{k+1} - D_k) \cos I_{k+1} \sin A_{k+1} \\ -(D_{k+1} - D_k) \sin I_{k+1} \end{array} \right]$$

$$\frac{d\Delta r_{k+1}}{dA_k} = \frac{1}{2} \left[ \begin{array}{c} -(D_{k+1} - D_k) \sin I_{k+1} \sin A_{k+1} \\ (D_{k+1} - D_k) \sin I_{k+1} \cos A_{k+1} \\ 0 \end{array} \right]$$

And so:

$$\frac{d\Delta r_{k+1}}{dp_k} = \frac{1}{2} \begin{bmatrix} -\sin I_k \cos A_k - \sin I_{k+1} \cos A_{k+1} & (D_{k+1} - D_k) \cos I_{k+1} \cos A_{k+1} & -(D_{k+1} - D_k) \sin I_{k+1} \sin A_{k+1} \\ -\sin I_k \sin A_k - \sin I_{k+1} \sin A_{k+1} & (D_{k+1} - D_k) \cos I_{k+1} \sin A_{k+1} & (D_{k+1} - D_k) \sin I_{k+1} \cos A_{k+1} \\ -\cos I_k - \cos I_{k+1} & -(D_{k+1} - D_k) \sin I_{k+1} & 0 \end{bmatrix}$$

So in summary, we have now calculated the 3x3 matrix equations which describe the change in the wellbore position, in the nev-co-ordinate frame caused by changes to the survey measurement at any preceding given station,  $k$ .

For the last survey station of interest, only the preceding interval is applicable and equation (A.1) becomes:

$$e_{i,l,k}^* = \sigma_{i,l} \left( \frac{d\Delta r_k}{dp_k} \right) \frac{\partial p_k}{\partial \varepsilon_i}$$



## A2 - Details of the Error Summation Method

Following on from the discussion in section [19.2.6](#), we have the example equations for adding error arithmetically or by root-sum-squaring:

$$e_{total} = e_1 + e_2$$

$$e_{total} = \sqrt{e_1^2 + e_2^2}$$

If we square both sides then we get:

$$e_{total}^2 = (e_1 + e_2)^2$$

$$e_{total}^2 = e_1^2 + e_2^2$$

So far we've only considered summing two error values. Generalising the sums to include more than two error sources, and remembering that for the error model at a particular point, the  $e$  variables will actually be 3x1 vectors and the squaring these would actually be  $e_i \cdot e_i^T$  then these equations become:

$$E_{total} = \left( \sum e_i \right) \left( \sum e_i \right)^T$$

$$E_{total} = \sum e_i e_i^T$$

Where now  $E_{total}$  is a 3x3 covariance matrix, whose lead diagonal terms are the  $e_{total}^2$  values along the principle axes.

Returning to the error model, when we come to create the final error summations, we need consider three summations – over the error sources, the survey legs and the survey stations and use the propagation modes to determine at which steps arithmetic summation is appropriate and at which RSS summation is required.

The overall summation of random, systematic and global/well by well error sources is

$$[C]_K^{svy} = \sum_{i \in R} [C]_{i,K}^{rand} + \sum_{i \in S} [C]_{i,K}^{syst} + \sum_{i \in \{W,G\}} [C]_{i,K}^{well}$$

The individual terms for the various groups of error sources are given below.

In these equations:

- $e_{i,l,k}$  is the vector contribution of  $i$ th error source, in the  $i$ th survey leg at the  $k$ th survey station (3x1 vector)
- $e_{i,l,K}^*$  is the vector contribution of  $i$ th error source, in the  $i$ th survey leg at the last survey point of interest i.e. the  $K$ th survey station (3x1 vector)
- $i$  is the summation over error sources from 1... $I$
- $k$  is the summation of survey stations from 1... $K$ : the current survey station
- $l$  is the summation over survey legs from 1.. $L$ : the current survey leg

The contribution of the random errors is given by:

$$[C]_{i,K}^{rand} = \sum_{l=1}^{L-1} [C]_{i,l}^{rand} + \sum_{k=1}^{K-1} (e_{i,l,k}) \cdot (e_{i,l,k})^T + (e_{i,L,K}^*) \cdot (e_{i,L,K}^*)^T$$

and

$$[C]_{i,l}^{rand} = \sum_{k=1}^{K_l} (e_{i,l,k}) \cdot (e_{i,l,k})^T$$

The systematic errors are:

$$[C]_{i,K}^{syst} = \sum_{l=1}^{L-1} [C]_{i,l}^{syst} + \left( \sum_{k=1}^{K_l} e_{i,L,k} + e_{i,L,K}^* \right) \cdot \left( \sum_{k=1}^{K_l} e_{i,L,k} + e_{i,L,K}^* \right)^T$$

$$[C]_{i,l}^{syst} = \left( \sum_{k=1}^{K_l} e_{i,l,k} \right) \left( \sum_{k=1}^{K_l} e_{i,l,k} \right)^T$$

And finally the well by well and global errors:

$$[C]_{i,K}^{well} = E_{i,K} \cdot E_{i,K}^T$$

$$E_{i,K}^{well} = \sum_{l=1}^{L-1} \left( \sum_{k=1}^{K_l} e_{i,l,k} \right) + \sum_{k=1}^{K-1} e_{i,L,k} + e_{i,L,K}^*$$



**CONTENTS**

## Appendix B: List of MWD Model Error Sources and Weighting Functions

### B1 - MWD Model Weighting Functions at Revision 3

Revisions 1 and 3 made changes to the MWD model weighting functions (see section 19.3.6 for a discussion of the revisions to the MWD model). This is the current list at revision 3. Revision 4 is a change to how certain error magnitude values are calculated and does not affect the weighting functions so this list is correct for both revisions 3 and 4. The next section lists the weighting functions which have been replaced.

	Error Code	Description	Propagation Mode	Weighting Function		
				MD	Inc	Azimuth
1	ABXY-TI1	Accelerometer bias – term1	S/R	0	$\frac{\cos I}{G}$	$\frac{\tan\theta \cdot \cos I \cdot \sin A_m}{G}$
2	ABXY-TI2	Accelerometer bias – term2	S/R	0	0	$\frac{\cot I - \tan\theta \cdot \cos A_m}{G}$
3	ABZ	Accelerometer bias z-axis	S	0	$\frac{-\sin I}{G}$	$\frac{\tan\theta \cdot \sin I \cdot \sin A_m}{G}$
4	ASXY-TI1	Accelerometer scale factor – term1	S	0	$\frac{\sin I \cdot \cos I}{\sqrt{2}}$	$-\frac{\tan\theta \cdot \sin I \cdot \cos I \cdot \sin A_m}{\sqrt{2}}$
5	ASXY-TI2	Accelerometer scale factor – term2	S/R	0	$\frac{\sin I \cdot \cos I}{\sqrt{2}}$	$-\frac{\tan\theta \cdot \sin I \cdot \cos I \cdot \sin A_m}{2}$
6	ASXY-TI3	Accelerometer scale factor – term3	S/R	0	0	$\frac{\tan\theta \cdot \sin I \cdot \cos A_m - \cos I}{2}$
7	ASZ	Accelerometer scalefactor z-axis	S	0	$-\sin I \cdot \cos I$	$\tan\theta \cdot \sin I \cdot \cos I \cdot \sin A_m$
8	MBXY-TI1	Magnetometer bias – term1	S/R	0	0	$\frac{-\cos I \cdot \sin A_m}{B \cdot \cos\theta}$
9	MBXY-TI2	Magnetometer bias – term2	S/R	0	0	$\frac{B \cdot \cos\theta}{\cos A_m}$
10	MBZ	Magnetometer bias z-axis	S	0	0	$\frac{-\sin I \cdot \sin A_m}{B \cdot \cos\theta}$
11	MSXY-TI1	Magnetometer scale factor – term1	S	0	0	$\frac{\sin I \cdot \sin A_m \cdot (\tan\theta \cdot \cos I + \sin I \cdot \cos A_m)}{\sqrt{2}}$
12	MSXY-TI2	Accelerometer scale factor – term2	S/R	0	0	$\frac{\sin A_m \cdot (\tan\theta \cdot \sin I \cdot \cos I - \cos^2 I \cdot \cos A_m - \cos A_m)}{2}$
13	MSXY-TI3	Magnetometer scale factor – term3	S/R	0	0	$\frac{(\cos I \cdot \cos^2 A_m - \cos I \cdot \sin^2 A_m - \tan\theta \cdot \sin I \cdot \cos A_m)}{2}$
14	MSZ	Magnetometer scalefactor z-axis	S	0	0	$-(\sin I \cdot \cos A_m + \tan\theta \cdot \cos I) \cdot \sin I \cdot \sin A_m$
15	DEC	Constant declination error	G	0	0	1
16	DBH	Declination error dependant on the horizontal component of Earth's field	G	0	0	$\frac{1}{B \cdot \cos\theta}$
17	SAG	BHA Sag	S	0	$\sin I$	0
18	AMIC	Constant axial magnetic interference	S	0	0	1

