

Quantifying Uncertainties in High-resolution Magnetic Field Models

Ciaran Beggan, Susan Macmillan, Brian
Hamilton, William Brown

Speaker Bio



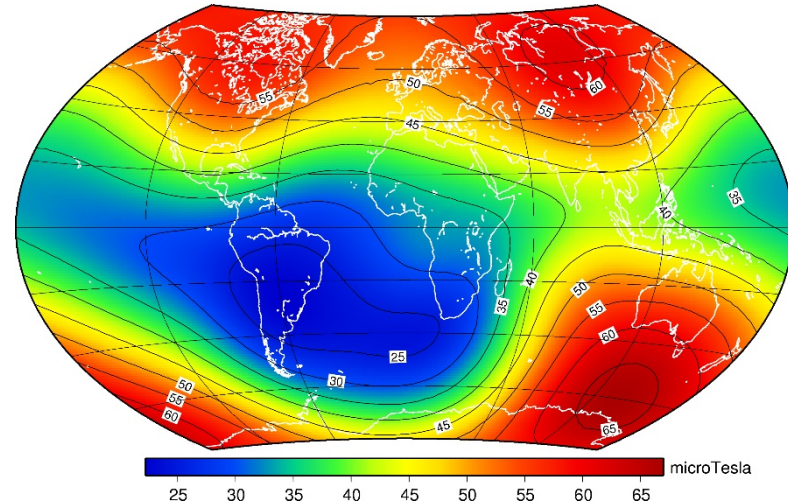
**British
Geological Survey**
Expert | Impartial | Innovative

- Introduction
 - British Geological Survey
 - 10+ years in geomagnetism
 - PhD, Univ. Edinburgh (2009)
 - Based in Edinburgh, UK
 - Specialize in main field modelling and forecasting, space weather, crustal field modelling

Magnetic field models

Industry requests higher degree, smaller scale magnetic models:

- Are these justified by the data available?
- What are the associated reduction (or otherwise) in uncertainties?
- What are the main sources of uncertainty and how to quantify them?
- We examine and quantify the main sources of error: (i) high degree *crustal field* and (ii) *spatial limitations* of crustal field input data (iii) *forecasting* uncertainty; (iv) *external field*,

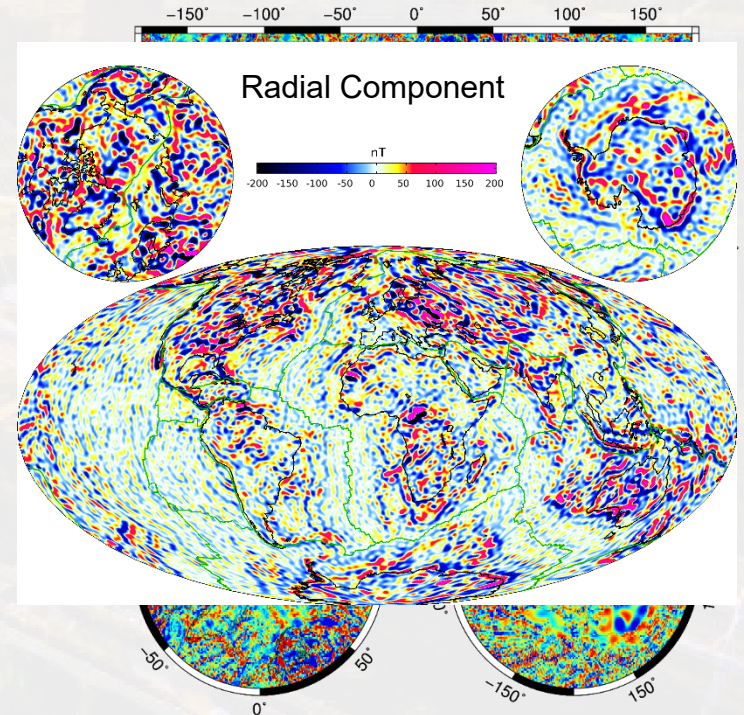


Total field (F): 2019.0

High degree models (degree > 133)

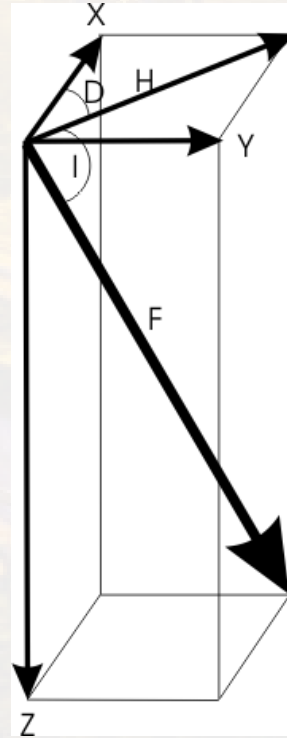
- Satellite data can be used to *consistently* model the field to degree 133 [wavelengths ~300 km]
- Adding in ground aeromagnetic and marine surveys; Global grid compilations at 0.05°
- Theoretical degree = 7200 [~4km]
- Realistically, available memory/computation time are limiting factors e.g. 800--1440 [~28-50 km]
- Look at errors in X, Y and Z (linear) and convert to Dec, Inc and Total Field (F) at the end
- Use **95.4% CI divided by 2 = 1 sigma** equivalent