19	AMID	Direction dependant axial magnetic interference	S	0	0	$\sin I . \sin A_m$
20	XYM1	xy misalignment 1	S/R	0	$w_{12}$	0
21	XYM2	xy misalignment 2	S/R	0	0	$-w_{12}/\sin I$
22	XYM3	xy misalignment 3	S	0	$w_{34}\cos A$	$-w_{34}\sin A/\sin I$
23	XYM4	xy misalignment 4	S	0	$w_{34}\sin A$	$w_{34}\cos A/\sin I$
24	ABIXY-TI1	Accelerometer bias – axial interference correction – term1	S/R	0	$\frac{\cos I}{G}$	$\frac{\cos^2 I . \sin A_m (\tan \theta . \cos I + \sin I . \cos A_m)}{G(1 - \sin^2 I . \sin^2 A_m)}$
25	ABIXY-TI2	Accelerometer bias – axial interference correction – term2	S/R	0	0	$\frac{-(\tan \theta . \cos A_m - \cot I)}{G(1 - \sin^2 I . \sin^2 A_m)}$
26	ABIZ	Accelerometer bias z-axis when axial interference correction applied.	S	0	$\frac{-\sin I}{G}$	$\frac{\sin I . \cos I . \sin A_m (\tan \theta . \cos I + \sin I . \cos A_m)}{G . (1 - \sin^2 I . \sin^2 A_m)}$
27	ASIXY-TI1	Accelerometer scale factor – axial interference correction – term1	S	0	$\frac{\sin I . \cos I}{\sqrt{2}}$	$-\frac{\sin I . \cos^2 I . \sin A_m . (\tan \theta . \cos I + \sin I . \cos A_m)}{\sqrt{2}(1 - \sin^2 I . \sin^2 A_m)}$
28	ASIXY-TI2	Accelerometer scale factor – axial interference correction – term2	S/R	0	$\frac{\sin I . \cos I}{\sqrt{2}}$	$-\frac{\sin I . \cos^2 I . \sin A_m . (\tan \theta . \cos I + \sin I . \cos A_m)}{2(1 - \sin^2 I . \sin^2 A_m)}$
29	ASIXY-TI3	Accelerometer scale factor – axial interference correction – term3	S/R	0	0	$-\frac{(\tan \theta . \sin I . \cos A_m - \cos I)}{2(1 - \sin^2 I . \sin^2 A_m)}$
30	ASIZ	Accelerometer scalefactor z-axis when axial interference correction applied.	S	0	$-\sin I . \cos I$	$\frac{\sin I . \cos^2 I . \sin A_m (\tan \theta . \cos I + \sin I . \cos A_m)}{G . (1 - \sin^2 I . \sin^2 A_m)}$
31	MBIXY-TI1	Magnetometer bias – axial interference correction – term1	S/R	0	0	$-\frac{\cos I . \sin A_m}{B . \cos \theta (1 - \sin^2 I . \sin^2 A_m)}$
32	MBIXY-TI2	Magnetometer bias – axial interference correction – term2	S/R	0	0	$\frac{\cos A_m}{B . \cos \theta (1 - \sin^2 I . \sin^2 A_m)}$
33	MSIXY-TI1	Magnetometer scale factor – axial interference correction – term1	S	0	0	$-\frac{\sin I . \sin A_m . (\tan \theta . \cos I + \sin I . \cos A_m)}{\sqrt{2}(1 - \sin^2 I . \sin^2 A_m)}$
34	MSIXY-TI2	Magnetometer scale factor – axial interference correction – term2	S/R	0	0	$-\frac{\sin A_m . (\tan \theta . \sin I . \cos I - \cos^2 I . \cos A_m - \cos A_m)}{2(1 - \sin^2 I . \sin^2 A_m)}$
35	MSIXY-TI3	Magnetometer scale factor – axial interference correction – term3	S/R	0	0	$\frac{(\cos I . \cos^2 A_m - \cos I . \sin^2 A_m - \tan \theta . \sin I . \cos A_m)}{2(1 - \sin^2 I . \sin^2 A_m)}$
36	MFI	Earth's total magnetic field when axial interference correction applied.	G	0	0	$-\frac{\sin I . \sin A_m (\tan \theta . \cos I + \sin I . \cos A_m)}{B . (1 - \sin^2 I . \sin^2 A_m)}$
37	MDI	Dip angle when axial interference correction applied.	G	0	0	$-\frac{\sin I . \sin A_m (\cos I - \tan \theta . \sin I . \cos A_m)}{(1 - \sin^2 I . \sin^2 A_m)}$
38	DREF-R	Depth reference random	R	1	0	0
39	DREF-S	Depth reference systematic	S	1	0	0

40	DSF-S	Depth Scale	S	$D$	0	0
41	DST-G	Depth Stretch	G	$D.D_V$	0	0

## B2 - Historic Terms: No Longer Used in the MWD Model After Revisions 1 and 3

See section [19.3.4](#) for a discussion of the revisions to the MWD model. The following weighting functions have been replaced by new methods introduced in revision 1 (misalignment terms MX and MY replaced) and revision 3 (toolface dependant terms – i.e. all the remaining terms below).

	Error Code	Description		Weighting Function		
				MD	Inc	Azimuth
1	MX	Tool axial misalignment – x-axis	S	0	$\sin\alpha$	$\frac{-\cos\alpha}{\sin I}$
2	MY	Tool axial misalignment – y-axis	S	0	$\cos\alpha$	$\frac{\sin\alpha}{\sin I}$
3	ABX	Accelerometer bias x-axis	S	0	$\frac{-\cos I \cdot \sin\alpha}{G}$	$\frac{(\cos I \cdot \sin A_m \cdot \sin\alpha - \cos A_m \cdot \cos\alpha) \cdot \tan\theta - \cot I \cdot \cos\alpha}{G}$
4	ABY	Accelerometer bias y-axis	S	0	$\frac{\cos I \cdot \cos\alpha}{G}$	$\frac{(\cos I \cdot \sin A_m \cdot \cos\alpha + \cos A_m \cdot \sin\alpha) \cdot \tan\theta - \cot I \cdot \sin\alpha}{G}$
5	ASX	Accelerometer scalefactor x-axis	S	0	$\sin I \cdot \cos I \cdot \sin^2\alpha$	$-\{ \tan\theta \cdot \sin I (\cos I \cdot \sin A_m \cdot \sin\alpha - \cos A_m \cdot \cos\alpha) + \cos I \cdot \cos\alpha \} \cdot \sin\alpha$
6	ASY	Accelerometer scalefactor y-axis	S	0	$\sin I \cdot \cos I \cdot \cos^2\alpha$	$-\{ \tan\theta \cdot \sin I (\cos I \cdot \sin A_m \cdot \cos\alpha + \cos A_m \cdot \sin\alpha) - \cos I \cdot \sin\alpha \} \cdot \cos\alpha$
7	MBX	Magnetometer bias x-axis	S	0	0	$\frac{\cos A_m \cdot \cos\alpha - \cos I \cdot \sin A_m \cdot \sin\alpha}{B \cdot \cos\theta}$
8	MBY	Magnetometer bias y-axis	S	0	0	$\frac{-\cos A_m \cdot \sin\alpha + \cos I \cdot \sin A_m \cdot \cos\alpha}{B \cdot \cos\theta}$
9	MSX	Magnetometer scalefactor x-axis	S	0	0	$(\cos I \cdot \cos A_m \cdot \sin\alpha - \tan\theta \cdot \sin I \cdot \sin\alpha + \sin A_m \cdot \cos\alpha) \cdot (\cos A_m \cdot \cos\alpha - \cos I \cdot \sin A_m \cdot \sin\alpha)$
10	MSY	Magnetometer scalefactor y-axis	S	0	0	$-(\cos I \cdot \cos A_m \cdot \cos\alpha - \tan\theta \cdot \sin I \cdot \cos\alpha - \sin A_m \cdot \sin\alpha) \cdot (\cos A_m \cdot \sin\alpha + \cos I \cdot \sin A_m \cdot \cos\alpha)$
11	ABIX	Accelerometer bias x-axis when axial interference correction applied.	S	0	$-\cos I \cdot \sin\alpha$	$\frac{\cos^2 I \cdot \sin A_m \cdot \sin\alpha (\tan\theta \cdot \cos I + \sin I \cdot \cos A_m) - \cos\alpha (\tan\theta \cdot \cos A_m - \cot I)}{G \cdot (1 - \sin^2 I \cdot \sin^2 A_m)}$
12	ABIY	Accelerometer bias y-axis when axial interference correction applied.	S	0	$-\cos I \cdot \cos\alpha$	$\frac{\cos^2 I \cdot \sin A_m \cdot \cos\alpha (\tan\theta \cdot \cos I + \sin I \cdot \cos A_m) + \sin\alpha (\tan\theta \cdot \cos A_m - \cot I)}{G \cdot (1 - \sin^2 I \cdot \sin^2 A_m)}$
13	ASIX	Accelerometer scalefactor x-axis when axial interference correction applied.	S	0	$\sin I \cdot \cos I \cdot \sin^2\alpha$	$\frac{-\sin\alpha [\sin I \cdot \cos^2 I \cdot \sin A_m \cdot \sin\alpha (\tan\theta \cdot \cos I + \sin I \cdot \cos A_m) - \cos\alpha (\tan\theta \cdot \sin I \cdot \cos A_m)]}{(1 - \sin^2 I \cdot \sin^2 A_m)}$
14	ASIY	Accelerometer scalefactor y-axis when axial interference correction applied.	S	0	$\sin I \cdot \cos I \cdot \cos^2\alpha$	$\frac{-\cos\alpha [\sin I \cdot \cos^2 I \cdot \sin A_m \cdot \cos\alpha (\tan\theta \cdot \cos I + \sin I \cdot \cos A_m) + \sin\alpha (\tan\theta \cdot \sin I \cdot \cos A_m)]}{(1 - \sin^2 I \cdot \sin^2 A_m)}$

15	MBIX	Magnetometer bias x-axis when axial interference correction applied.	S	0	0	$-\frac{\cos I \cdot \sin A_m \sin \alpha - \cos A_m \cos \alpha}{B \cos \theta \cdot (1 - \sin^2 I \cdot \sin^2 A_m)}$
16	MBIY	Magnetometer bias y-axis when axial interference correction applied.	S	0	0	$-\frac{\cos I \cdot \sin A_m \cos \alpha + \cos A_m \sin \alpha}{B \cos \theta \cdot (1 - \sin^2 I \cdot \sin^2 A_m)}$
17	MSIX	Magnetometer scalefactor x-axis when axial interference correction applied.	S	0	0	$-\frac{(\cos I \cdot \cos A_m \sin \alpha - \tan \theta \cdot \sin I \cdot \sin \alpha + \sin A_m \cos \alpha)(\cos I \cdot \sin A_m \sin \alpha - \cos A_m \cos \alpha)}{(1 - \sin^2 I \cdot \sin^2 A_m)}$
18	MSIY	Magnetometer scalefactor y-axis when axial interference correction applied.	S	0	0	$-\frac{(\cos I \cdot \cos A_m \cos \alpha - \tan \theta \cdot \sin I \cdot \cos \alpha + \sin A_m \sin \alpha)(\cos I \cdot \sin A_m \cos \alpha + \cos A_m \sin \alpha)}{(1 - \sin^2 I \cdot \sin^2 A_m)}$

### B3 - MWD Defined Error Magnitudes – Revision 3

The table below defines all MWD error magnitudes at revision 3. The revision 4 changes introduce look up tables for the reference magnitude field terms DEC-G and DBH-G. Some models may also include DEC-R and DBH-R to take into account random fluctuations in the reference field. These are not explicitly included in the standard model.

	Error Code	Description	MWD	MWD with Axial Interference Correction
1	ABXY-TI1	Accelerometer bias xy – term1	0.004ms <sup>-2</sup>	
2	ABXY-TI2	Accelerometer bias xy – term2	0.004ms <sup>-2</sup>	
3	ABZ	Accelerometer bias z-axis	0.004ms <sup>-2</sup>	
4	ASXY-TI1	Accelerometer scale factor xy – term1	0.0005	
5	ASXY-TI2	Accelerometer scale factor xy – term2	0.0005	
6	ASXY-TI3	Accelerometer scale factor xy – term3	0.0005	
7	ASZ	Accelerometer scalefactor z-axis	0.0005	
8	MBXY-TI1	Magnetometer bias xy – term1	70nT	
9	MBXY-TI2	Magnetometer bias xy – term2	70nT	
10	MBZ	Magnetometer bias z-axis	70nT	
11	MSXY-TI1	Magnetometer scale factor xy – term1	0.0016	
12	MSXY-TI2	Accelerometer scale factor xy – term2	0.0016	
13	MSXY-TI3	Magnetometer scale factor xy – term3	0.0016	
14	MSZ	Magnetometer scalefactor z-axis	0.0016	
15	DEC	Constant declination error	0.36°	0.36°
16	DBH	Declination error dependant on the horizontal component of Earth's field	5000nT	5000nT
17	SAG	BHA Sag	0.2°	0.2°
18	AZ	Constant axial magnetic interference	0.25°	
19	AMID	Direction dependant axial magnetic interference	0.6°	
20	XYM1	xy misalignment 1	0.06°	0.06°
21	XYM2	xy misalignment 2	0.06°	0.06°
22	XYM3	xy misalignment 3	0.06°	0.06°
23	XYM4	xy misalignment 4	0.06°	0.06°
24	ABIXY-TI1	Accelerometer bias xy – axial interference correction – term1		0.004ms <sup>-2</sup>
25	ABIXY-TI2	Accelerometer bias xy – axial interference correction – term2		0.004ms <sup>-2</sup>
26	ABIZ	Accelerometer bias z-axis when axial interference correction applied.		0.004ms <sup>-2</sup>
27	ASIXY-TI1	Accelerometer scale factor xy – axial interference correction – term1		0.0005