Degree 1440 model: Z crustal comp



Analysis in XYZ

- Working with magnetic field values in X, Y and Z is **linear**
- Computing errors and differences in DIF is **non-linear** (e.g. angles with cosine/sine, square roots)
- Errors computed in XYZ and converted to DIF (using main field, H and F values) at the end



$$\delta D = \frac{\sqrt{(\delta X)^2 \sin^2 D + (\delta Y)^2 \cos^2 D}}{H}$$

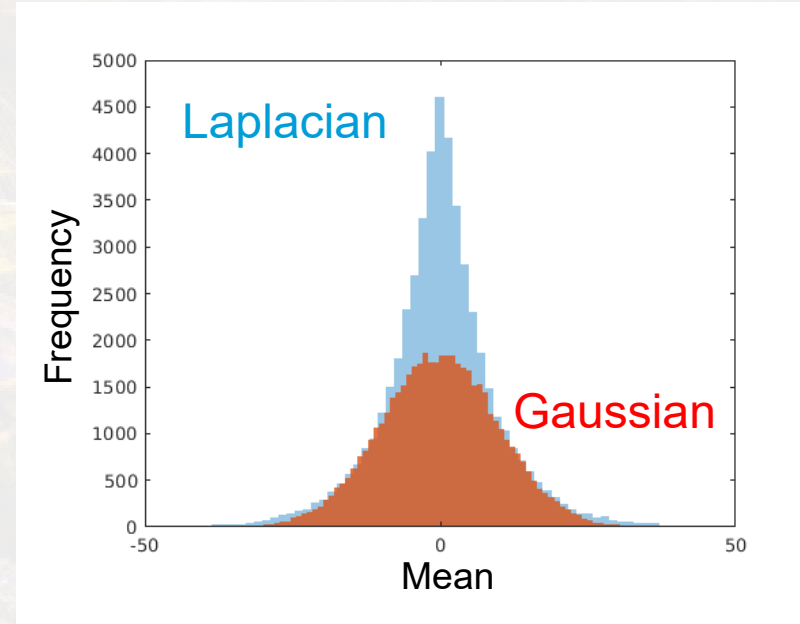
$$\delta I = \frac{\sqrt{(\delta H)^2 \sin^2 I + (\delta Z)^2 \cos^2 I}}{F}$$

$$\delta F = \sqrt{(\delta H)^2 \cos^2 I + (\delta Z)^2 \sin^2 I}$$

$$|\delta H = \sqrt{[(\delta X)^2 (\cos D)^2 + (\delta Y)^2 (\sin D)^2]}$$

Errors in magnetic data

- Errors in magnetic data are not Gaussian
 - $1\sigma = 68.3\%$
 - $2 \times 1\sigma = 95.4\%$
 - $3 \times 1\sigma = 99.7\%$, etc
- Usually, better described by Laplacian
 - $2 \times 1\sigma \neq 95.4\%$!
- To compute confidence intervals: sort the residuals, then *find* the 68.3%, 95.4% values
- Typically, CI 68.3% $< 1\sigma$; CI 95.4% $> 2\sigma$
- To be conservative: use CI 95.4% divided by 2; call this a **scalable 1 sigma equivalent**



Value of adding more SH degrees

Adding more resolution is better, *right?*

- Comparison with *independent* ground vector data reveals real signal being missed
- Adding more degrees is a diminishing *return on investment*

- Start with crustal field differences for the satellite era (1979 MAGSAT)
- Estimate the total uncertainty from various sources

**Mean absolute differences of
85000 global ground vector data 1900-2018**

Max degree/resolution	D (°)	I (°)	F (nT)
133/300 km	0.35	0.17	189
800/50 km	0.30	0.15	168
1440/28 km	0.29	0.15	165

1 sigma equiv (9300 global ground vector data 1979-2018)

1 sigma CI equiv	X (nT)	Y (nT)	Z (nT)
133/300 km	107	100	195
1440/28 km	90	91	185