28	ASIXY-TI2	Accelerometer scale factor xy – axial interference correction – term2		0.0005
29	ASIXY-TI3	Accelerometer scale factor xy – axial interference correction – term3		0.0005
30	ASIZ	Accelerometer scalefactor z-axis when axial interference correction applied.		0.0005
31	MBIXY-TI1	Magnetometer bias xy – axial interference correction – term1		70nT
32	MBIXY-TI2	Magnetometer bias xy – axial interference correction – term2		70nT
33	MSIXY-TI1	Magnetometer scale factor xy – axial interference correction – term1		0.0016
34	MSIXY-TI2	Magnetometer scale factor xy – axial interference correction – term2		0.0016
35	MSIXY-TI3	Magnetometer scale factor xy – axial interference correction – term3		0.0016
36	MFI	Earth's total magnetic field when axial interference correction applied.		130nT
37	MDI	Dip angle when axial interference correction applied.		0.20°

	Error Code	Description	Drillpipe – Fixed Rig	Drillpipe – Floating Platform
38	DREF-R	Random Depth Reference	0.35m	2.20m
39	DREF-S	Systematic Depth Reference	0.00m	1.00m
40	DSF-S	Depth Scalefactor	$5.6 \times 10^{-4}$	$5.6 \times 10^{-4}$
41	DST-G	Depth Stretch	$2.5 \times 10^{-7} \text{m}^{-1}$	$2.5 \times 10^{-7} \text{m}^{-1}$

### B4 - MWD Defined Error Magnitudes – Revision 3

The table below defines all MWD error magnitudes at revision 3. The revision 4 changes introduce look up tables for the reference magnitude field terms DEC-G and DBH-G. Some models may also include DEC-R and DBH-R to take into account random fluctuations in the reference field. These are not explicitly included in the standard model.

	Error Code	Description	MWD	MWD with Axial Interference Correction
1	ABXY-TI1	Accelerometer bias xy – term1	0.004ms <sup>-2</sup>	
2	ABXY-TI2	Accelerometer bias xy – term2	0.004ms <sup>-2</sup>	
3	ABZ	Accelerometer bias z-axis	0.004ms <sup>-2</sup>	
4	ASXY-TI1	Accelerometer scale factor xy – term1	0.0005	
5	ASXY-TI2	Accelerometer scale factor xy – term2	0.0005	
6	ASXY-TI3	Accelerometer scale factor xy – term3	0.0005	
7	ASZ	Accelerometer scalefactor z-axis	0.0005	
8	MBXY-TI1	Magnetometer bias xy – term1	70nT	
9	MBXY-TI2	Magnetometer bias xy – term2	70nT	
10	MBZ	Magnetometer bias z-axis	70nT	
11	MSXY-TI1	Magnetometer scale factor xy – term1	0.0016	
12	MSXY-TI2	Magnetometer scale factor xy – term2	0.0016	
13	MSXY-TI3	Magnetometer scale factor xy – term3	0.0016	
14	MSZ	Magnetometer scalefactor z-axis	0.0016	
15	DEC	Constant declination error	0.36°	0.36°
16	DBH	Declination error dependant on the horizontal component of Earth's field	5000nT	5000nT
17	SAG	BHA Sag	0.2°	0.2°
18	AZ	Constant axial magnetic interference	0.25°	
19	AMID	Direction dependant axial magnetic interference	0.6°	
20	XYM1	xy misalignment 1	0.06°	0.06°
21	XYM2	xy misalignment 2	0.06°	0.06°
22	XYM3	xy misalignment 3	0.06°	0.06°
23	XYM4	xy misalignment 4	0.06°	0.06°
24	ABIXY-TI1	Accelerometer bias xy – axial interference correction – term1		0.004ms <sup>-2</sup>
25	ABIXY-TI2	Accelerometer bias xy – axial interference correction – term2		0.004ms <sup>-2</sup>
26	ABIZ	Accelerometer bias z-axis when axial interference correction applied.		0.004ms <sup>-2</sup>
27	ASIXY-TI1	Accelerometer scale factor xy – axial interference correction – term1		0.0005
28	ASIXY-TI2	Accelerometer scale factor xy – axial interference correction – term2		0.0005
29	ASIXY-TI3	Accelerometer scale factor xy – axial interference correction – term3		0.0005
30	ASIZ	Accelerometer scalefactor z-axis when axial interference correction applied.		0.0005
31	MBIXY-TI1	Magnetometer bias xy – axial interference correction – term1		70nT
32	MBIXY-TI2	Magnetometer bias xy – axial interference correction – term2		70nT

33	MSIXY-TI1	Magnetometer scale factor xy – axial interference correction – term1		0.0016
34	MSIXY-TI2	Magnetometer scale factor xy – axial interference correction – term2		0.0016
35	MSIXY-TI3	Magnetometer scale factor xy – axial interference correction – term3		0.0016
36	MFI	Earth's total magnetic field when axial interference correction applied.		130nT
37	MDI	Dip angle when axial interference correction applied.		0.20°

	Error Code	Description	Drillpipe – Fixed Rig	Drillpipe – Floating Platform
38	DREF-R	Random Depth Reference	0.35m	2.20m
39	DREF-S	Systematic Depth Reference	0.00m	1.00m
40	DSF-S	Depth Scalefactor	$5.6 \times 10^{-4}$	$5.6 \times 10^{-4}$
41	DST-G	Depth Stretch	$2.5 \times 10^{-7} \text{m}^{-1}$	$2.5 \times 10^{-7} \text{m}^{-1}$



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## Appendix C: List of Gyro Model Error Sources and Weighting Functions

In addition to the above MWD weighting functions the gyro error model introduces a whole new set of error sources and associated weighting functions.

The weighting functions can be grouped into those which apply in Stationary survey mode, Continuous survey mode or either mode. During a single survey leg a tool made transition between these modes as a function of inclination.

	Error Code	Description	SurveyMode	Propagation Mode	Weighting Function		
					MD	Inc	Azimuth
1	XYZ-XYB	3-axis: xy accelerometer bias	C/S	S/R	0	$\frac{\cos I}{G}$	0
2	XYZ-ZB	3-axis: z accelerometer bias	C/S	S	0	$\frac{\sin I}{G}$	0
3	XYZ-SF	3-axis: accelerometer scale factor error	C/S	S	0	$1.3 \sin I \cos I$	0
4	XYZ-MS	3-axis: accelerometer misalignment	C/S	S	0	1	0
5	AXY-B	2-axis: xy accelerometer bias	C/S	S/R	0	$\frac{1}{G \cos(1 - k \cdot \gamma)}$	0
6	AXY-SF	2-axis: Accelerometer scale factor error	C/S	S	0	$\tan(I - k \cdot \gamma)$	0
7	AXY-MS	2-axis: Accelerometer misalignment	C/S	S	0	1	0
8	AXY-GB	2-axis: Gravity Bias	C/S	S	0	$\frac{\tan(I - k \cdot \gamma)}{G}$	0
9	GXYZ-XYB1	3-axis, stationary: xy gyro bias 1	S	S/R	0	0	$\frac{\sin A \cos I}{\Omega \cos \phi}$
10	GXYZ-XYB2	3-axis, stationary: xy gyro bias 2	S	S/R	0	0	$\frac{\cos A}{\Omega \cos \phi}$
11	GXYZ-XYRN	3-axis, stationary: xy gyro random noise	S	R	0	0	$f \cdot \frac{\sqrt{1 - \sin^2 A \cdot \sin^2 I}}{\Omega \cos \phi}$
12	GXYZ-XYG1	3-axis, stationary: xy gyro g-dependent error 1	S	S	0	0	$\frac{\cos A \sin I}{\Omega \cos \phi}$
13	GXYZ-XYG2	3-axis, stationary: xy gyro g-dependent error 2	S	S/R	0	0	$\frac{\cos A \cos I}{\Omega \cos \phi}$
14	GXYZ-XYG3	3-axis, stationary: xy gyro g-dependent error 3	S	S/R	0	0	$\frac{\sin A \cos^2 I}{\Omega \cos \phi}$
15	GXYZ-XYG4	3-axis, stationary: xy gyro g-dependent error 4	S	S	0	0	$\frac{\sin A \sin I \cos I}{\Omega \cos \phi}$
16	GXYZ-ZB	3-axis, stationary: z gyro bias	S	S	0	0	$\frac{\sin A \sin I}{\Omega \cos \phi}$

17	GXYZ-ZRN	3-axis, stationary: z gyro random noise	S	R	0	0	$\frac{\sin A \sin I}{\Omega \cos \phi}$
18	GXYZ-ZG1	3-axis, stationary: z gyro g-dependent error 1	S	S/R	0	0	$\frac{\sin A \sin^2 I}{\Omega \cos \phi}$
19	GXYZ-ZG2	3-axis, stationary: z gyro g-dependent error 2	S	S	0	0	$\frac{\sin A \sin I \cos I}{\Omega \cos \phi}$
20	GXYZ-SF	3-axis, stationary: Gyro scalefactor	S	S	0	0	$\tan \phi \sin A \sin I \cos I$
21	GXYZ-MIS	3-axis, stationary: Gyro misalignment	S	S	0	0	$\frac{1}{\cos \phi}$
22	GXY-B1	2-axis, stationary: xy gyro bias 1	S	S/R	0	0	$\frac{\sin A}{\Omega \cos \phi \cos I}$
23	GXY-B2	2-axis, stationary: xy gyro bias 2	S	S/R	0	0	$\frac{\cos A}{\Omega \cos \phi}$
24	GXY-RN	2-axis, stationary: xy gyro random noise	S	R	0	0	$f \cdot \frac{\sqrt{1 - \cos^2 A} \cdot \sin^2 I}{\Omega \cos \phi \cos I}$
25	GXY-G1	2-axis, stationary: xy gyro g-dependent error 1	S	S	0	0	$\frac{\cos A \sin I}{\Omega \cos \phi}$
26	GXY-G2	2-axis, stationary: xy gyro g-dependent error 2	S	S/R	0	0	$\frac{\cos A \cos I}{\Omega \cos \phi}$
27	GXY-G3	2-axis, stationary: xy gyro g-dependent error 3	S	S/R	0	0	$\frac{\sin A}{\Omega \cos \phi}$
28	GXY-G4	2-axis, stationary: xy gyro g-dependent error 4	S	S	0	0	$\frac{\sin A \tan I}{\Omega \cos \phi}$
29	GXY-SF	2-axis, stationary: Gyro scalefactor	S	S	0	0	$\tan \phi \sin A \tan I$
30	GXY-MIS	2-axis, stationary: Gyro misalignment	S	S	0	0	$\frac{1}{\cos \phi \cos I}$
31	EXTREF	External reference error	S	S	0	0	1
32	EXTTIE	Un-modelled random azimuth error in tie-on tool	S	S	0	0	1
33	EXTMIS	Misalignment effect at tie-on	S	S	0	0	$\frac{1}{\sin I}$
34	GXYZ-GD	3-axis, continuous: xyz gyro drift	C	S	0	0	$h_i = h_{i-1} + \frac{\Delta D_i}{c}$
35	GXYZ-RW	3-axis, continuous: xyz gyro random walk	C	S	0	0	$h_i = \sqrt{h_{i-1}^2 + \frac{\Delta D_i}{c}}$
36	GXY-GD	2-axis, continuous: xy gyro drift	C	S	0	0	$h_i = h_{i-1} + \frac{1}{\sin \left( \frac{I_{i-1} + I_i}{2} \right)} \frac{\Delta D_i}{c}$

37	GXY-RW	2-axis, continuous: xy gyro random walk	C	S	0	0	$h_i = \sqrt{h_{i-1}^2 + \frac{1}{\sin\left(\frac{I_{i-1} + I_i}{2}\right)} \cdot \frac{\Delta D_i}{c}}$
38	GZ-GD	z-axis, continuous: z gyro drift	C	S	0	0	$h_i = h_{i-1} + \frac{1}{\sin\left(\frac{I_{i-1} + I_i}{2}\right)} \cdot \frac{\Delta D_i}{c}$
39	GZ-RW	z-axis, continuous: z gyro random walk	C	S	0	0	$h_i = \sqrt{h_{i-1}^2 + \frac{1}{\sin\left(\frac{I_{i-1} + I_i}{2}\right)} \cdot \frac{\Delta D_i}{c}}$

The following terms are common to both the gyro and MWD models.

	Error Code	Description	Survey Mode	Propagation Mode	Weighting Function		
					MD	Inc	Azimuth
40	XYM1	xy misalignment 1	C/S	S	0	$w_{12}$	0
41	XYM2	xy misalignment 2	C/S	S	0	0	$-w_{12}/\sin l$
42	XYM3	xy misalignment 3	C/S	S	0	$w_{34}\cos A$	$-w_{34}\sin A/\sin l$
43	XYM4	xy misalignment 4	C/S	S	0	$w_{34}\sin A$	$w_{34}\cos A/\sin l$
44	VSAG	Vertical sag (SAG in MWD model)	C/S	S	0	$\sin l$	0
45	DRF-R	Depth random error	C/S	R	1	0	0
46	DRF-S	Depth systematic reference	C/S	S	-	0	0
47	DSF-W	Depth scale	C/S	S/W	$\Delta D$	0	0
48	DST-G	Depth stretch type	C/S	G	$(D_v + D\cos l)$ $\Delta D$	0	0

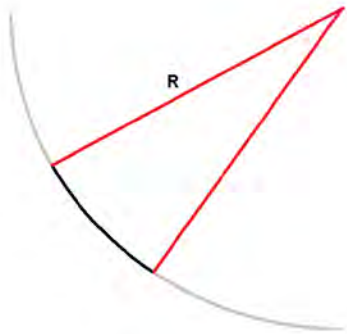


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## Appendix D: Some Useful Mathematics

### D1 - Equivalent Radius Formula

A dogleg severity can be converted to an equivalent radius using the following. If using degs / 100ft use the top formula and if using degs/30m use the bottom formula.