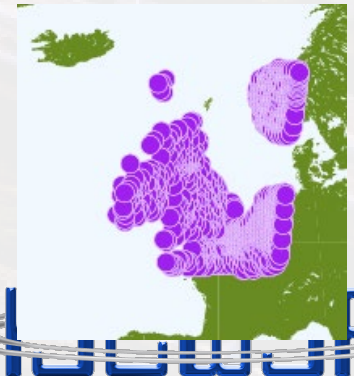
Crustal field uncertainties

1 sigma CI equiv.	X (nT)	Y (nT)	Z (nT)
1440/28 km	90	91	185

- These are global averages (include volcanoes etc.)
- Better to use a crustal field error estimates applicable for *hydrocarbon geology*, where appropriate.
- Compare IFR setups and ground shots in hydrocarbon areas (including e.g. Alberta) to HD model
- Derive a reducing scaling factor for hydrocarbon areas:

	X	Y	Z
Scaling factor (hydrocarbon)	0.66	0.75	0.85

North Sea fields and ground shots



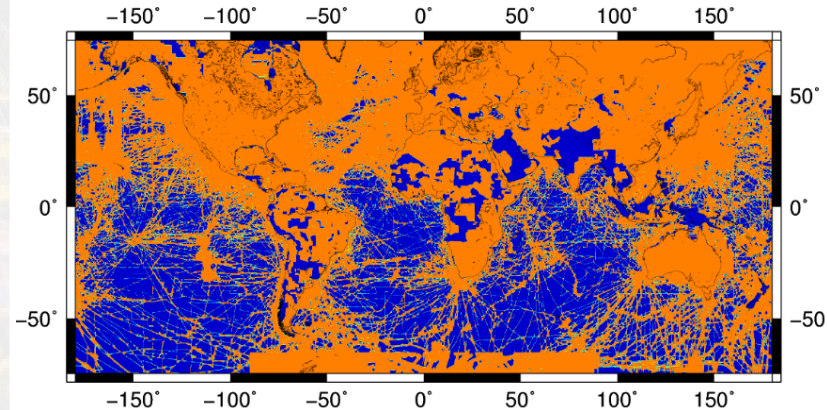
Data coverage

- High-degree magnetic field models based on airborne/shipborne surveys
- Other areas use satellite-only or other inferences
- Use this as a basis for introducing hydrocarbon scaling factor i.e.

Orange = use lower uncertainties

Blue = use higher uncertainties

WDMAM2



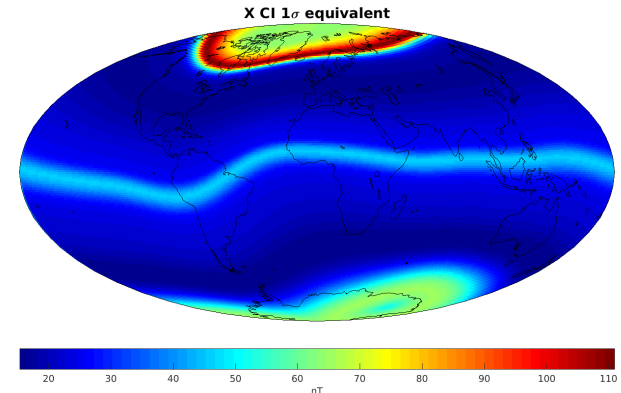
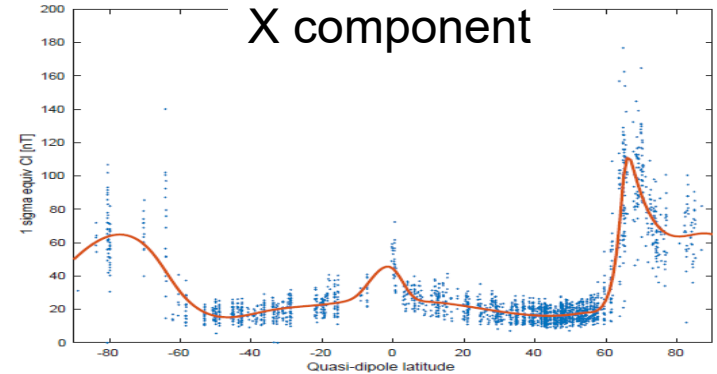
Orange = survey data

Blue = satellite only/model *pseudo-data*

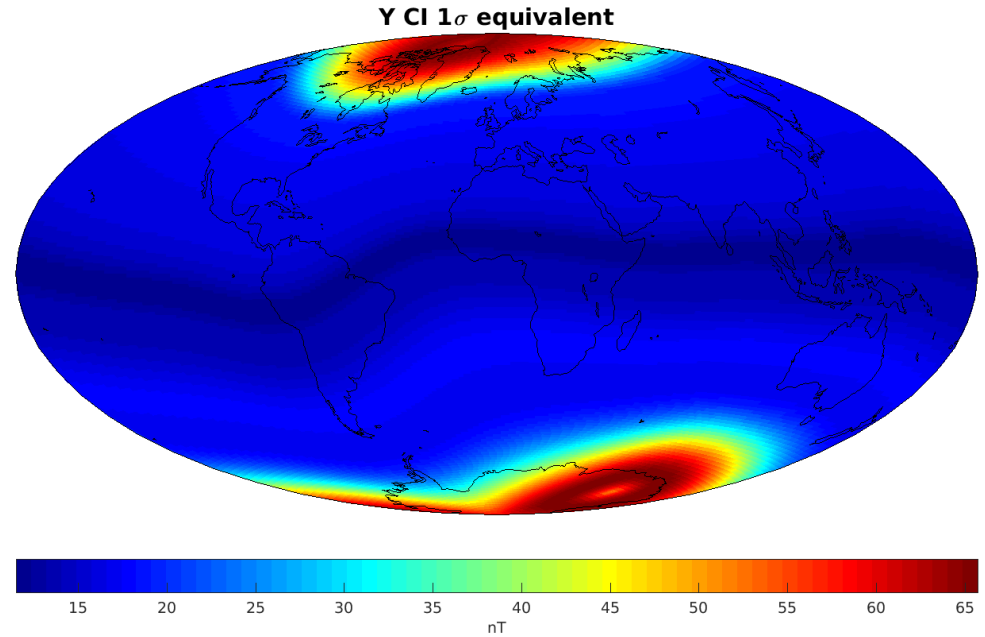
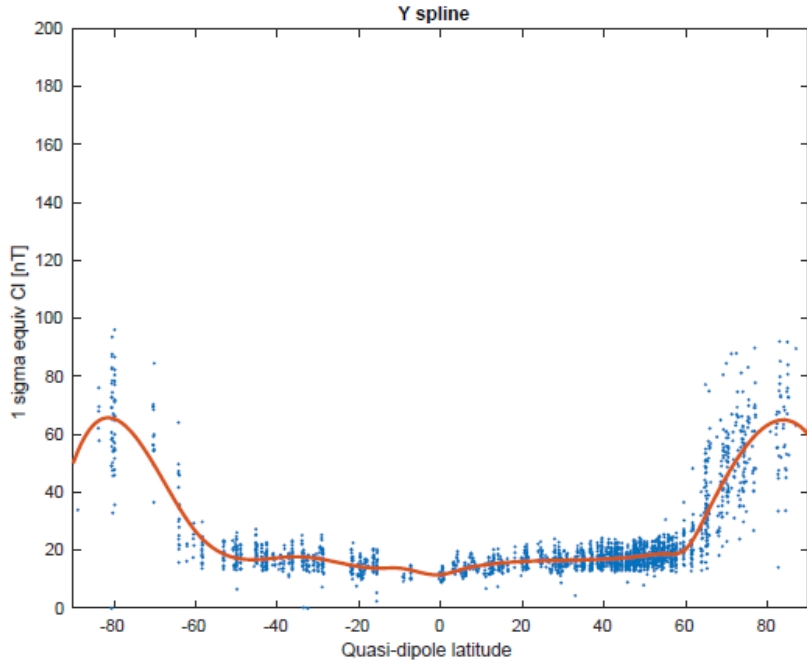
External field uncertainty

External fields:

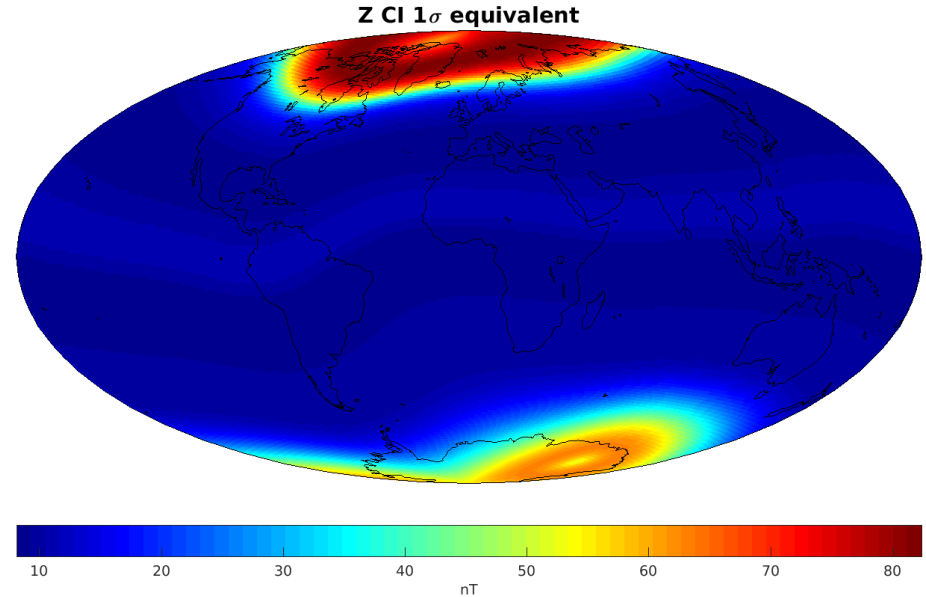
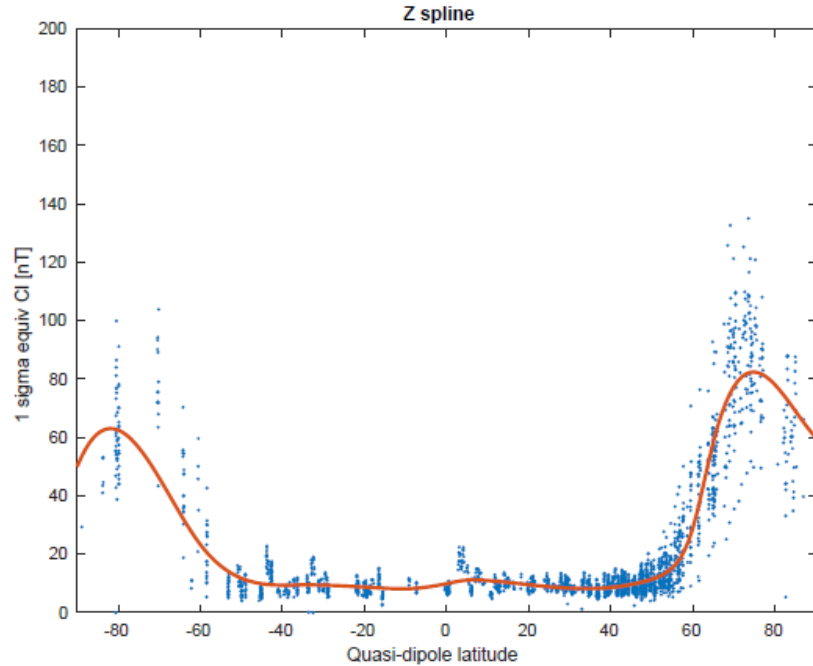
- Auroral electrojets; Equatorial electrojet; Geomagnetic storms
- Look at global observatories (1997-2018)
- Each year: collect XYZ minute mean data; remove core field and crustal offset; detrend; sort external field into 1/2/3 CI equivalents
- Organised in quasi-dipole (QD) coordinate system
- Fit spline in QD coords
- Convert to geographic coordinates



External field contribution - Y



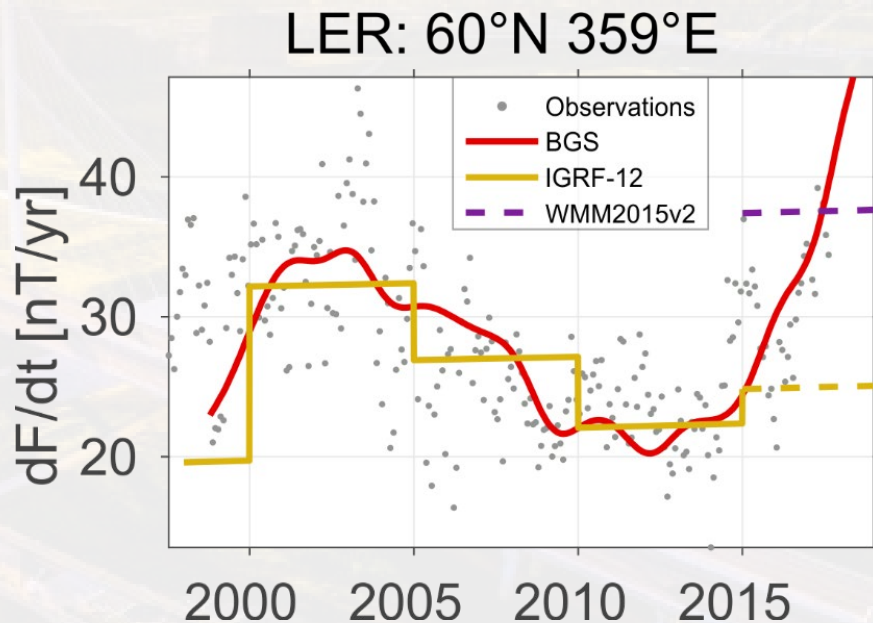
External field contribution - Z



Core field prediction uncertainty

- Errors in SV prediction assessed by comparing 1-year forecast of a core field, to the subsequent model release
- Difference is e.g. BGGM2015 at 2016.0 and BGGM2016
- Derive a scaling factor for annual 'look-ahead' uncertainty in satellite era
- Global RMS changes (small scale)