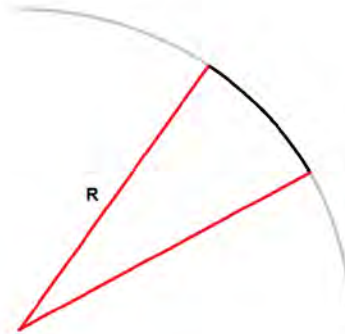


For any DLS

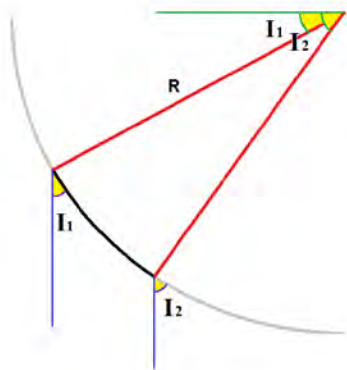
$$R = \frac{180 \times 100}{\pi \times \text{DLS}} \text{ ft}$$

or

$$R = \frac{180 \times 30}{\pi \times \text{DLS}} \text{ m}$$



### D2 - TVD and Step Out change When Building Angle



When Building Angle

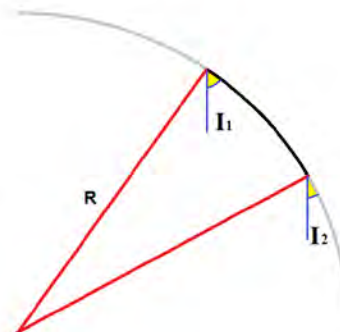
$$dTVD = R (\sin(I_2) - \sin(I_1))$$

$$dH = R (\cos(I_1) - \cos(I_2))$$

When Dropping Angle

$$dTVD = R (\sin(I_1) - \sin(I_2))$$

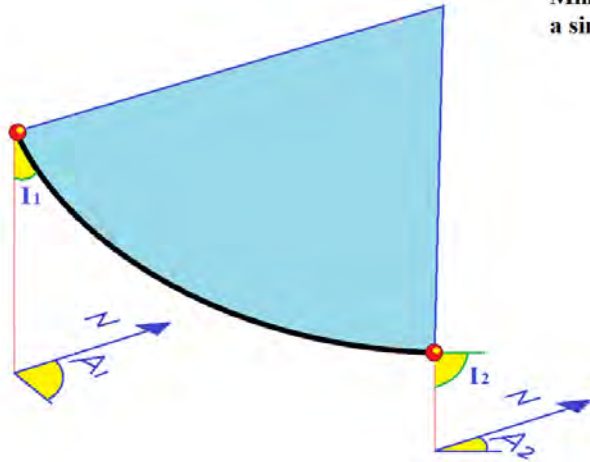
$$dH = R (\cos(I_2) - \cos(I_1))$$



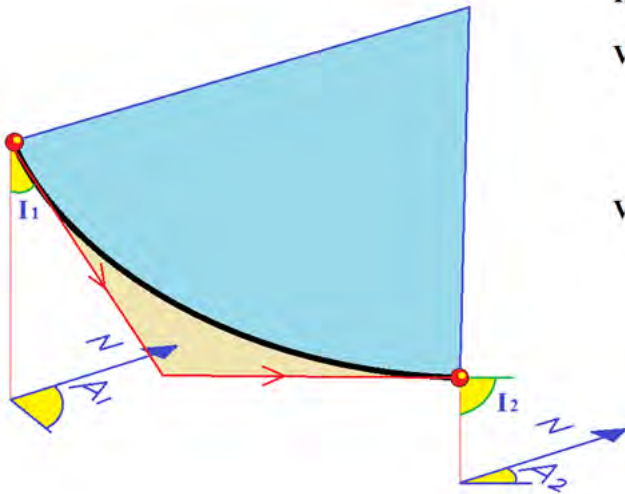


### D3 - Minimum Curvature

Minimum Curvature joins survey points with a single arc in 3D space.

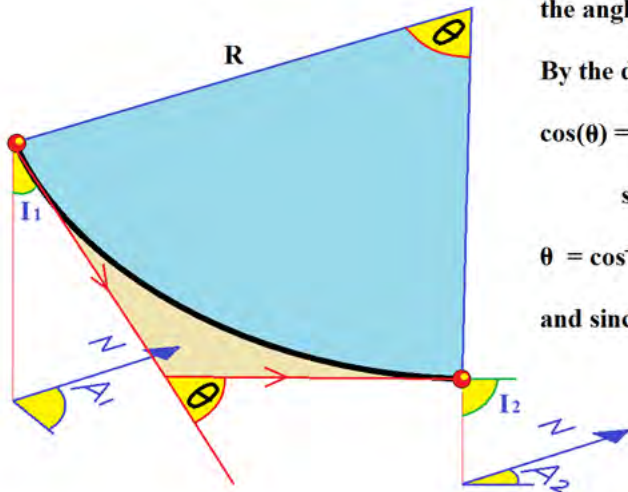


Imagine two vectors tangential to the well



Vector 1	dN	$\sin(I_1) \cos(A_1)$
	dE	$\sin(I_1) \sin(A_1)$
	dV	$\cos(I_1)$

Vector 2	dN	$\sin(I_2) \cos(A_2)$
	dE	$\sin(I_2) \sin(A_2)$
	dV	$\cos(I_2)$



The angle between these vectors is the same as the angle subtended by the arc of length delta M

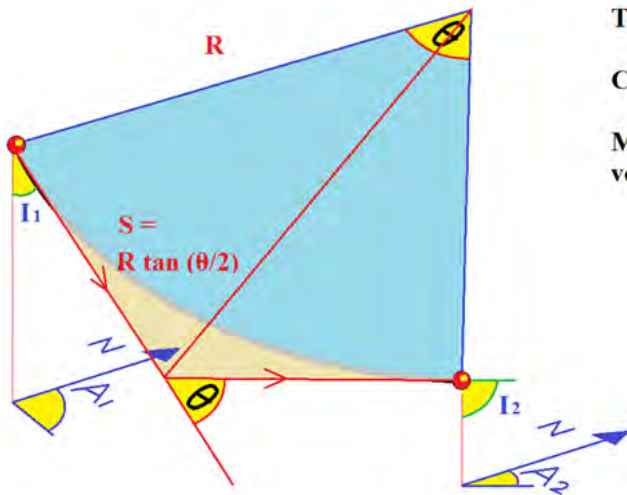
By the dot product rule the cos of this angle is

$$\cos(\theta) = (dN_1 \times dN_2 + dE_1 \times dE_2 + dV_1 \times dV_2)$$

so .....

$$\theta = \cos^{-1}(dN_1 \times dN_2 + dE_1 \times dE_2 + dV_1 \times dV_2)$$

$$\text{and since } R\theta = \text{delta M} \quad R = \text{delta M} / \theta$$



To go from point 1 to point 2

Calculate the length  $S = R \tan(\theta/2)$

Move S along vector 1 then S again along vector 2 and you will arrive at point 2

In the special case where  $I_1$  and  $I_2$  are the same and  $A_1$  and  $A_2$  are also the same, you only need to calculate S as  $0.5 \times dM$  where  $dM$  is the measured depth change from point 1 to point 2.

## Step by Step

1.  $dN1 = \sin(I1)\cos(A1)$
2.  $dE1 = \sin(I1)\sin(A1)$
3.  $dV1 = \cos(I1)$
4.  $dN2 = \sin(I2)\cos(A2)$
5.  $dE2 = \sin(I2)\sin(A2)$
6.  $dV2 = \cos(I2)$
7.  $\text{Theta} = \text{Acos}(dN1dN2+dE1dE2+dV1dV2)$
8.  $dM = (Md2 - Md1)$
9.  $R = dM/\text{Theta}$
10. If  $\text{Theta} = 0$  then  $S = .5*dM$
11. If  $\text{Theta} > 0$  then  $S = R\tan(\text{Theta}/2)$
12.  $d\text{North} = s(dN1+dN2)$
13.  $d\text{East} = s(dE1+dE2)$
14.  $d\text{TVD} = s(dV1+dV2)$

**D4 - MWD QC Checks**

These formulas can be used to calculate Btotal, Gtotal and Dip from a long survey

$$Bt = \sqrt{Bx^2 + By^2 + Bz^2}$$

$$Gt = \sqrt{Gx^2 + Gy^2 + Gz^2}$$

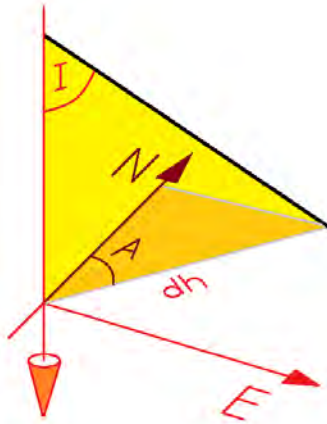
$$\text{Dip} = \sin^{-1} \left[ \frac{GxBx + GyBy + GzBz}{Gt Bt} \right]$$

1. Inclination and Azimuth calculation from raw data

$$I = \cos^{-1} \left( \frac{G_z}{\sqrt{G_x^2 + G_y^2 + G_z^2}} \right),$$

$$A_m = \tan^{-1} \left( \frac{(G_x B_y - G_y B_x) \sqrt{G_x^2 + G_y^2 + G_z^2}}{B_z (G_x^2 + G_y^2) - G_z (G_x B_x + G_y B_y)} \right)$$

## D5 - Useful MWD Vectors



In this diagram the length of the slope is 1 unit. The unit vector describing the along hole axis can be determined from the shifts to North, East and Vertical caused by 1 unit at inclination  $I$ , azimuth  $A$ .

Let's call the vertical shift  $dV$ .

The vertical shift  $dV = \cos(I)$

$dh$  is the horizontal shift where  $dh = \sin(I)$

The shift to the North  $dN$  will therefore be  $dh \cos(A)$  or, in full,

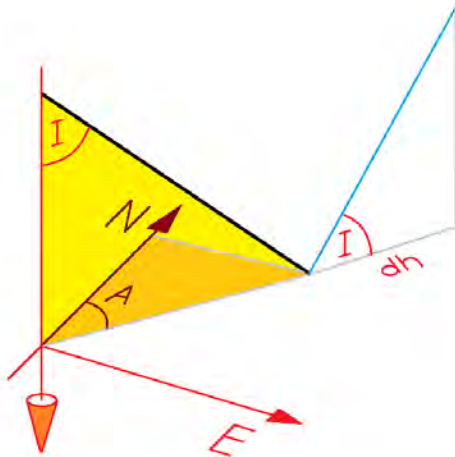
$$dN = \sin(I)\cos(A)$$

the shift to the East  $dE$  will therefore be  $dh \sin(A)$  or, in full,

$$dE = \sin(I)\sin(A)$$

So an along hole axis set at inclination  $I$ , Azimuth  $A$ , has a unit vector:

$$\begin{aligned} dE &= \sin(I)\sin(A) \\ dN &= \sin(I)\cos(A) \\ dV &= \cos(I) \end{aligned}$$

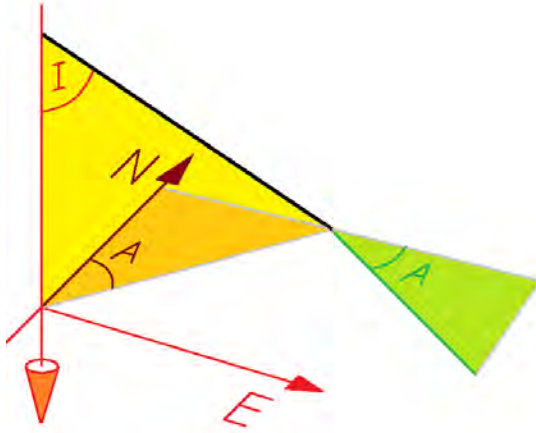


A unit vector to high side can be similarly defined. In this case the horizontal shift  $dH$  is 1 unit  $\times \cos(I)$  and the Vertical shift is 1 unit  $\times \sin(I)$  but is back towards the surface so the high side unit vector in full is:

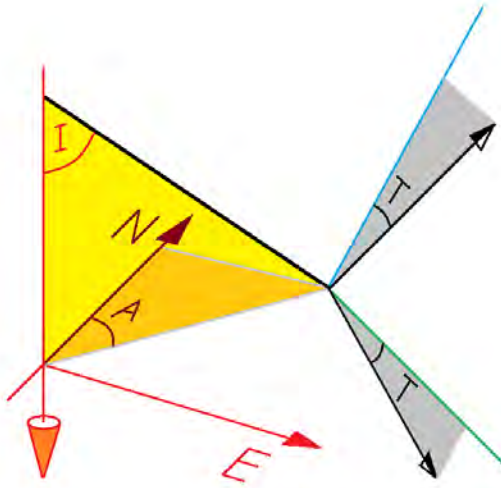
$$\begin{aligned} dE &= \cos(I)\sin(A) \\ dN &= \cos(I)\cos(A) \\ dV &= -\sin(I) \end{aligned}$$

For a lateral unit vector there is no vertical component so we can say:

$$\begin{aligned}dE &= \cos(A) \\dN &= -\sin(A) \\dV &= 0\end{aligned}$$





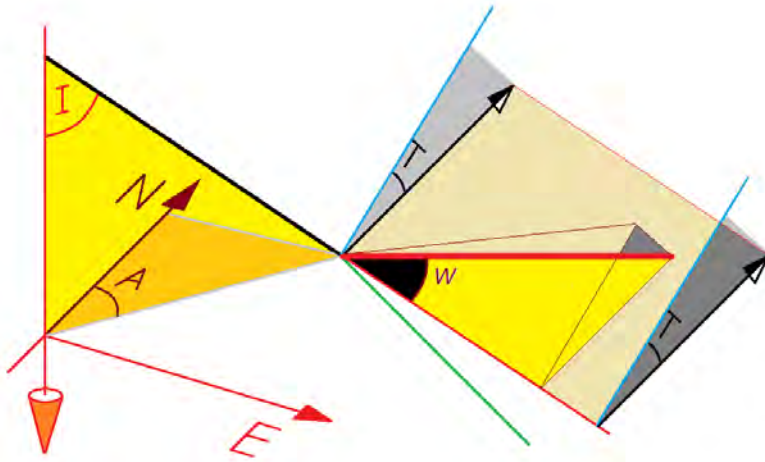


Our X and Y axes will be orientated with the toolface angle T. The X axis is normally pointing along the toolface angle with the Y axis clockwise 90 degrees. So the actual unit vector for the X axis consists of :

$$\text{Highside Vector} \times \cos(T) + \text{Lateral Vector} \times \sin(T)$$

and similarly the actual unit vector for the Y axis consists of:

$$\text{Lateral Vector} \times \cos(T) - \text{High Side vector} \times \sin(T)$$



In General for any sensor axis aligned at an angle  $W$  from the along hole axis and rotated  $T$  from the toolface we can determine the attitude vectors from the following construction:

The along hole component will be  $\cos(W)$   
 The offset component will be  $\sin(W)$

This will have a high side component  $\sin(W) \cos(T)$   
 and a lateral component  $\sin(W) \sin(T)$

This is a useful result for axes aligned at any angle and so the unit vector for any  $W$  and  $T$  value set at Inc  $I$ , Azimuth  $A$  and Toolface  $T_f$  can be written as:

$$\begin{aligned} dE &= \cos(W) A_e + \sin(W)\cos(T+T_f) H_e + \sin(W)\sin(T+T_f) L_e \\ dN &= \cos(W) A_n + \sin(W)\cos(T+T_f) H_n + \sin(W)\sin(T+T_f) L_n \\ dV &= \cos(W) A_v + \sin(W)\cos(T+T_f) H_v + \sin(W)\sin(T+T_f) L_v \end{aligned}$$

where  $A_e, A_n, A_v$  describes the Along Hole Vector  
 $H_e, H_n, H_v$  describes the High Side Vector  
 $L_e, L_n, L_v$  describes the Lateral Vector

The Equations in full can be expanded as follows:

$$\begin{aligned}dE &= \cos(W) Ae + \sin(W)\cos(T+Tf) He + \sin(W)\sin(T+Tf) Le \\dN &= \cos(W) An + \sin(W)\cos(T+Tf) Hn + \sin(W)\sin(T+Tf) Ln \\dV &= \cos(W) Av + \sin(W)\cos(T+Tf) Hv + \sin(W)\sin(T+Tf) Lv\end{aligned}$$

$$dE = \cos(W) \sin(I) \sin(A) + \sin(W) \cos(T+Tf) \cos(I) \sin(A) + \sin(W) \sin(T+Tf) \cos(A)$$

$$dN = \cos(W) \sin(I) \cos(A) + \sin(W) \cos(T+Tf) \cos(I) \cos(A) - \sin(W) \sin(T+Tf) \sin(A)$$

$$dV = \cos(W) \cos(I) - \sin(W) \cos(T+Tf) \sin(I)$$

This can be used to determine the theoretical G and B values to be read on any sensor by taking the dot products with the earths gravitational vector and the earths magnetic vector respectively.