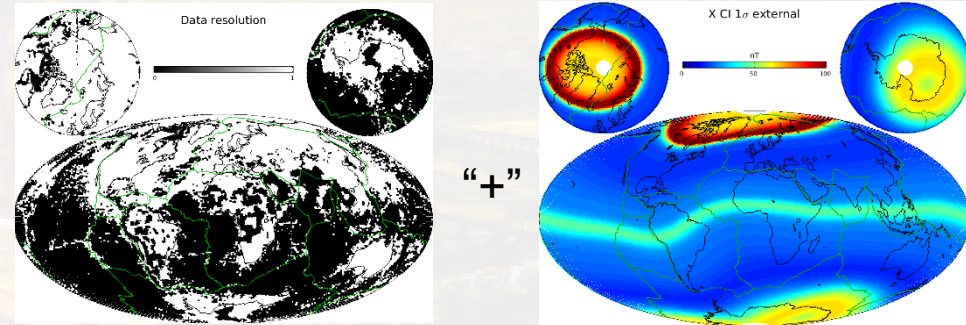
CI 1sigma equiv RMS (nT)	X	Y	Z
Uncertainty from forecasting	3	3	6



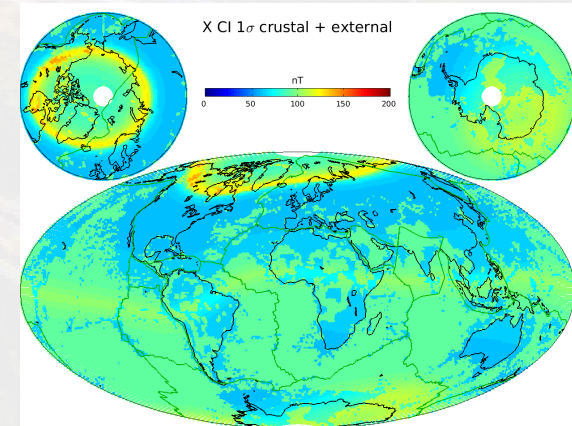
Combining the uncertainties

- Aiming for lat-long grid of useful **scalable 1-sigma error estimates**
- Robust spatial variations can only be obtained for the crustal field (with hydrocarbon area scaling) and external field
- Combine via Root Sum Square (as uncertainties are assumed independent)
- Scale by temporal variations for core field prediction uncertainties

Use main field model to obtain values for DIF from XYZ



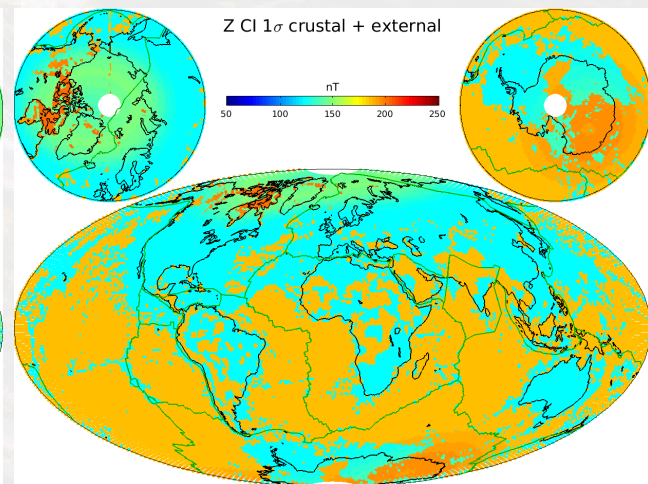
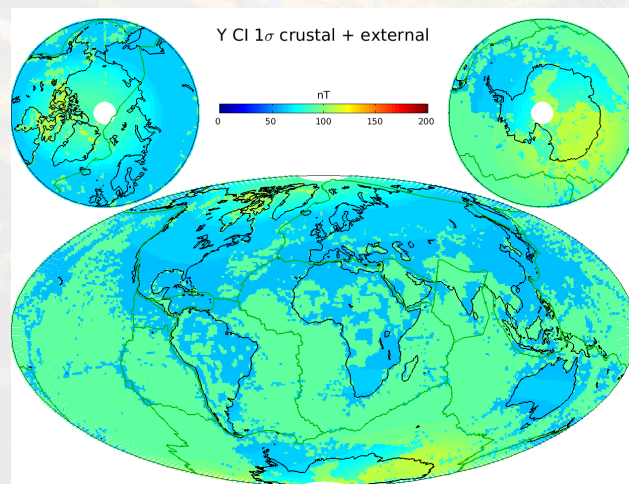
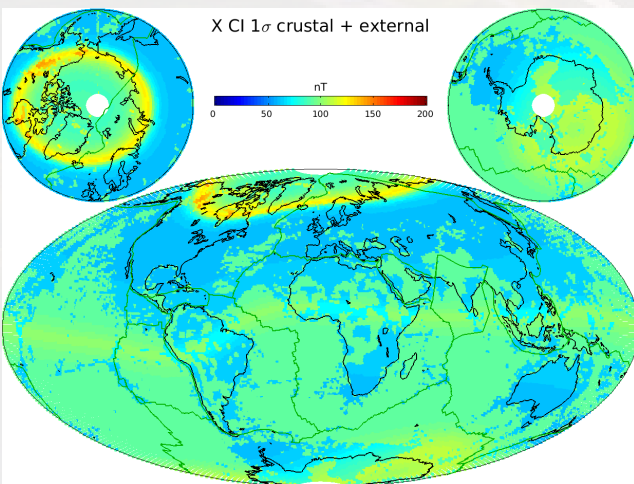
* *“Hydrocarbon scaling”*



Final CI 1 sigma equivalent values

1 sigma CI equiv.	X	Y	Z
L = 1440/28 km Global RMS* (nT)	86	82	160
Forecast scaling per year (%)	3.5	3.6	3.7

*not latitude weighted



Conversion to DIF

1 sigma CI equiv. RMS

Dec (°)

Inc (°)

F (nT)

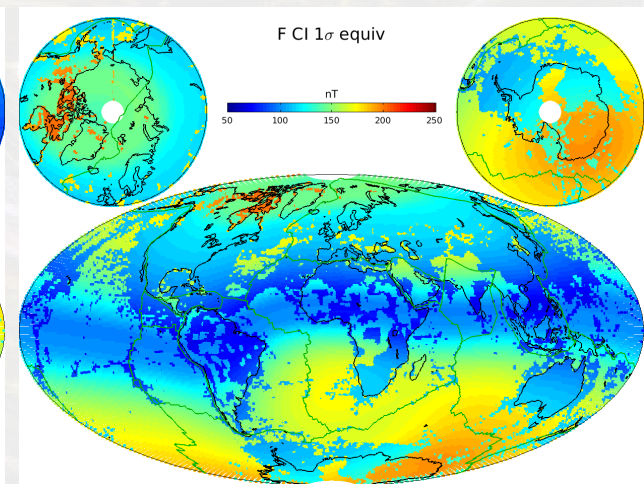
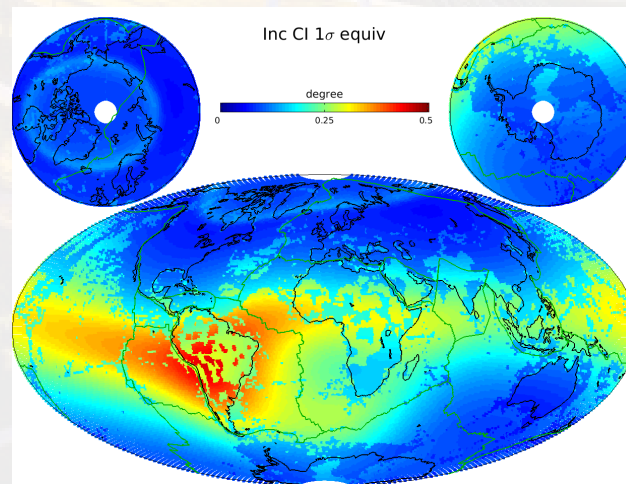
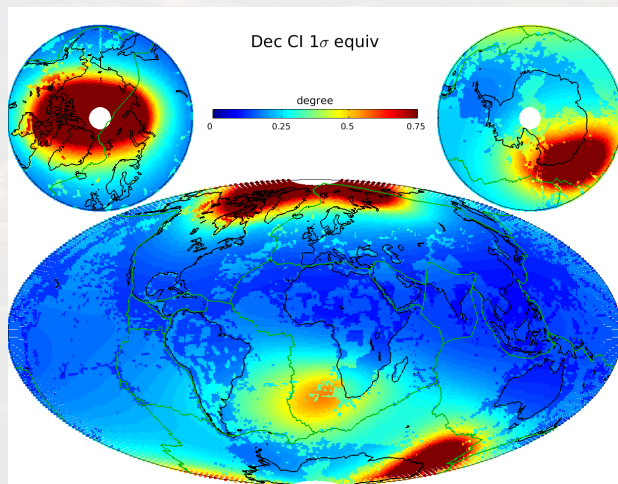
* latitude weighted