$G_e = 0$   $G_n = 0$   $G_v = 1g$  (or expected local gravity field) so an accelerometer aligned W from along hole, T from high side will read

$$G_{\text{sensor}} = G_e dE + G_n dN + G_v dV$$

If we assume our reference is magnetic North for now then

$M_e = 0$   $M_n = B_t \cos(\text{Dip})$   $M_v = B_t \sin(\text{Dip})$  so a magnetometer aligned W from along hole, T from high side will read

$$M_{\text{sensor}} = M_e dE + M_n dN + M_v dV \quad \text{but since } M_e = 0 \text{ this is just } M_n dN + M_v dV$$

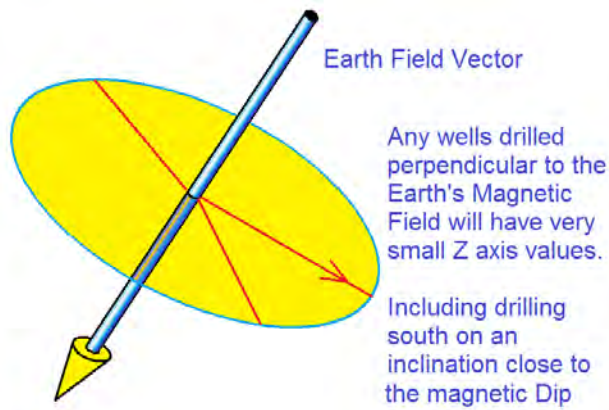
## D6 - Short Collar Correction

This is the most common formula for calculating a synthetic Bz value for substitution into the azimuth formula.

$$B_t = \sqrt{B_x^2 + B_y^2 + B_z^2} \quad \text{SO ....}$$

$$B_z = \sqrt{B_t^2 - B_x^2 - B_y^2}$$

This can be unstable in areas where the z axis value is small. This is any time when the well attitude is close to a right angle with the Earth's Magnetic Field.



An alternative sometimes used is to derive the synthetic  $B_z$  from the Dip Angle but Dip is not often known to a high degree of accuracy and this formula will also fail when  $G_z$  goes to zero (i.e. horizontal)

$$\text{Dip} = \sin^{-1} \left[ \frac{G_x B_x + G_y B_y + G_z B_z}{G_t B_t} \right] \text{ SO } \dots$$

$$B_z = \frac{G_t B_t \sin(\text{Dip}) - G_x B_x - G_y B_y}{G_z}$$

### D7 - Multi Station Analysis

In theory, we only need one magnetometer to determine the azimuth albeit with an east or west ambiguity. So we may not know what side of East or West we are but we can come up with an azimuth 0 to 180. However, we have 3 magnetometers and so, not only is the ambiguity resolved but we have redundancy on the measurement. You can imagine that we have a slight disagreement between the 3 sensors and also a disagreement with the dip and field strength of the background field. These disagreements are due to magnetic interference on each axis. If we found the right scale and bias corrections to clean out the interference, the three sensors would all agree with each other and agree with the  $B_t$  and Dip of the known background field.

Now let's take a look at the vectors derived above that describe the sensor axes for a given inclination, azimuth and toolface.

The Equations in full can be expanded as follows:

$$\begin{aligned}dE &= \cos(W) A_e + \sin(W)\cos(T+Tf) H_e + \sin(W)\sin(T+Tf) L_e \\dN &= \cos(W) A_n + \sin(W)\cos(T+Tf) H_n + \sin(W)\sin(T+Tf) L_n \\dV &= \cos(W) A_v + \sin(W)\cos(T+Tf) H_v + \sin(W)\sin(T+Tf) L_v\end{aligned}$$

$$dE = \cos(W) \sin(I) \sin(A) + \sin(W) \cos(T+Tf) \cos(I) \sin(A) + \sin(W) \sin(T+Tf) \cos(A)$$

$$dN = \cos(W) \sin(I) \cos(A) + \sin(W) \cos(T+Tf) \cos(I) \cos(A) - \sin(W) \sin(T+Tf) \sin(A)$$

$$dV = \cos(W) \cos(I) - \sin(W) \cos(T+Tf) \sin(I)$$

This can be used to determine the theoretical G and B values to be read on any sensor by taking the dot products with the earths gravitational vector and the earths magnetic vector respectively.

$G_e = 0$   $G_n = 0$   $G_v = 1g$  (or expected local gravity field) so an accelerometer aligned W from along hole, T from high side will read

$$G_{\text{sensor}} = G_e dE + G_n dN + G_v dV$$

If we assume our reference is magnetic North for now then

$M_e = 0$   $M_n = B_t \cos(\text{Dip})$   $M_v = B_t \sin(\text{Dip})$  so a magnetometer aligned W from along hole, T from high side will read

$$M_{\text{sensor}} = M_e dE + M_n dN + M_v dV \quad \text{but since } M_e = 0 \text{ this is just } M_n dN + M_v dV$$

We typically have 3 axes as follows:

X axis  $T = 0$  :  $W = 90$

Y axis  $T = 90$  :  $W = 90$

Z axis  $T = 0$  :  $W = 0$

If we then set up the following step by step procedure, we can derive corrections to  $B_x$ ,  $B_y$  and  $B_z$  to minimise the disagreements all the way down the BHA run.

## D8 - Multi Station Procedure

1. Use the  $G_x$ ,  $G_y$ ,  $G_z$ ,  $B_x$ ,  $B_y$ ,  $B_z$  to calculate the best fit inclination, azimuth and instrument toolface using the standard formulae.
2. Identify and remove any observations that produce highly inconsistent  $B_t$ ,  $G_t$  or Dip values from those around it. (Note inconsistent with the rest of the data NOT with the background field values. We are expecting to fail basic QC against the background field when we know there is magnetic interference to be found)
3. For each axis calculate the unit vectors describing their attitude in N,E and Vertical
4. For each magnetometer calculate what you would expect a clean reading to be by taking the dot product with the earth's magnetic field vector.
5. Define an 'error' as the difference between the clean value and the observed value.
6. For all surveys so far add up the sum of the squares of the errors.
7. See if the Errors are improved with a +/- 5 nT bias on  $B_z$  and if so apply it until there is no further improvement.
8. Repeat for  $B_y$  and  $B_x$
9. See if the errors are improved by swapping bias errors with some scale error on  $B_z$
10. Repeat for  $B_x$  and  $B_y$
11. Once the minimum error cannot be improved, you have found the best corrections. It is unusual for good quality data to drop into a 'local minimum' that is not the correct result but a good test is to start with large values and see if the final set is the same.

# VERSION & SUBMISSION INFORMATION

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Anyone who has expertise, techniques or updates they wish to submit to the author for assessment for inclusion in the next revision should email the data in the first instance to:

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