L = 1440/28 km*

0.22

0.15

91



Fit of Dec to DECG/DBHG

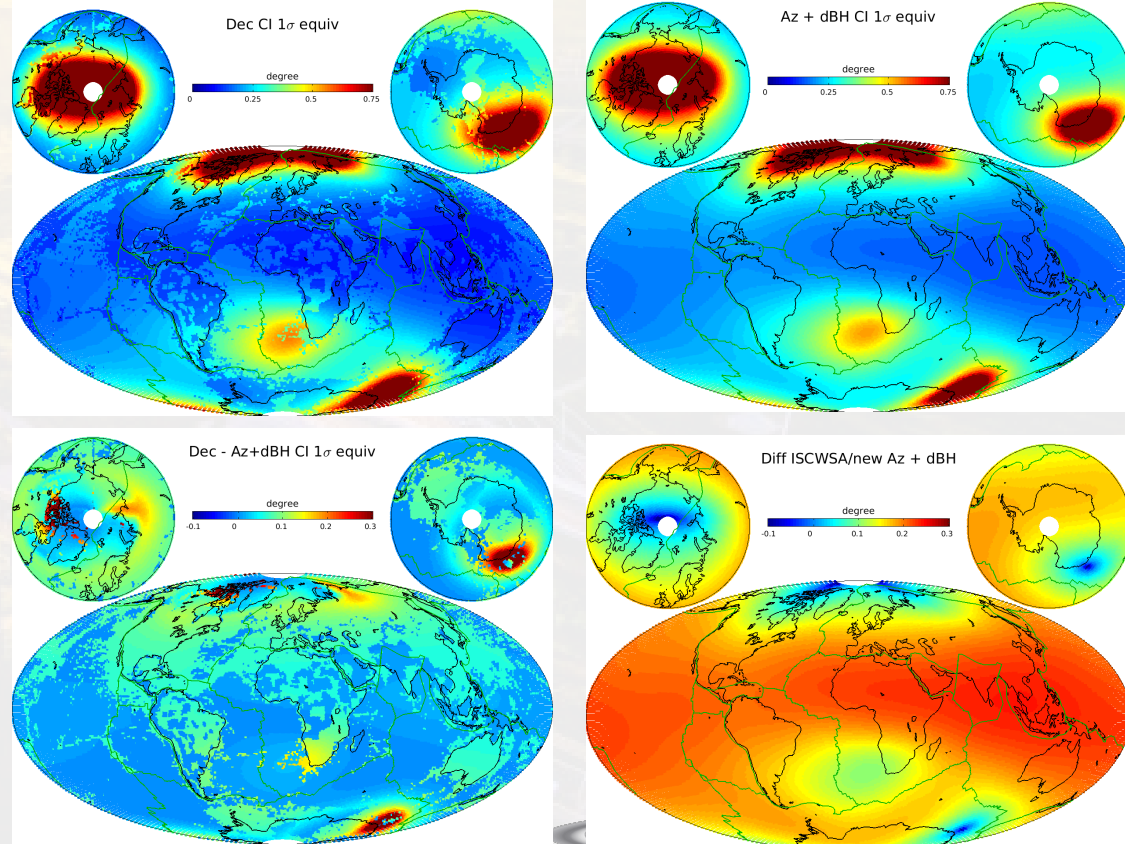
Can fit Dec CI to the ISCWSA 2 parameter model (Williamson, 2000)

Solve (least-squares) for:

$$Dec = \sqrt{DECG^2 + \frac{DBHG^2}{H^2}}$$

Best fit: 0.07° ; 5055° nT

- $DECG = 0.36^\circ$ (const)
- $DBHG = 5000^\circ \text{ nT}$ (H dependent)

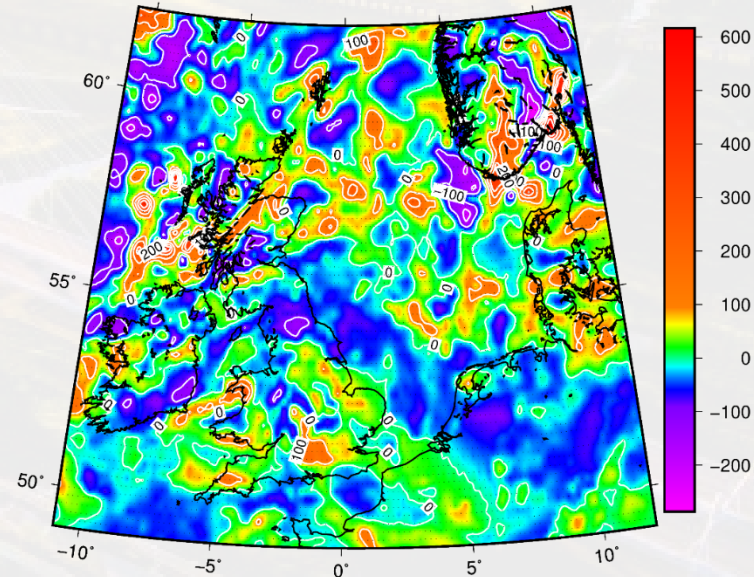


Conclusions

- Investigated uncertainties in high degree models
- Captures external fields, core field prediction, hydrocarbon crustal fields and more general data availability
- Available as XYZ or DIF uncertainties in a $1^\circ \times 1^\circ$ degree maps (with temporal scaling)
- Numbers are given as scalable 1-sigma equivalent uncertainties
- Some areas (Offshore SA) have larger uncertainties than expected

1 sigma CI equiv. RMS	X (nT)	Y (nT)	Z (nT)
L = 1440/28 km	86	82	160

L = 1440; Crustal field Z comp



Questions?

19

Thank you for listening